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# D. V. Boger Research Interests

- ❖ Viscoelastic Fluid Mechanics
- ❖ Particulate Fluids
- ❖ Environmental Rheology
- ❖ Hydrocolloids



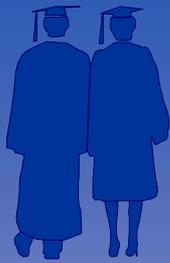
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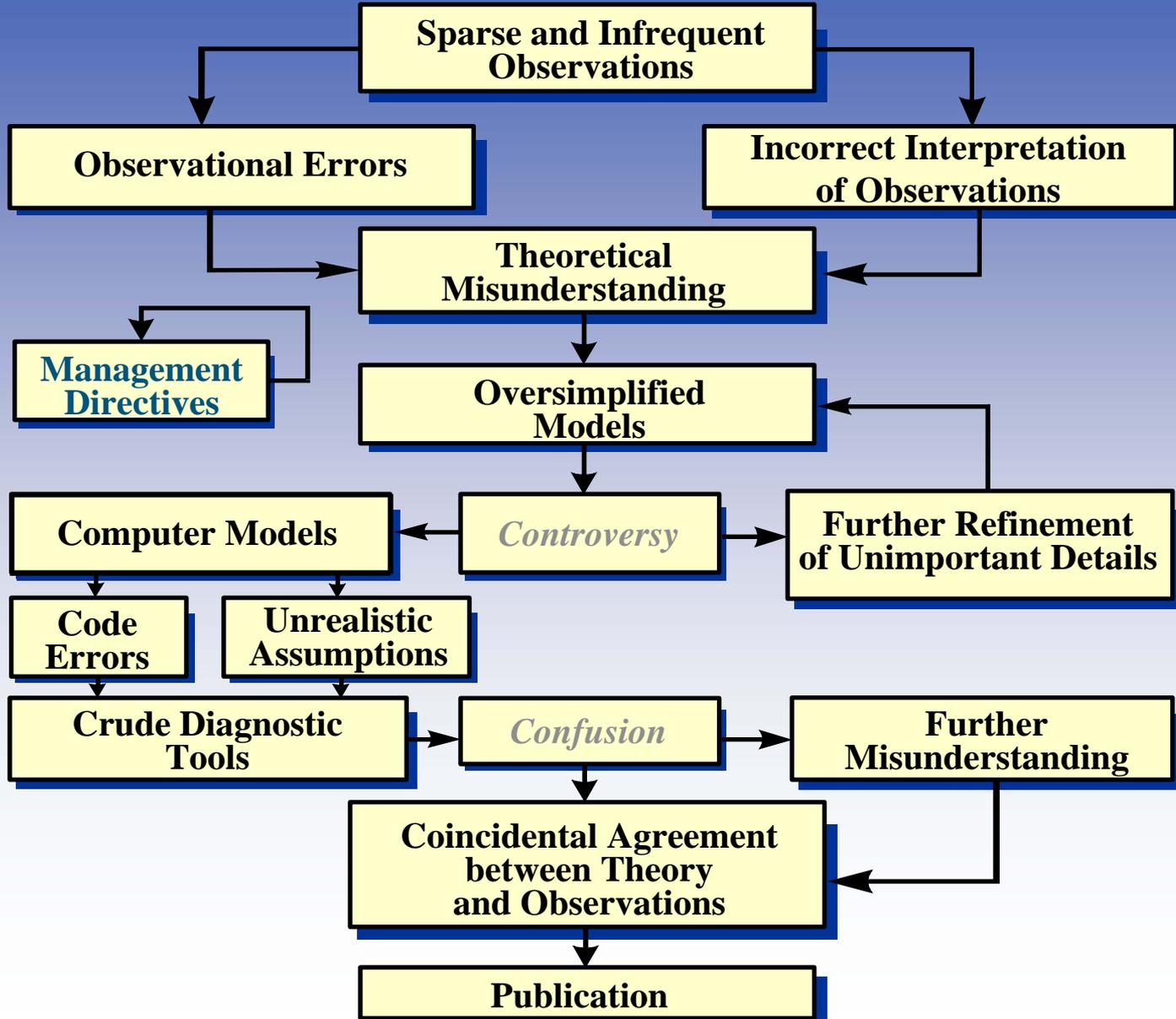
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# *The Course of Science*





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# The Rheology and Surface Chemistry of Slurries

**David V Boger**  
**Laureate Professor**  
**The University of Melbourne**  
**Australia**



# Particulate Fluids – Suspensions

- ❖ Settling Suspensions
- ❖ Non-Settling Suspensions

Ratio of Time Scales =  $N_{Se}$

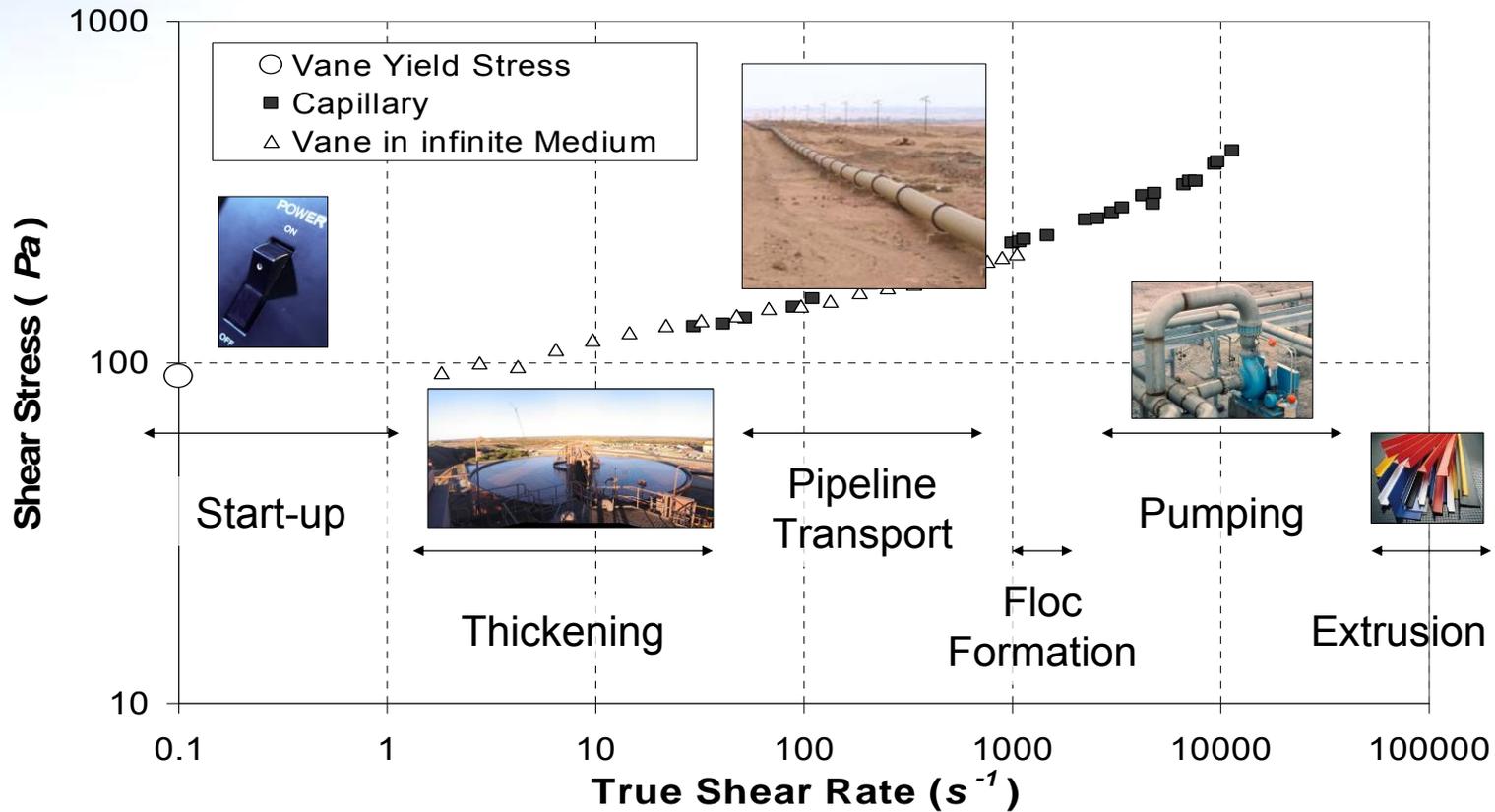
$$N_{Se} = \frac{\tau}{t_S}$$

$\tau$  = Characteristic time of the process

$t_S$  = Characteristic time of settling

$N_{Se} \ll 1$  Non-Settling (Rheology)

# Why do we want to Characterise Rheology?





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# Bauxite Residue Disposal

- 1974 - Alcoa of Australia (Consulting)
- 1978 - G. Sarmiento (Ph.D)
- 1983 - Q.D. Nguyen (Ph.D - Alcoa)
- 1986 - N.J. De Guingand (M.Eng.Sc - Alcoa)
- 1992 - PROBLEM SOLVED ?
- 1993 - N. Pashias (Ph.D - Alcoa)
- 2000 - F. Sofra (Ph.D - Alcoa)
- 2005 - D. Cooling (Ph.D - Alcoa)



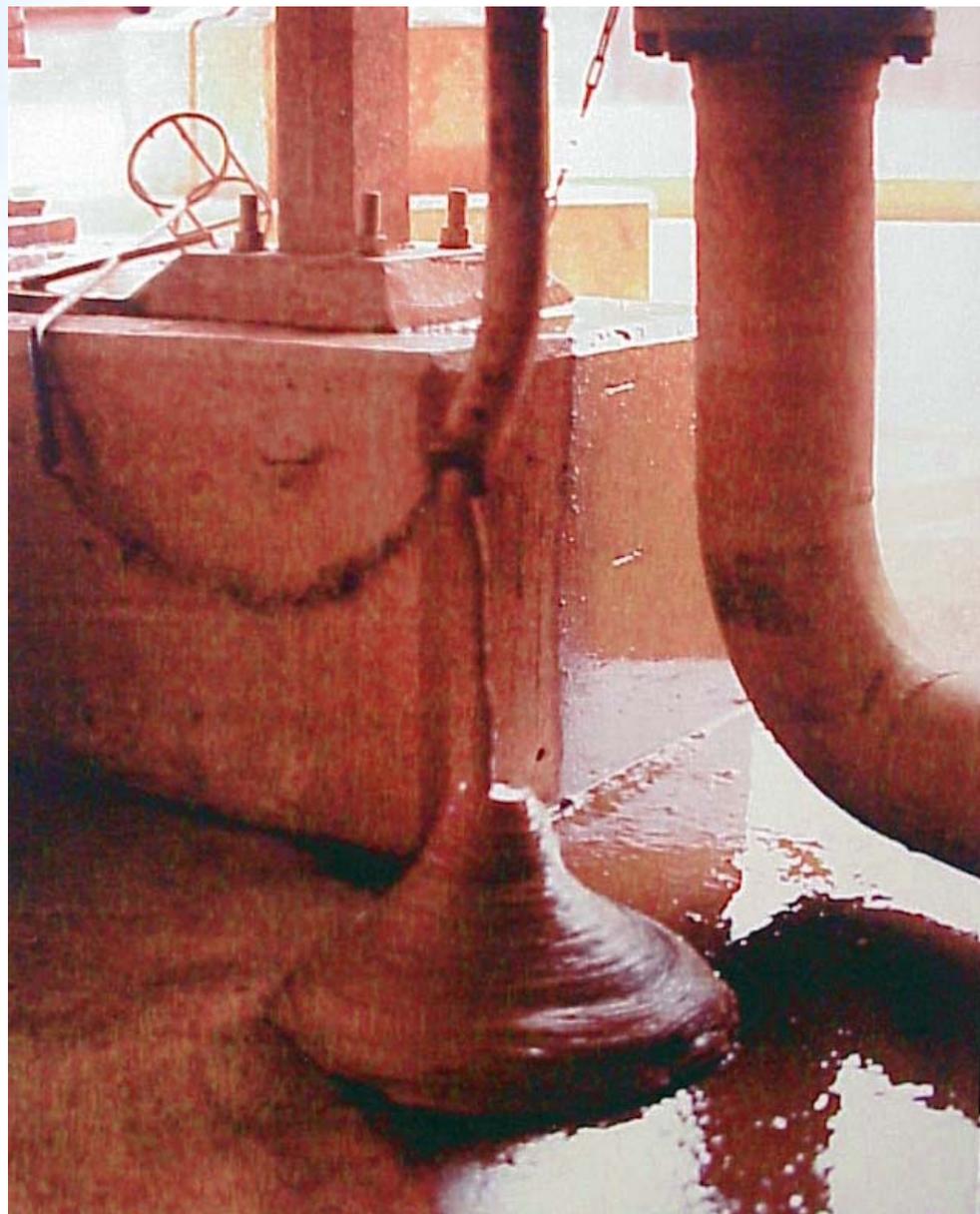
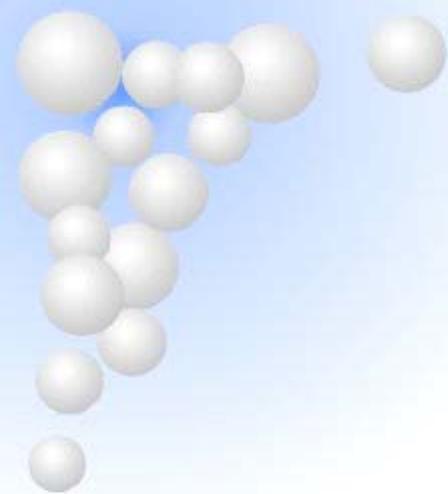


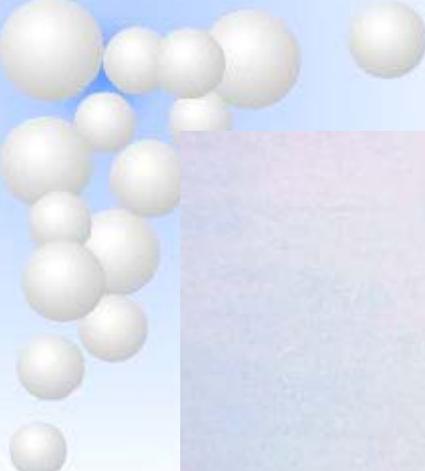
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# Exploiting the Rheology of Mineral Tailings

D.V.Boger

Particulate Fluids Processing Centre  
Department of Chemical & Biomolecular Engineering  
The University of Melbourne  
Victoria Australia





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# Environmental Rheology

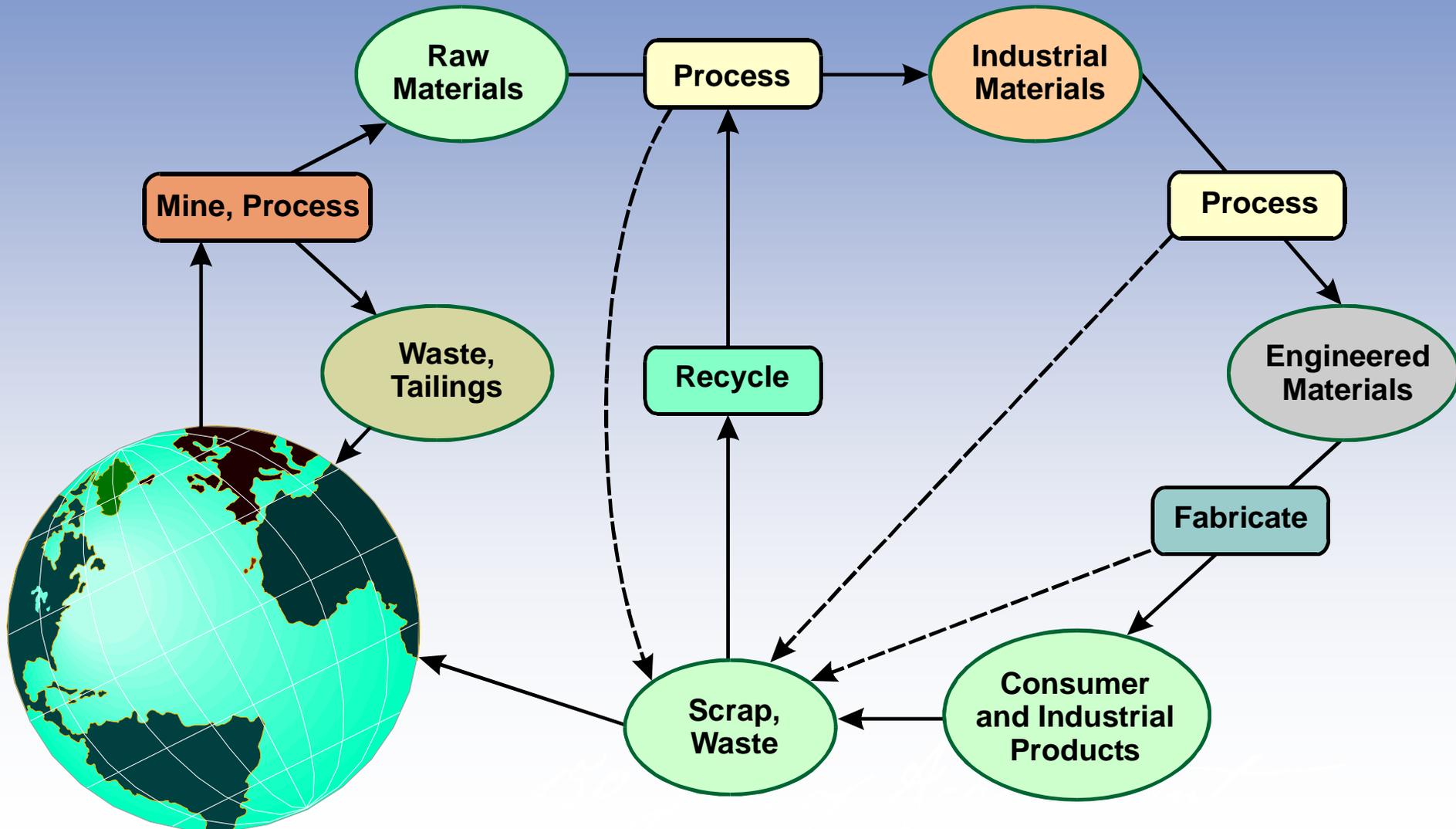
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# Sustainability, Recycling and Environmental Modelling





# Escondida

D. V. Boger

BHP Billiton Fellow



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# The Canadian Oil Sands Industry

“By 2010 the oil sands industry will be producing about one million barrels of oil per day from surface mined oil sands. This equates to about one million cubic metres of coarse tailings deposit per day and 0.2 to 0.3 million cubic metres of fine tailings per day. To date the industry has produced 400 million cubic metres of fine tailings.”

D.V.Boger

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Department of Chemical & Biomolecular Engineering  
The University of Melbourne  
Victoria Australia



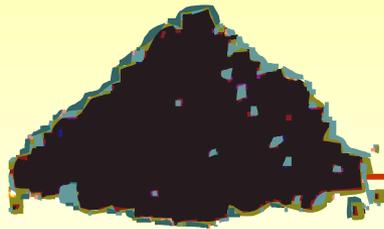
# *Oil Sands Tailings Deposition*



# Processing

# Products

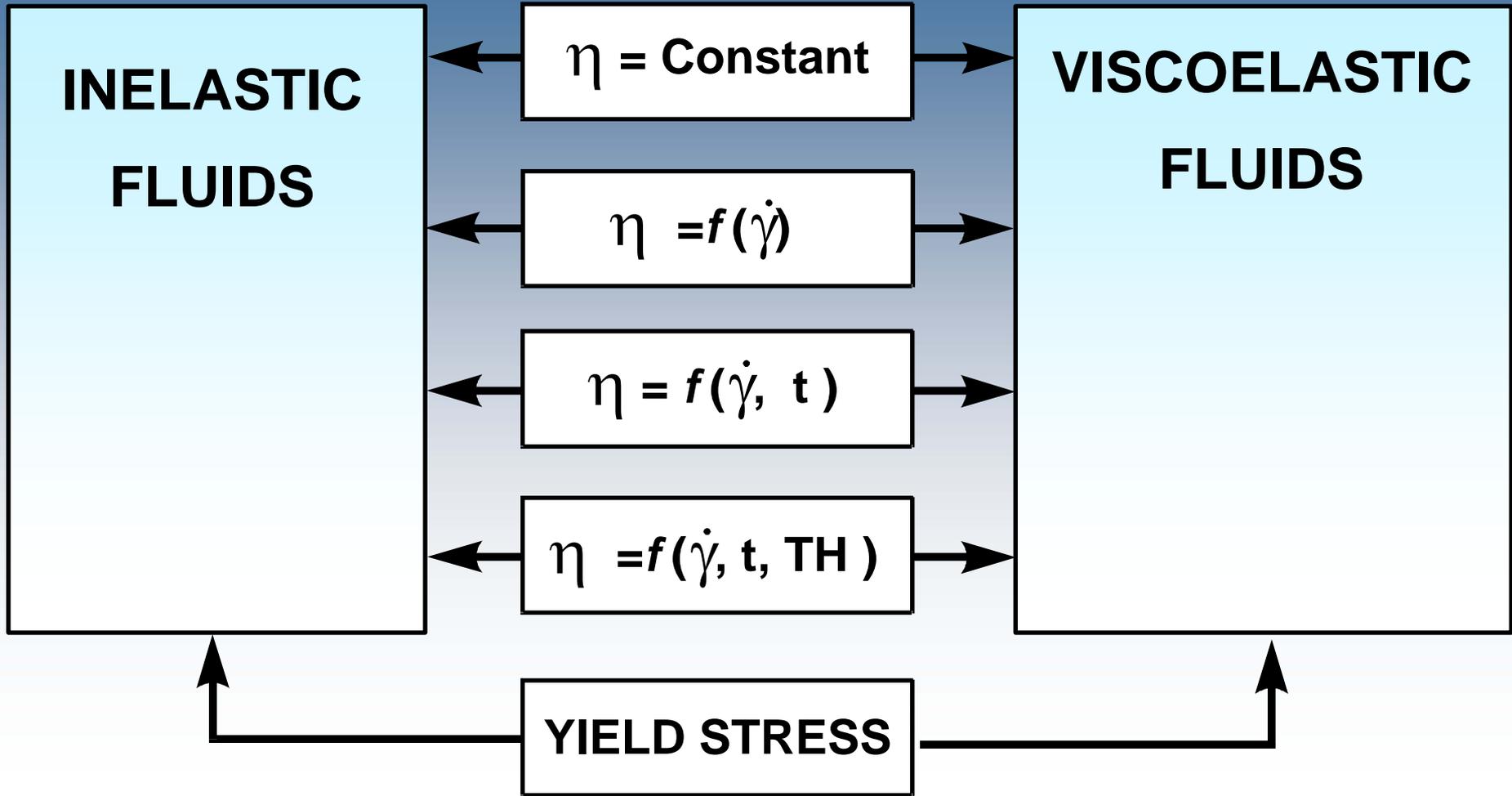
Ore



Tailings



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# Rheometry





# Developments motivated by applications in minerals industry

- The Vane Yield Stress Rheometer  
(J. Rheol., 27, 321, 1983; and 29, 335, 1985)
- The Conical Slump Test for Yield Stress Measurement (50 cent Rheometer)  
(J. Rheol., 40, 1119, 1996)
- The Bucket Rheometer  
(J. Rheol. *In press*, 2007)



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# *Yield Stress Measurement*

*D.V. Boger*

*Particulate Fluids Processing Centre  
Department of Chemical & Biomolecular Engineering  
The University of Melbourne  
Victoria Australia*



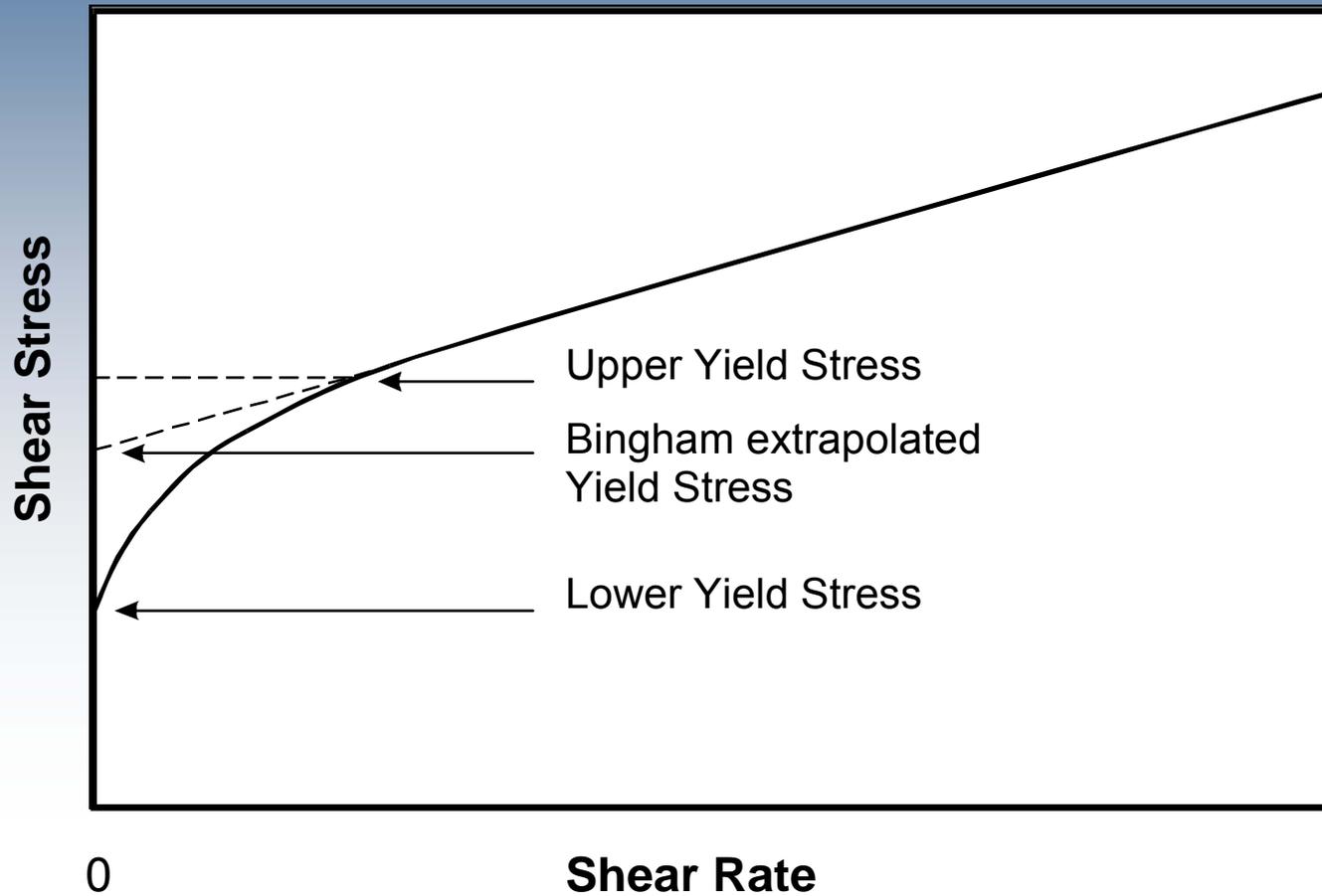


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# Typical Yield Stress Values

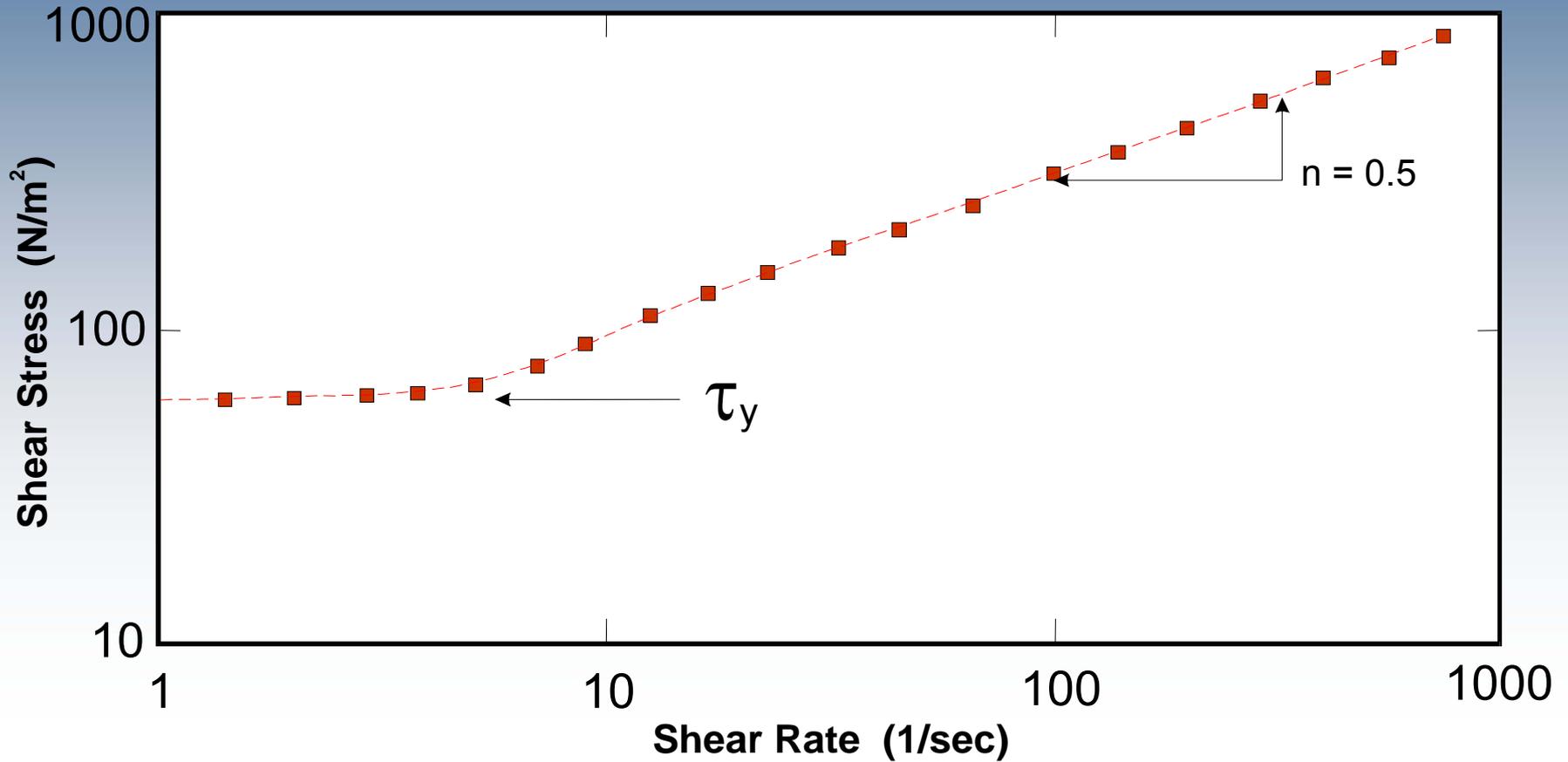
<b>Tomato Sauce (Rosella)</b>	<b>15 Pa</b>
<b>Yoghurt</b>	<b>80 Pa</b>
<b>Toothpaste</b>	<b>110 Pa</b>
<b>Peanut Butter</b>	<b>1900 Pa</b>
<b>Thickened Tailing Disposal</b>	<b>30-100 Pa</b>
<b>Mine Stope Fill</b>	<b>250-800 Pa</b>

# The Yield Stress

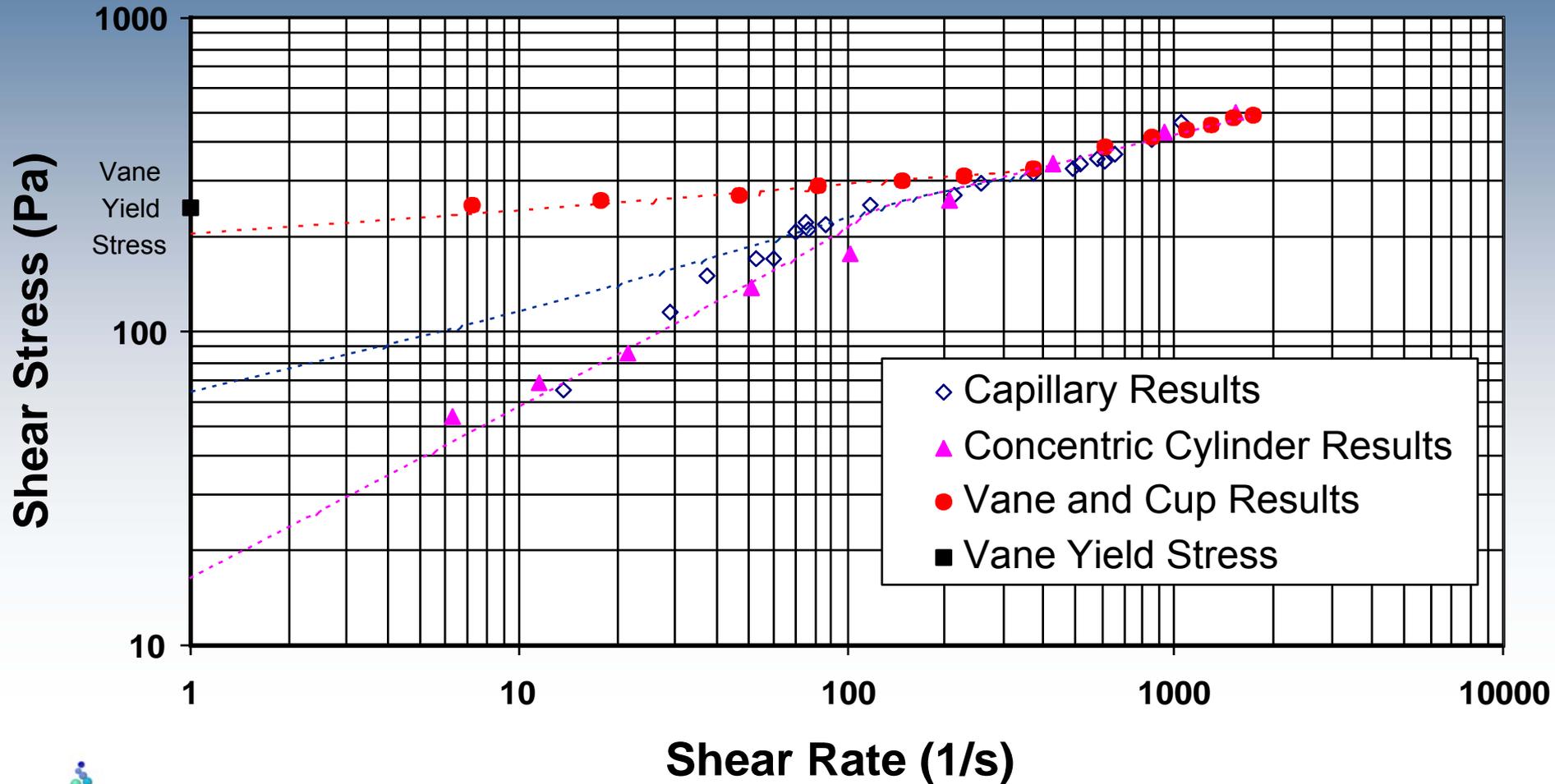


# Tomato Soup Concentrate

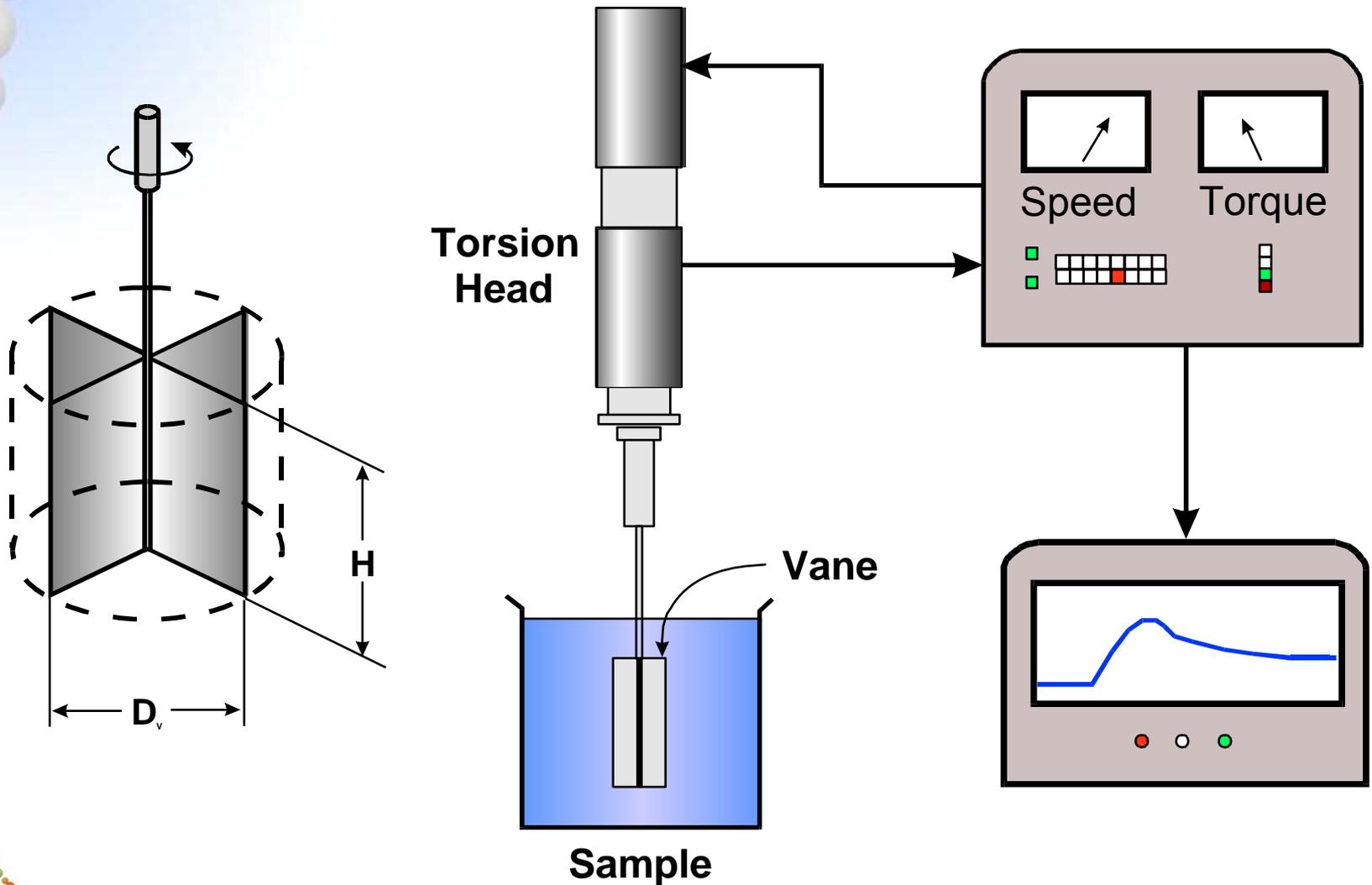
Temperature 20°C



# Flow Curves for Paste Sample - Yield Stress = 250 Pa



# Vane Technique



# The Vane Method

$$T_m = (\pi dl) \frac{d}{2} \tau_y + 4\pi \int_0^{d/2} \tau_e(r) r^2 dr$$

If  $\tau_e = \tau_y$  then

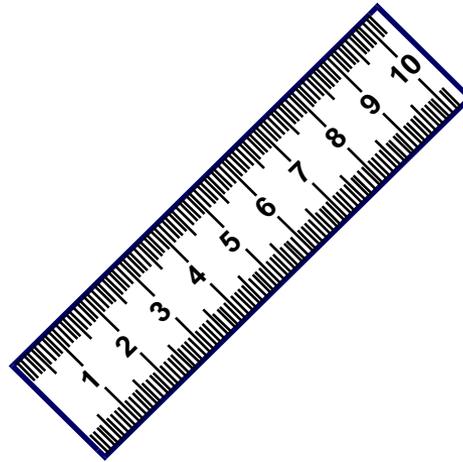
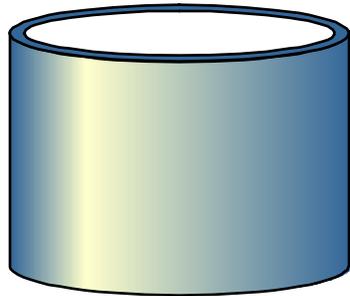
$$T_m = \frac{\pi}{2} d^3 \left( \frac{1}{d} + \frac{1}{3} \right) \tau_y$$

“Yield Stress Measurement for Concentrated Suspensions”  
(with Q.D. Nguyen), J. of Rheology, 27, 321 (1983)”

“Direct Yield Stress Measurement with the Vane Method”  
(with Q.D. Nguyen), J. of Rheology, 29, 335 (1985)”



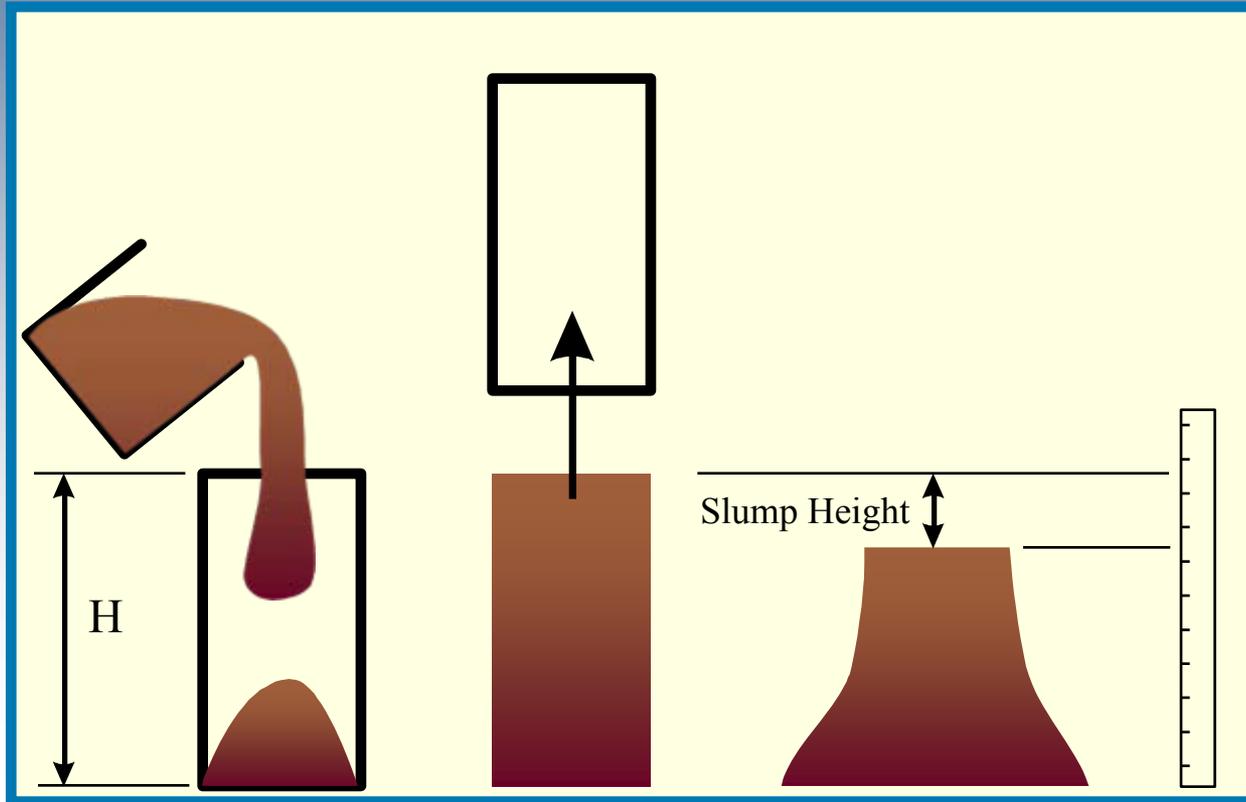
“D#Iw#Ehw#khpwhu#ru  
\\hg#whw#P hdxhphw”



M#khrd#73+9, #14:<#1<9



# The Slump Test



1. Fill slump mould
2. Remove mould vertically
3. Measure distance between mould and top of sample

# Slump Test

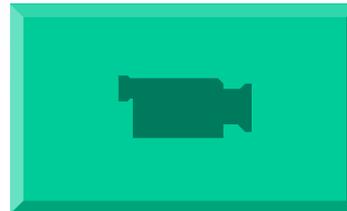
**Approximate Result:**

$$\tau'_y = \frac{1}{2} + \frac{1}{2} \sqrt{S'}$$

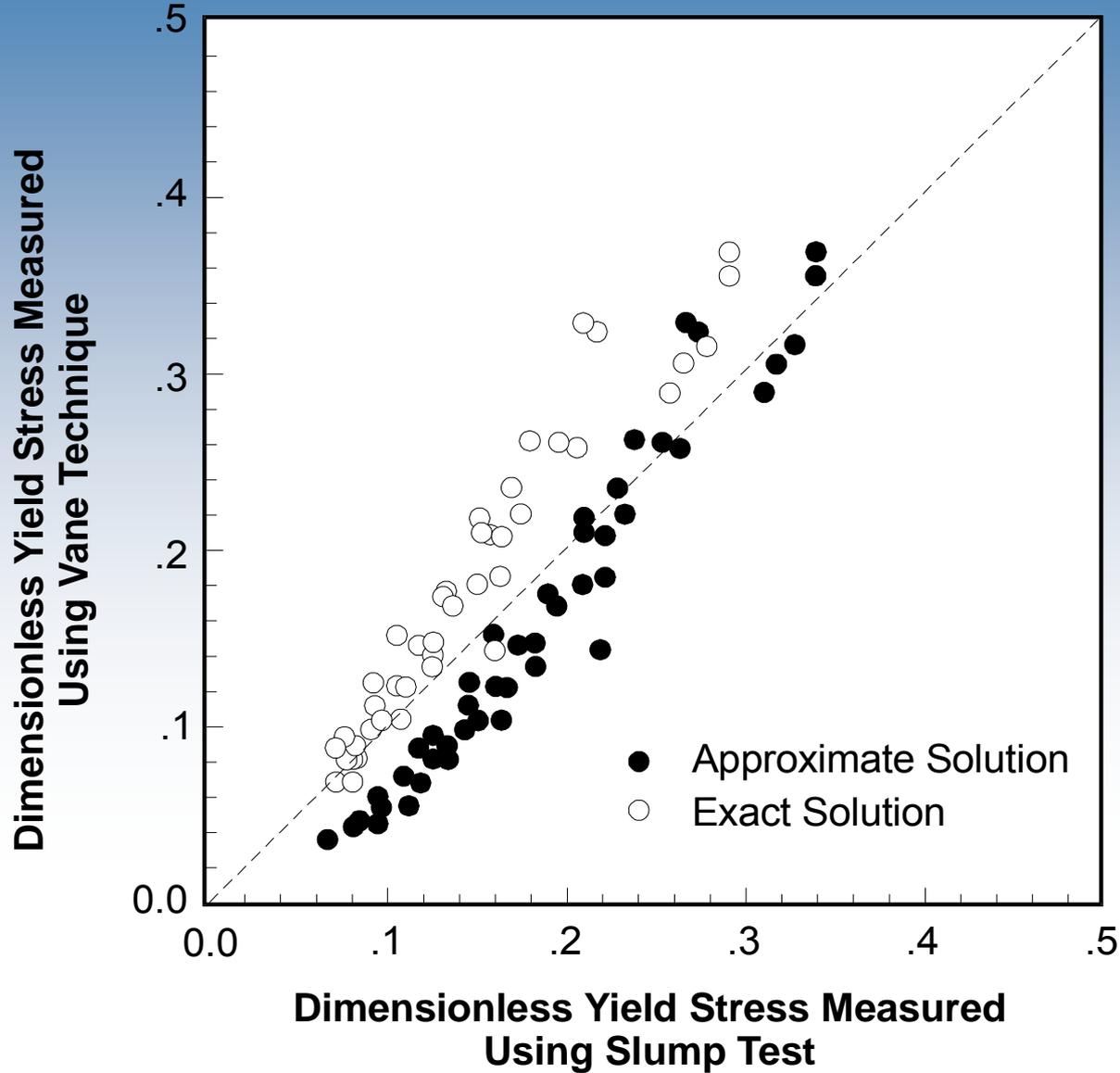
# The Fifty Cent Rheometer

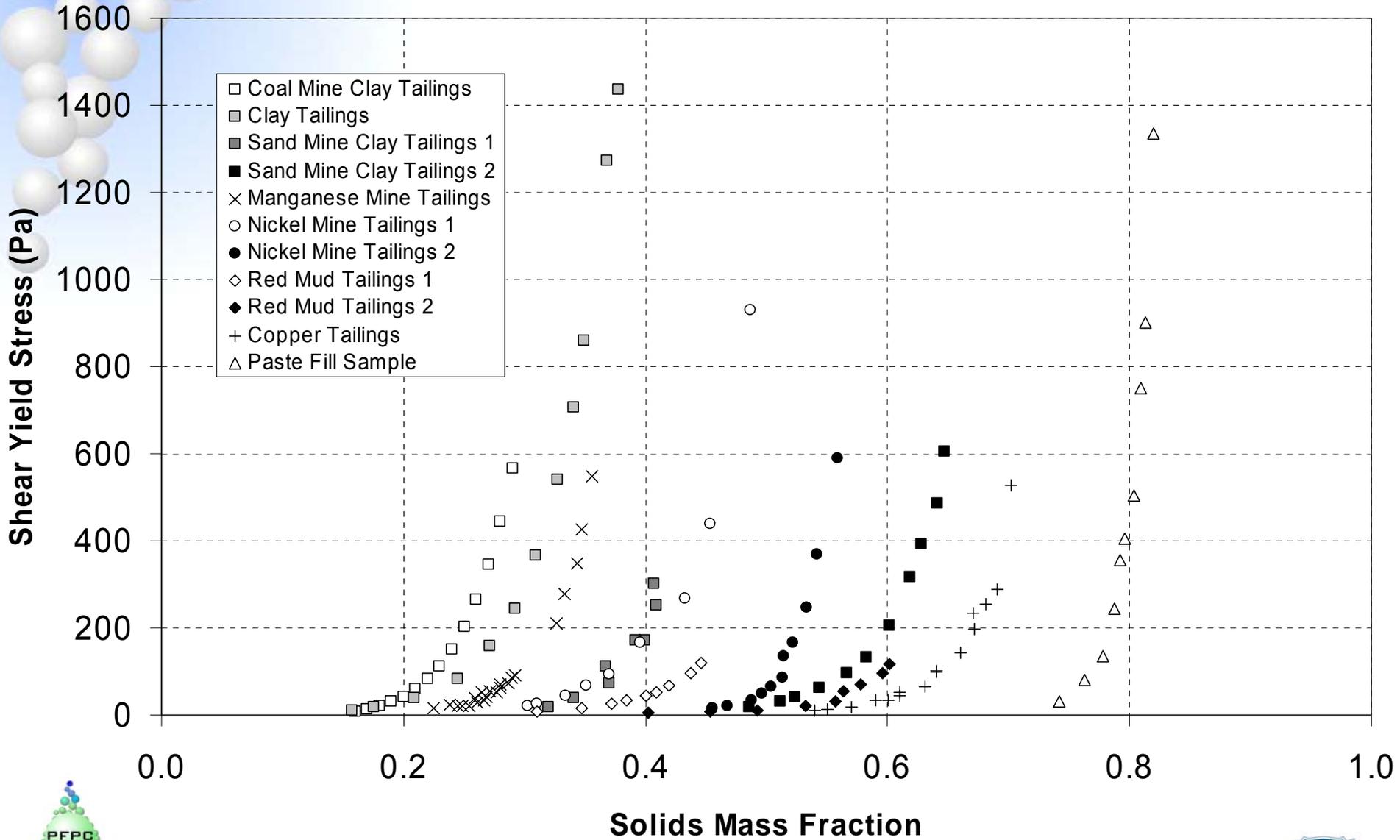
D.V. Boger  
N. Pashals

D.J. Glenister  
J. Summers



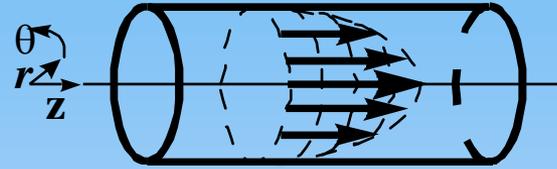
# Comparison of Yield Stress Measuring Techniques



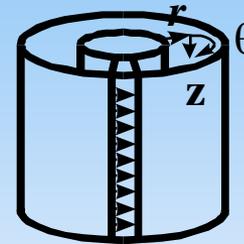


# Viscometric flows used for viscosity measurement

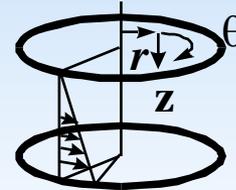
Poiseuille Flow



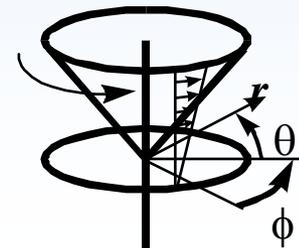
Couette Flow



Parallel Plate Torsion

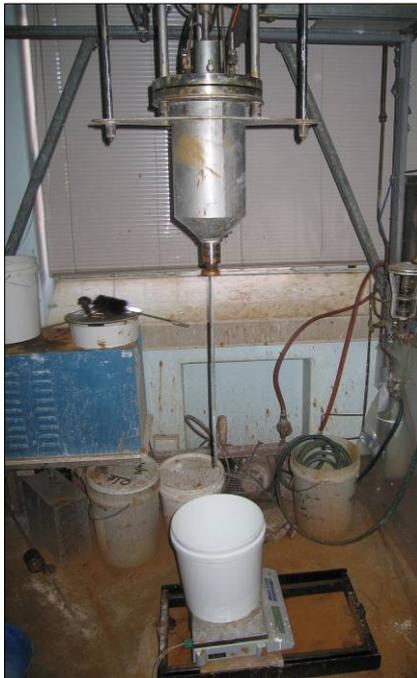


Cone and Plate Torsion

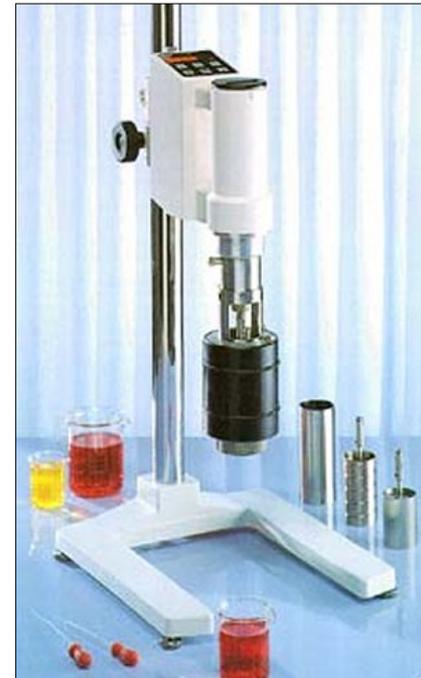


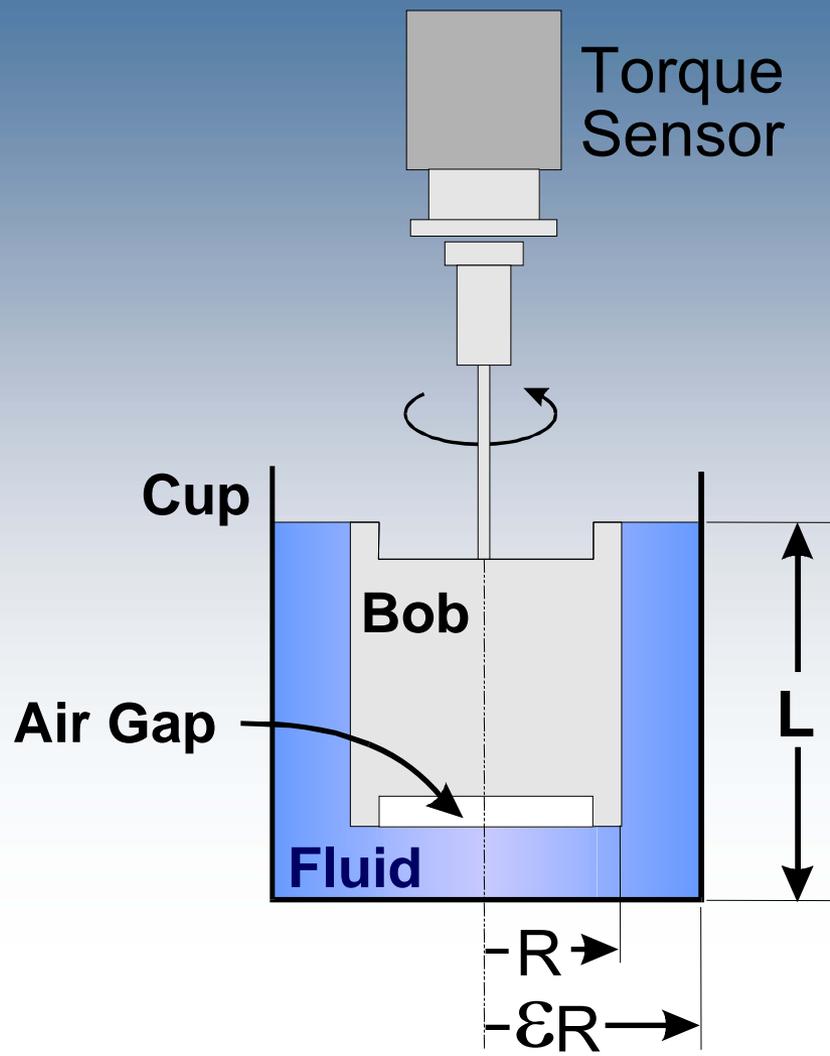
# Current Methods of Characterisation

## Capillary Rheometry



## Rotational Rheometry





# Couette Viscometry

**Basic Equations:**  $\dot{\gamma} = f(\tau) = - r d\omega / dr$

$$\tau = T / 2\pi L r^2$$

$$\tau_1 = T / 2\pi L R^2 = \varepsilon^2 \tau_2$$

$$\Omega = \int_{\tau_2}^{\tau_1} \frac{f(\tau)}{2\tau} d\tau$$

where  $\tau_1$  and  $\tau_2$  are the shear stress at the surfaces of the bob ( $r=R$ ) and the cup ( $r=\varepsilon R$ ), respectively.

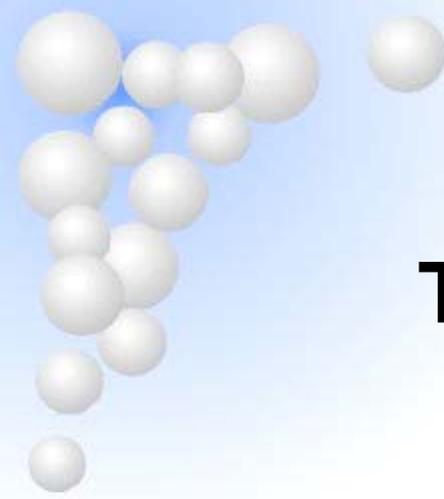
**Newtonian Fluid:**

$$\dot{\gamma}_1 = f(\tau_1) = 2\Omega / (1 - \varepsilon^{-2})$$



# Overview of the Problem

- Samples are not stable over time.
- Some testing methods are susceptible to particle size effects.
- Slip between the sample and the shearing interface can occur.
- Some instrumentation is very large and not portable.



# THE BUCKET RHEOMETER FOR THE VISCOSITY CHARACTERISATION OF YIELD STRESS SUSPENSIONS

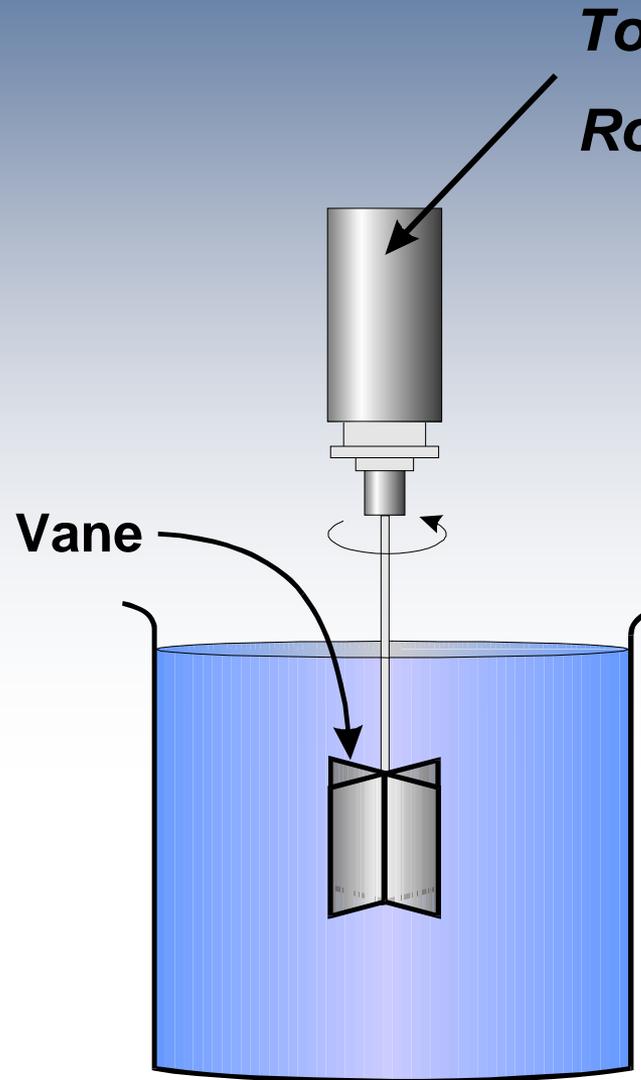
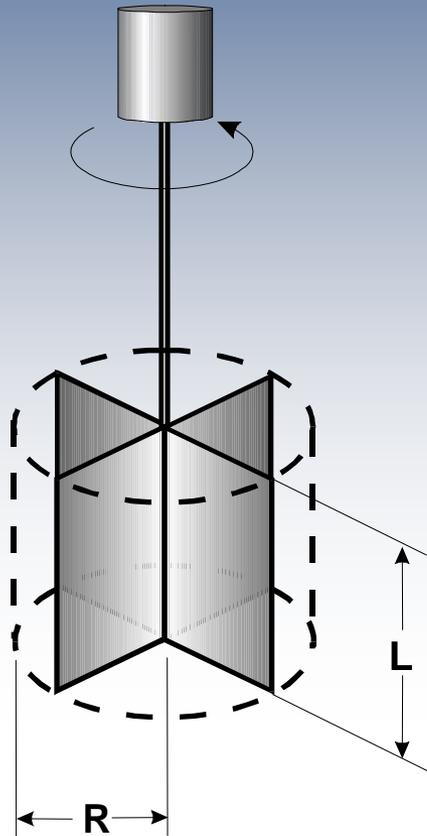
Daniel T. Fisher

Professor Peter J. Scales

Laureate Professor David V. Boger



# The Bucket Rheometer



**Torque (T)**

**Rotational Speed ( $\Omega$ )**

**Shear Stress:**

$$\tau = \frac{T}{2\pi LR}$$

where  $R$  = vane radius

$L$  = vane height

**Shear Rate:**

$$\dot{\gamma} = \frac{2\Omega}{S}$$

where  $S = \frac{d \ln T}{d \ln \Omega}$

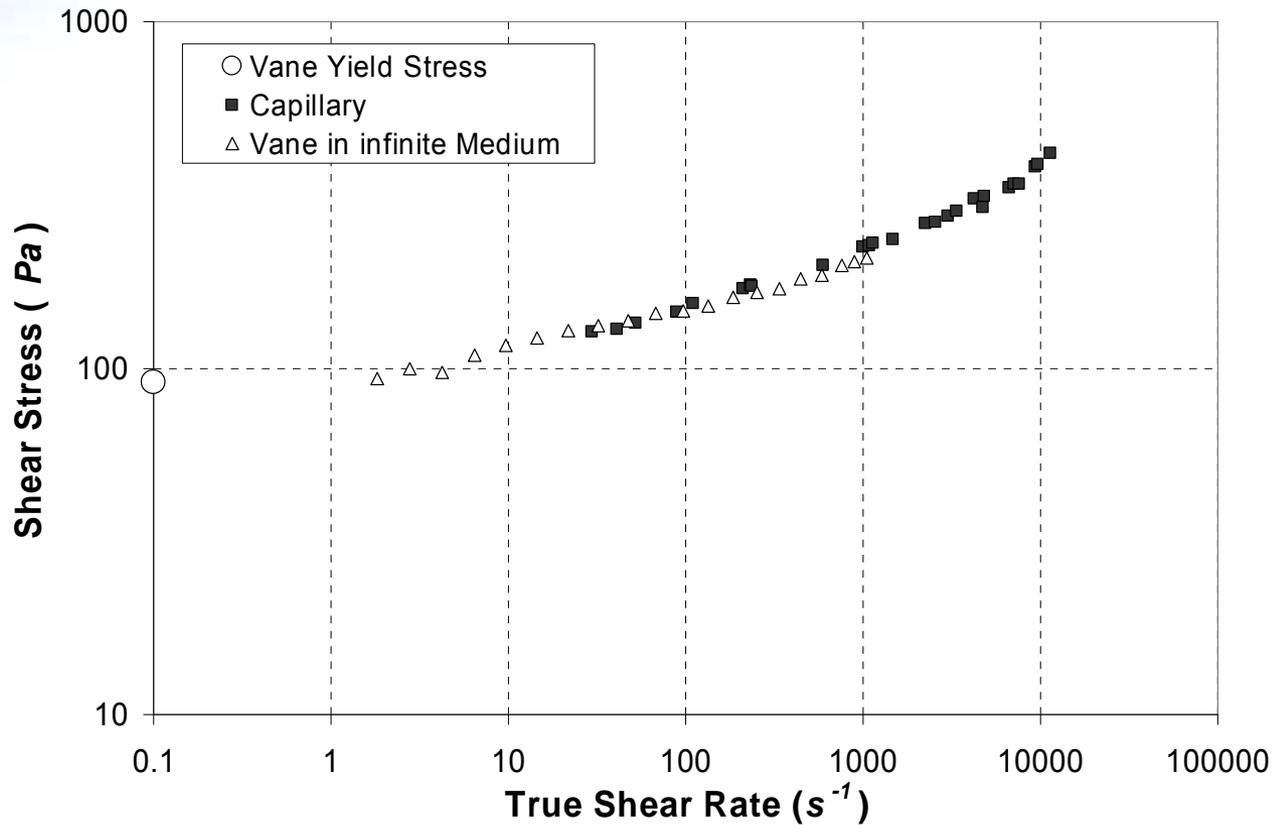


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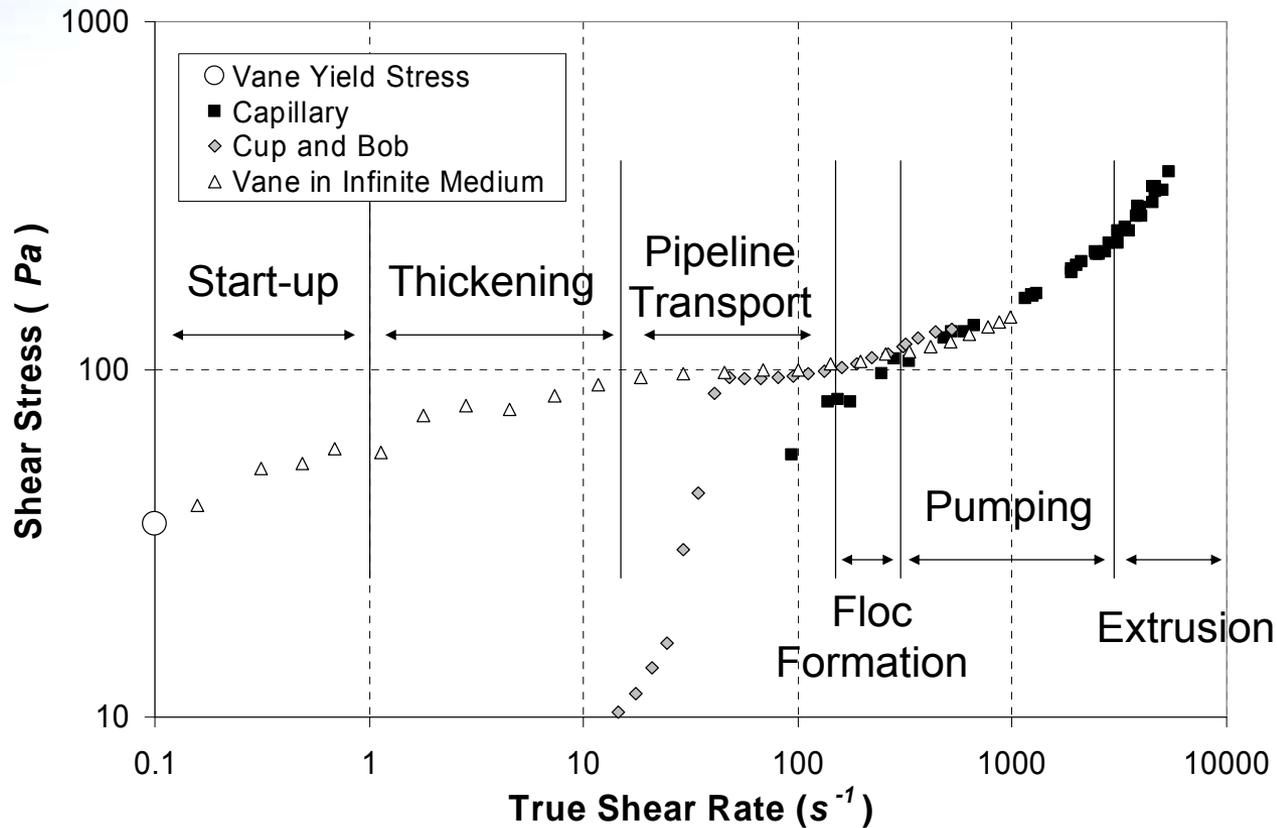
# Alumina Paste (AKP50)

50.2%w/w and pH 7.60



# Transitional Limonite Slurry

45.1%w/w and pH 6.34





# *Ideal Particulate Fluids*

*D.V. Boger*

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# Rheology of Suspensions

## DEFINITIONS:

### Relative Viscosity

$$\eta_r = \frac{\eta}{\eta_0} = 1 + \overset{\text{Einstein}}{\downarrow} 2.5\phi + 6.2\phi^2 + O(\phi^3)$$

$\uparrow$   
*Bachelor*

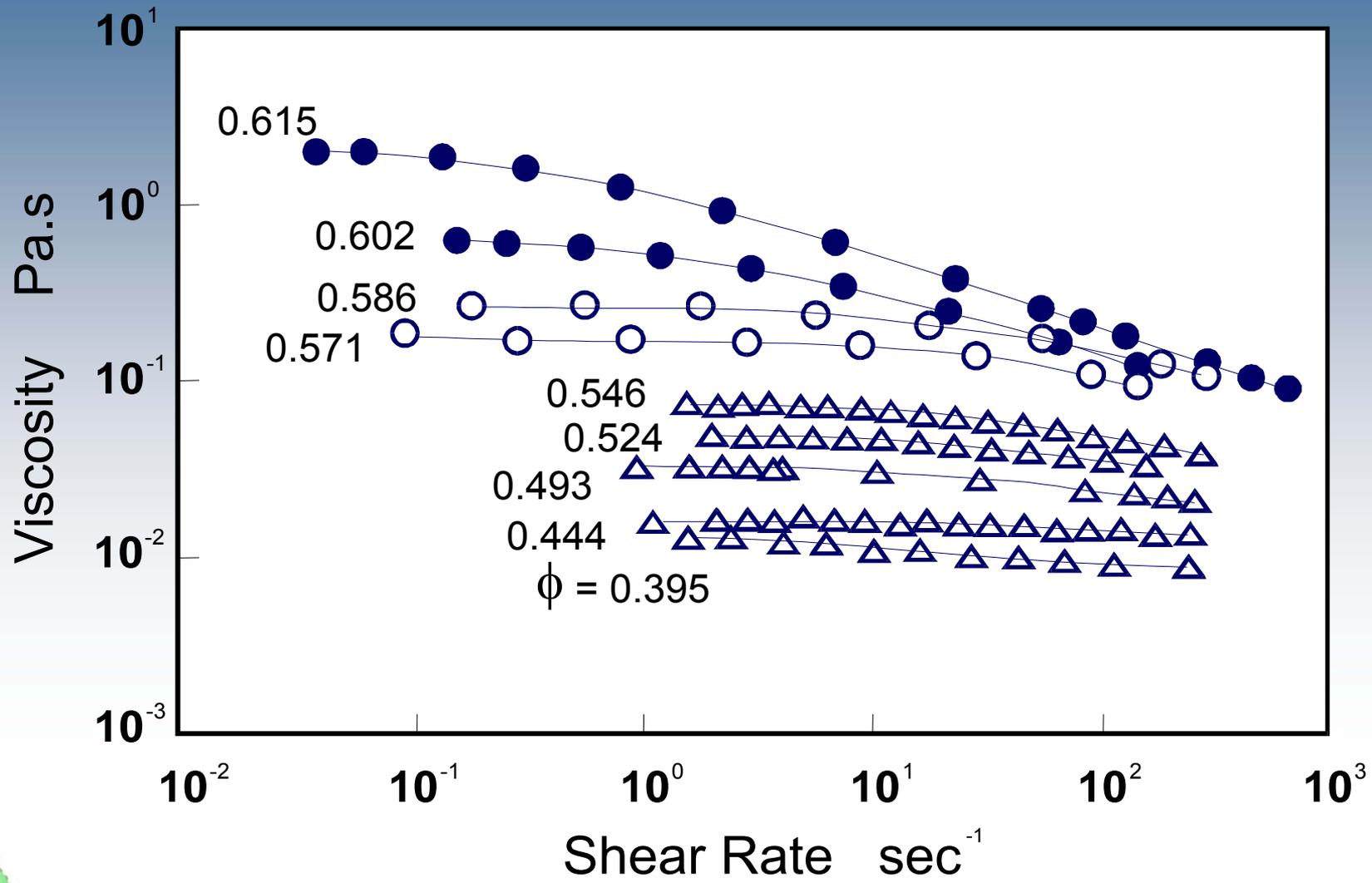
### Specific Viscosity

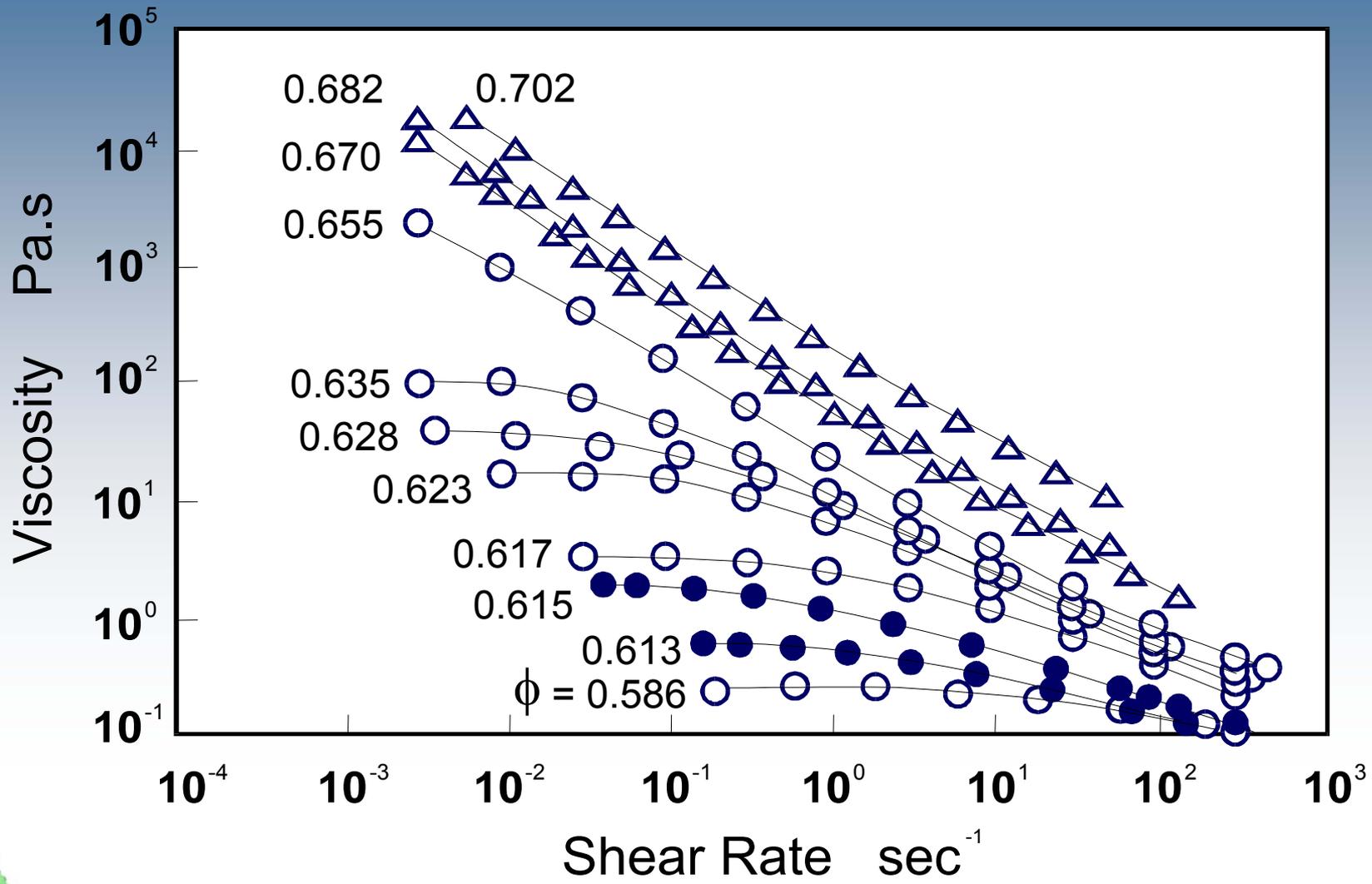
$$\eta_{sp} = \eta_r - 1 = \frac{\eta - \eta_0}{\eta_0}$$

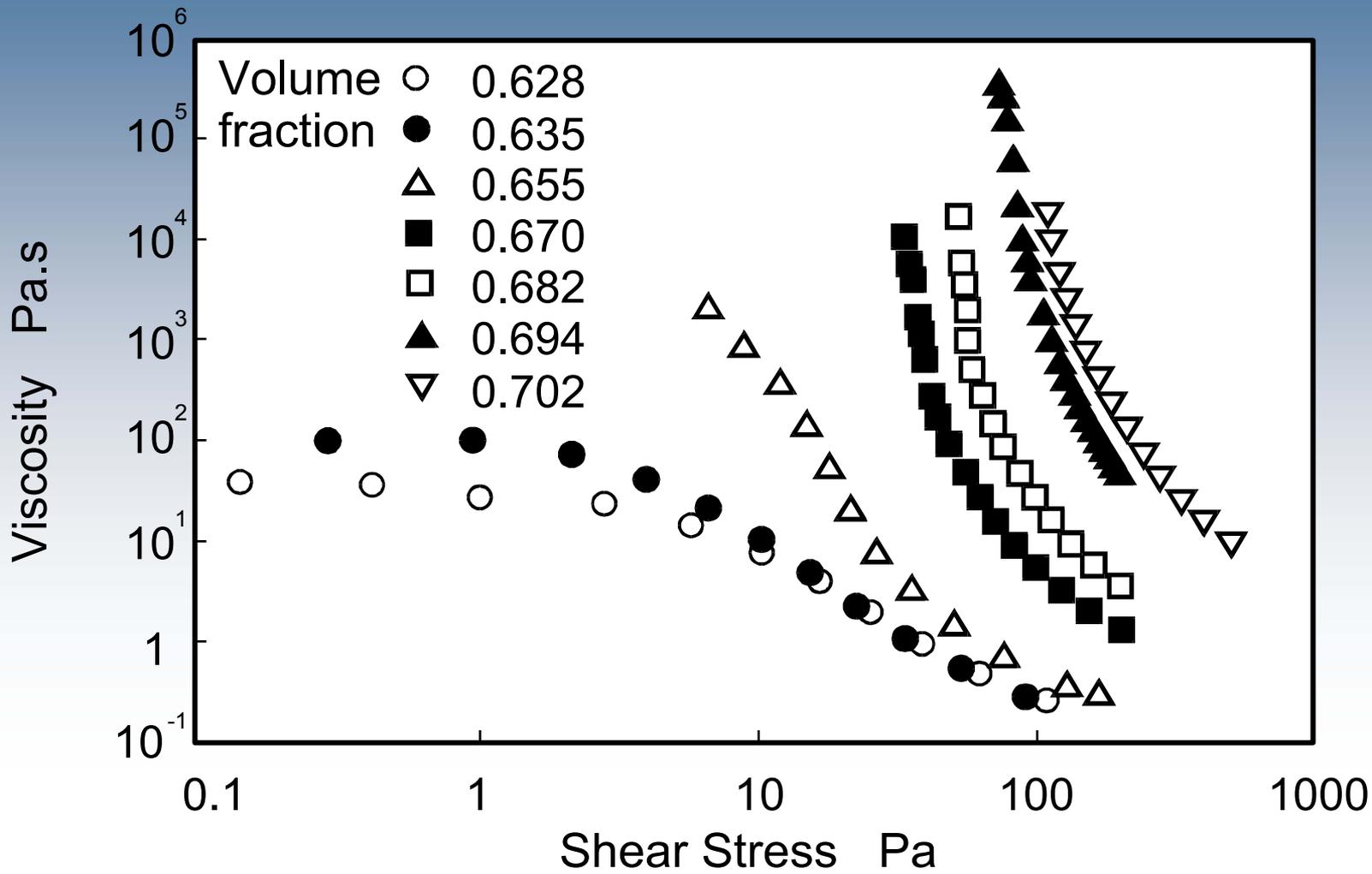
### Intrinsic Viscosity

$$[\eta] = \lim_{\phi \rightarrow 0} \frac{\eta_{sp}}{\phi}$$









# Yield Stress for Hard Sphere Suspensions

$\phi$ (Volume Fraction)	$\tau_y$ (Yield Stress, Pa)		
	Vane	Steady Shear	Creep
0.670	----	30 +/- 5	25 +/- 5
0.682	22 +/- 5	50 +/- 5	45 +/- 5
0.694	67 +/- 6	80 +/- 8	90 +/- 5
0.708	108 +/- 2	100 +/- 10	90 +/- 10

# Our Ceramic Will Test Your Metal

## Introducing The New Z-Driver From Coors CeraSports

**Superior Performance.** A well-hit ball with the Coors CeraSports Ceramic Z-Driver is an experience unlike any other in golf. The way it looks. The way it sounds. The way it feels. A confident feeling that translates into superior performance.

**Precision Advantage.** The secret is in the clubface. Computer-designed with optimum roll and bulge characteristic that maximize distance and accuracy. The Coors CeraSports Ceramic Z-Driver features the Zirconia (Z) clubface—a diamond-hard surface, precision-machined to the most

exacting tolerances. So its accuracy and clean look are permanent. And in a game of unending variables, you'll welcome the consistency.

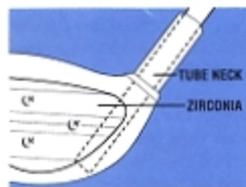


Drive after drive, your efforts translate into perfection off the tee.

### Test Drive The Z-Driver.

Playing the Z-Driver is exhilarating. Visit your pro shop and ask for a test drive. Or call 1-800-252-PUTT. The ceramic difference will change the way you feel about golf. Forever.

**Consistent Accuracy.** That's only the beginning. To give you every advantage, the Coors CeraSports Ceramic Z-Driver has an aerodynamically sleek tube neck design that maximizes clubhead speed. And because accurate distance is the real test, the tube neck design and deep penetrating shaft virtually eliminate twist and torque.



Coors CeraSports Ceramic Z-Drivers			
Model	Head Size	Shaft Type	Head Color
Men's Z	Standard	Graphite R/SX	Grey gloss
Men's Z	Standard	Steel	Grey gloss
Men's ZX	Expanded	Graphite R/SX	Black gloss
Men's ZX	Expanded	Steel	Black gloss
Senior's ZS	Expanded	Custom Graphite	Black gloss
Ladies' ZL	Standard	Custom Graphite	Grey gloss

Only right-handed Z-Drivers are offered at this time.

### Ceramicon Designs, Ltd.

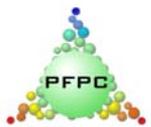
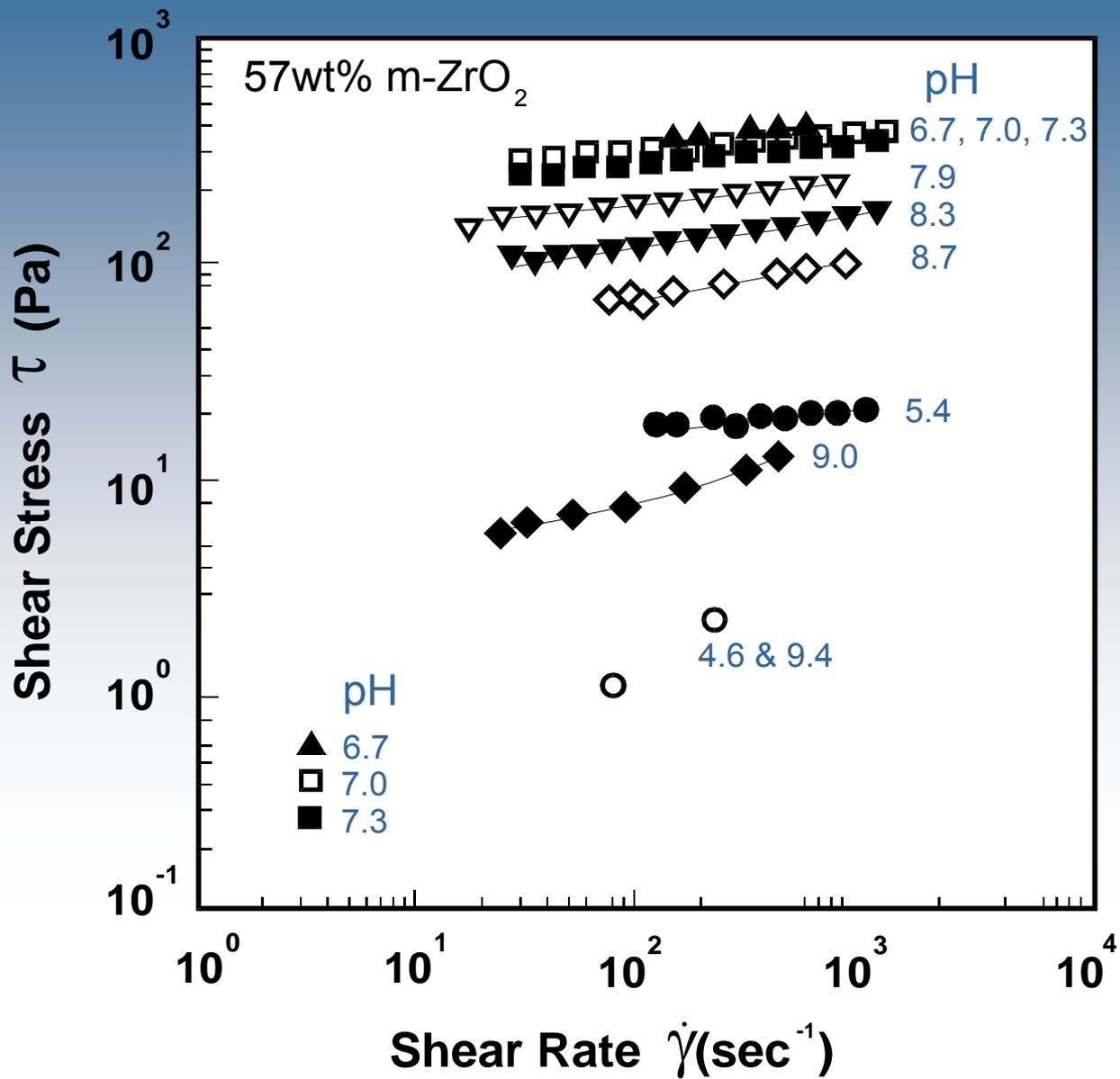
A Division of Coors Ceramics Company  
600 9th Street, Golden, Colorado 80401  
**1-800-252-PUTT**



Discover The Ceramic Difference

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...SNAKE SCALES, FROG  
FEET, BAT EARS ...

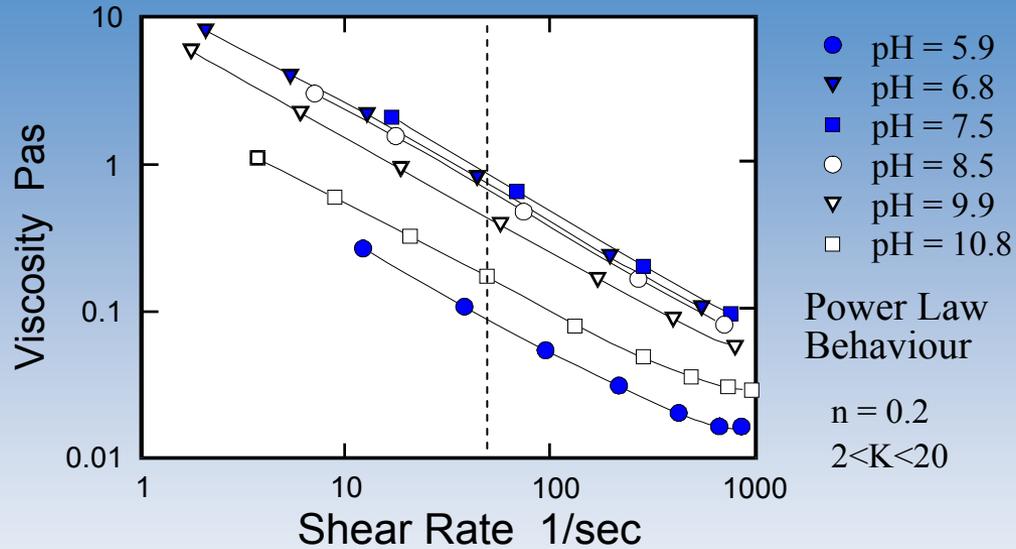


B.Parker, J.Hart & R.Binnington

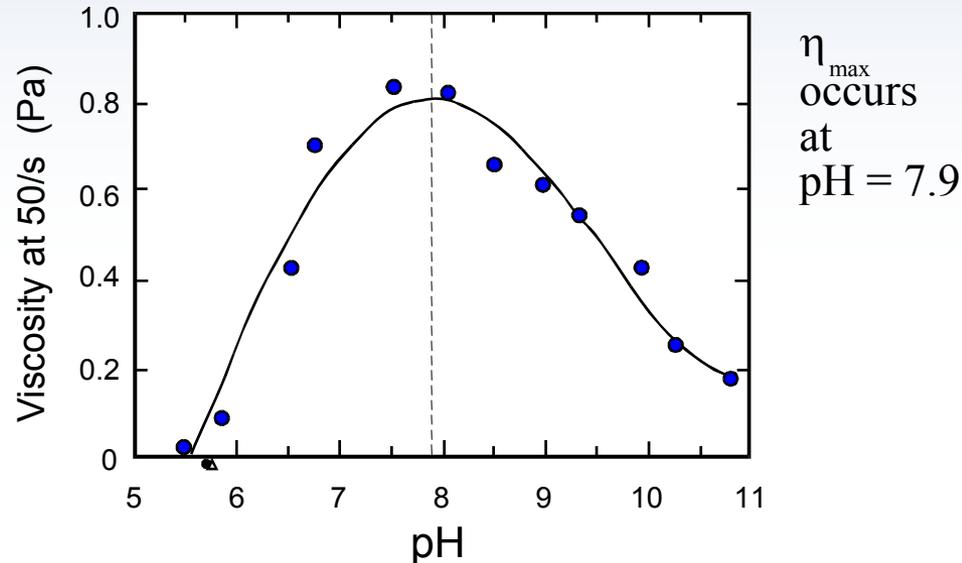
# The Rheology of $\text{TiO}_2$ Pigment Suspensions

50wt% solids CR62

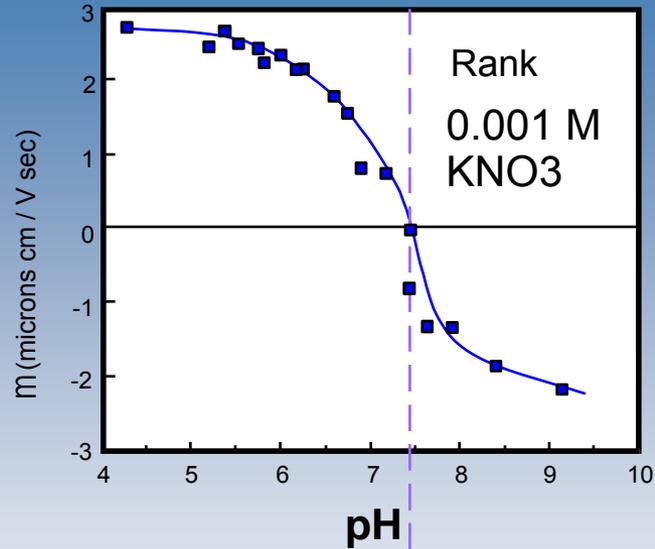
Viscosity Profiles as a function of pH



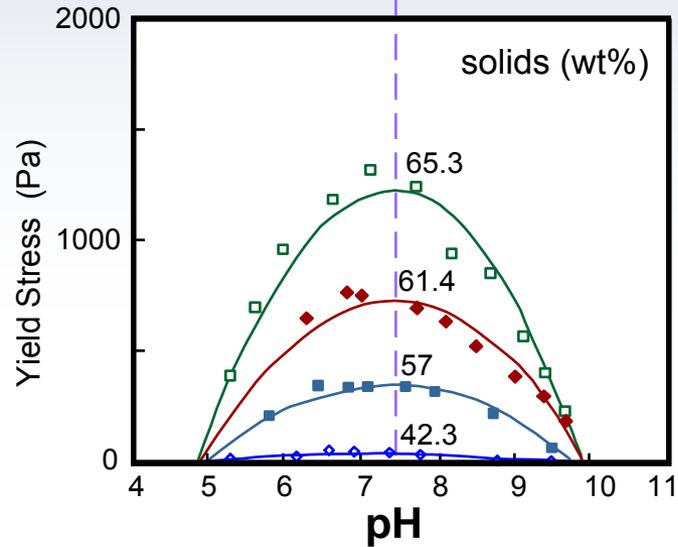
Viscosity Curve



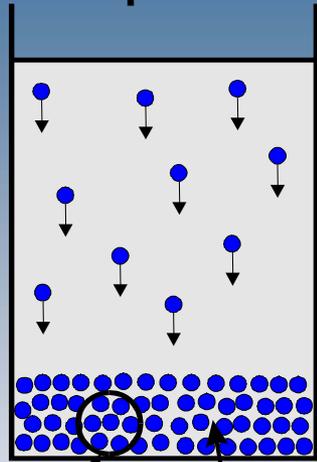
# 1. Electrokinetics



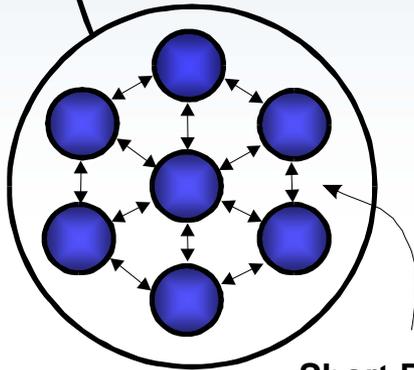
# 2. Rheology



### Stable Suspension

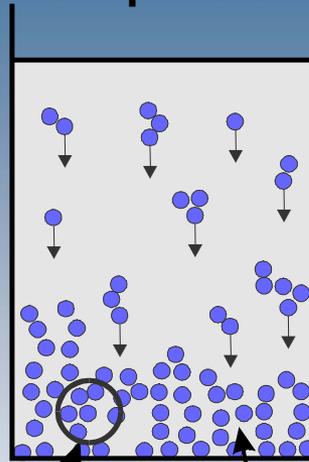


Close Packed Sediment

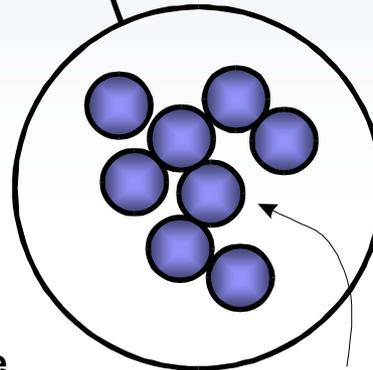


Short Range Repulsive Forces

### Flocculated Suspension

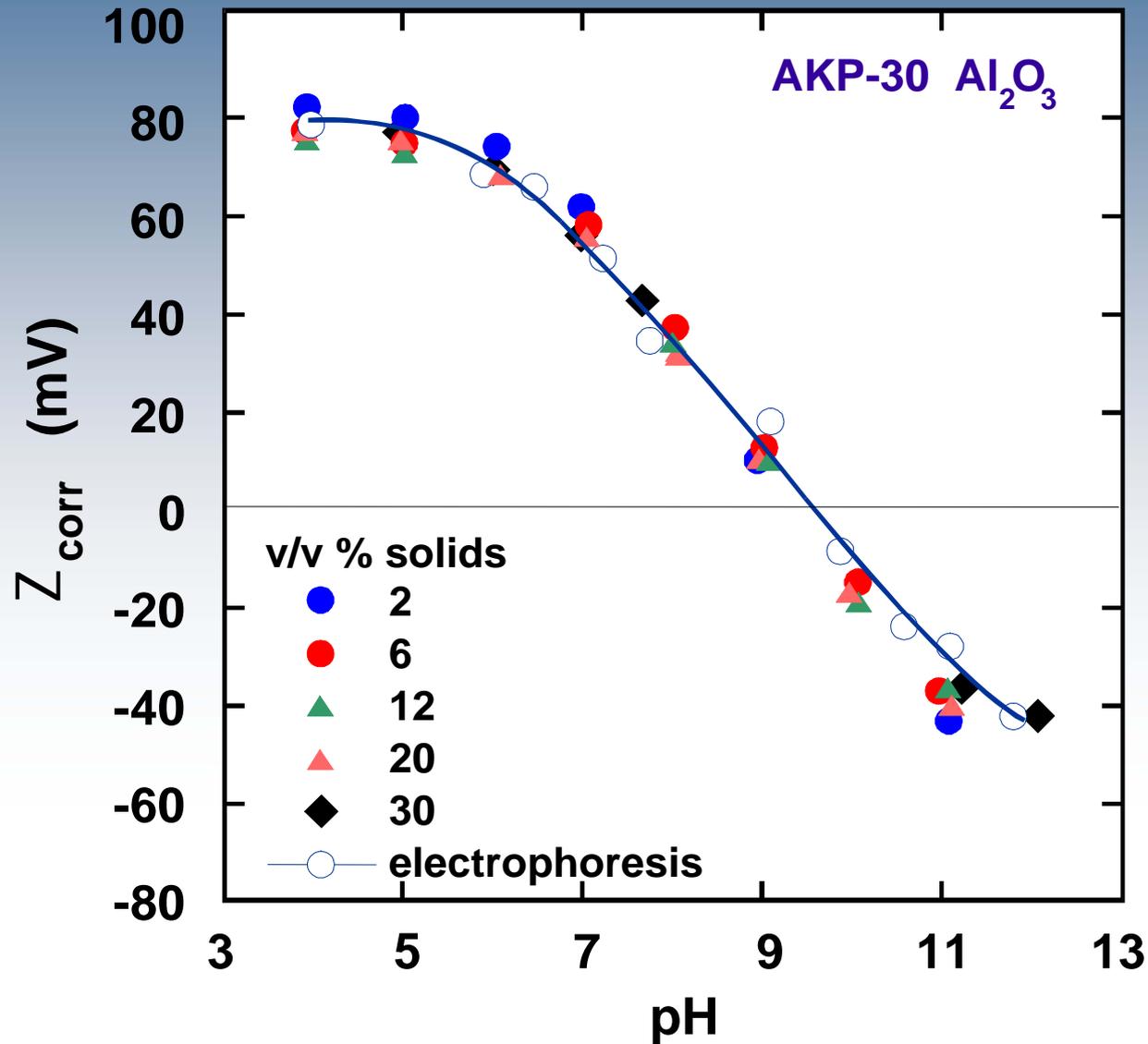


Open Network with Large Voids

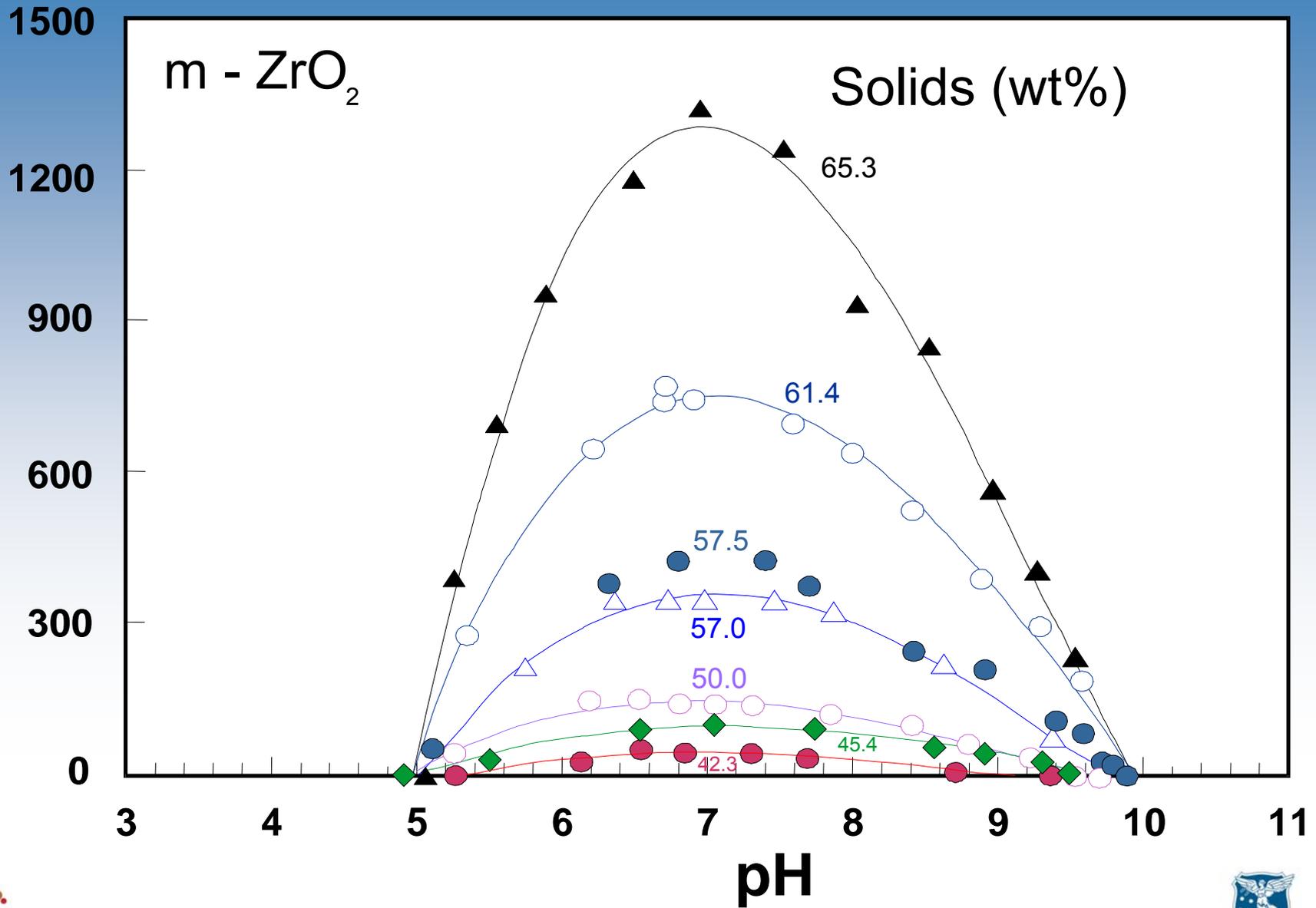


Attractive Forces

# Alumina Electrokinetics

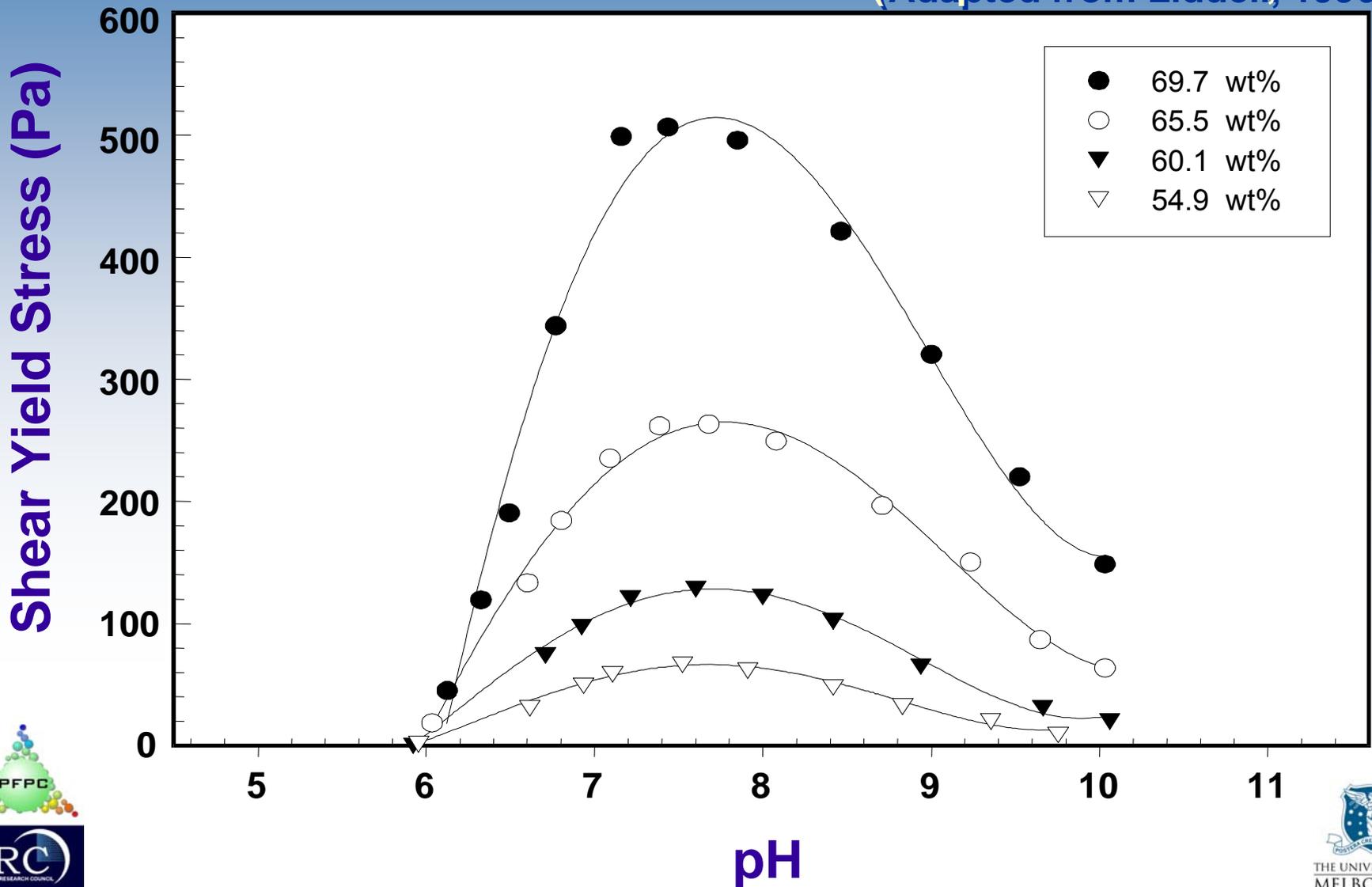


Yield Stress,  $\tau_y$  (Pa)



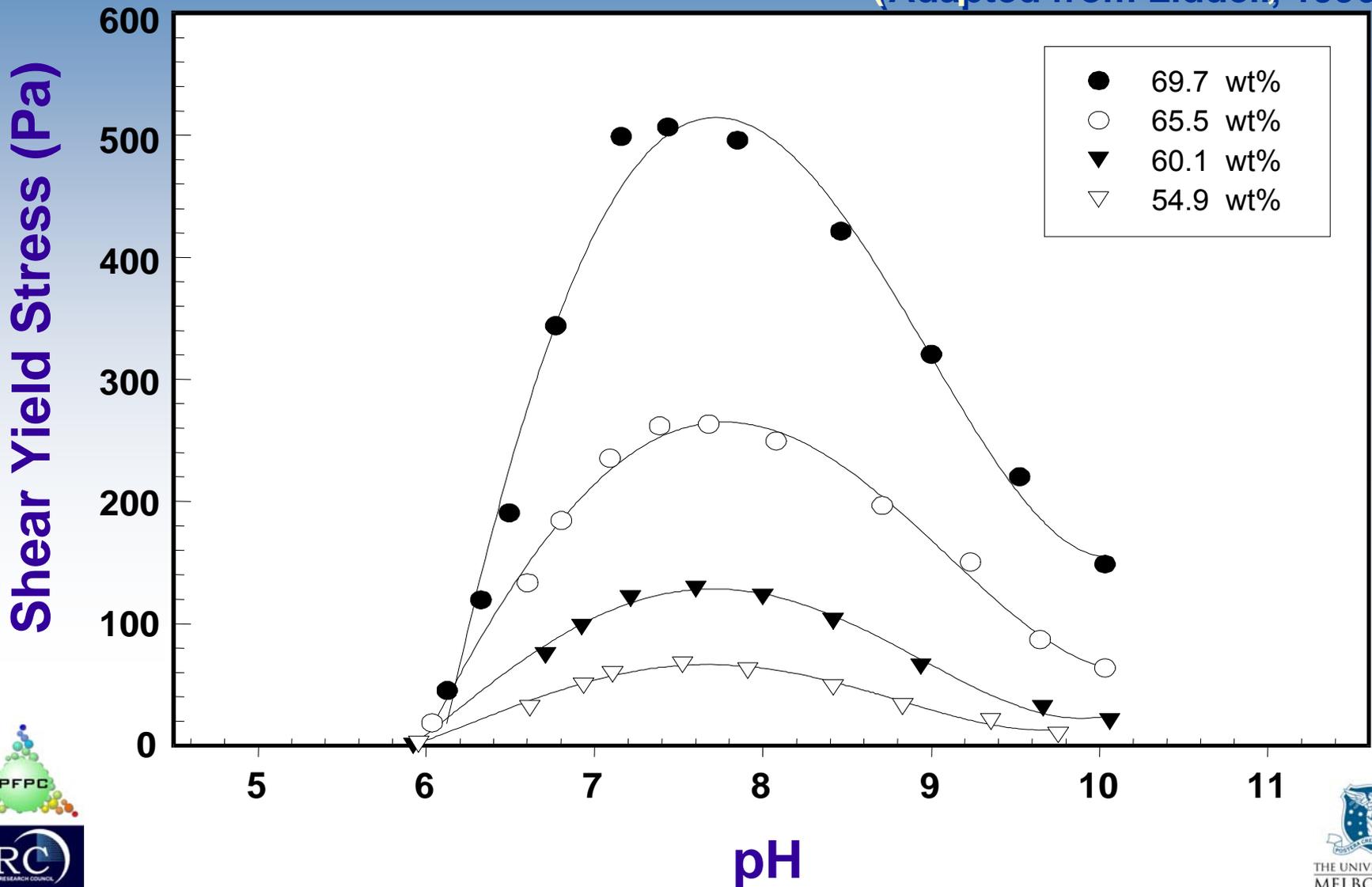
# Yield Stress of Titania Suspensions as a Function of pH and Solids Concentration

(Adapted from Liddell, 1996)



# Yield Stress of Titania Suspensions as a Function of pH and Solids Concentration

(Adapted from Liddell, 1996)



# Additive Effects -Type of Interaction

## a) STERIC INTERACTION

- i) illustrated by small additive molecules
- ii) modelling to show the importance of additive molecular size

## b) BRIDGING FLOCCULATION

- i) high molecular weight polyelectrolyte

## c) HYDROPHOBIC INTERACTION

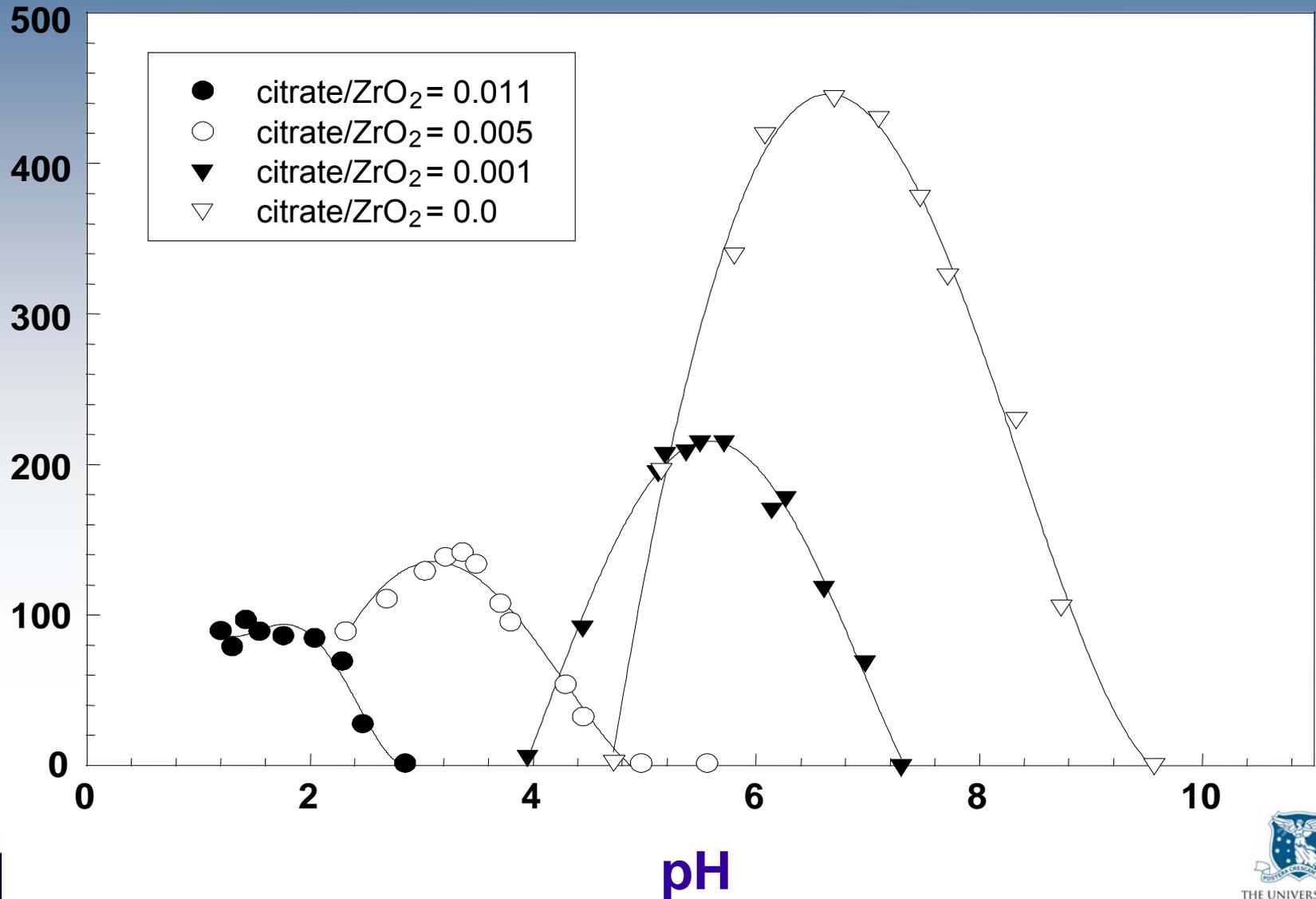
- i) additive with a charge head group and a long hydrophobic tail, eg. dodecyl sulphate

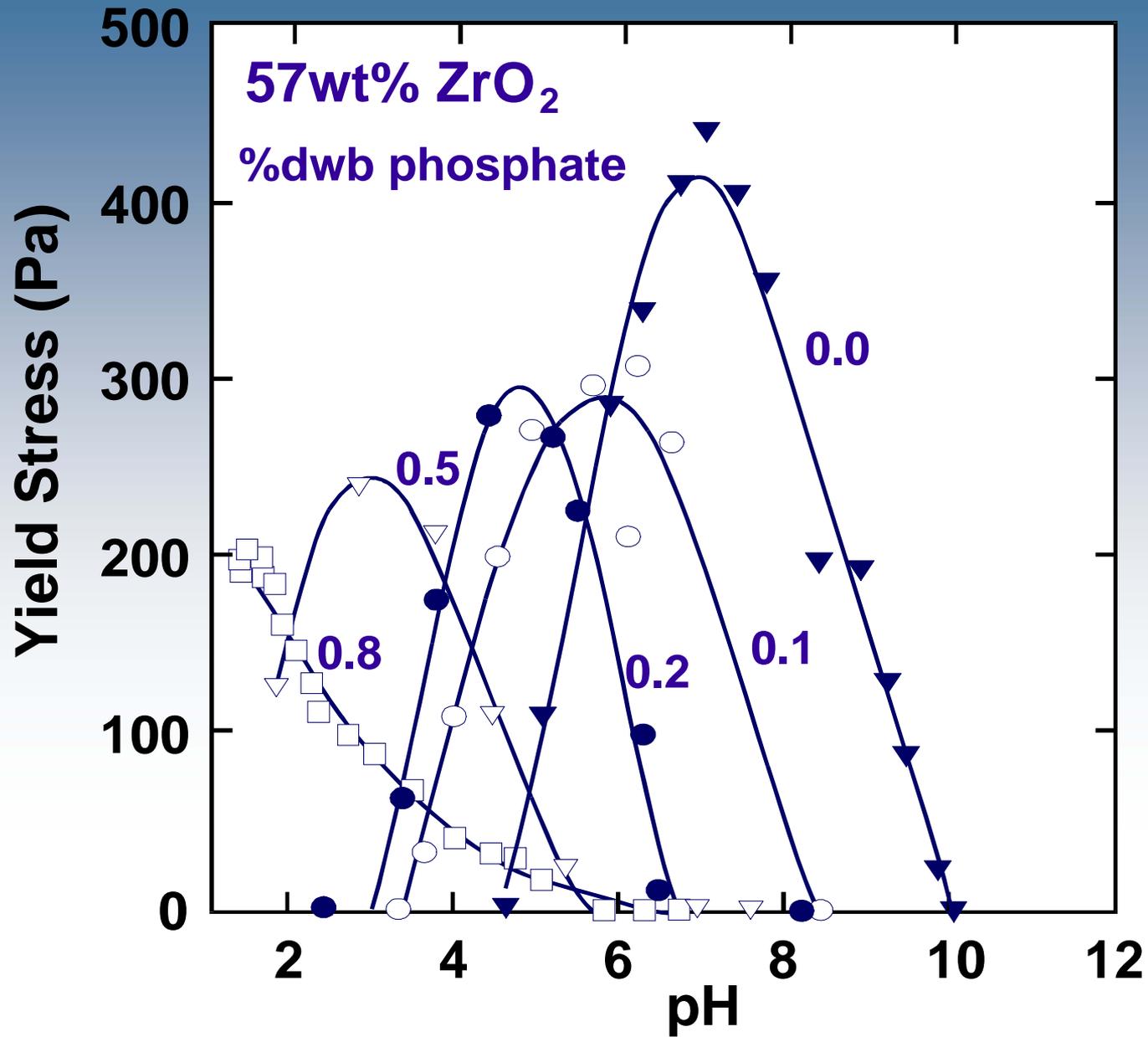
*Note that most analyses were conducted at the IEP so as to eliminate complication arising from electrostatic interaction*

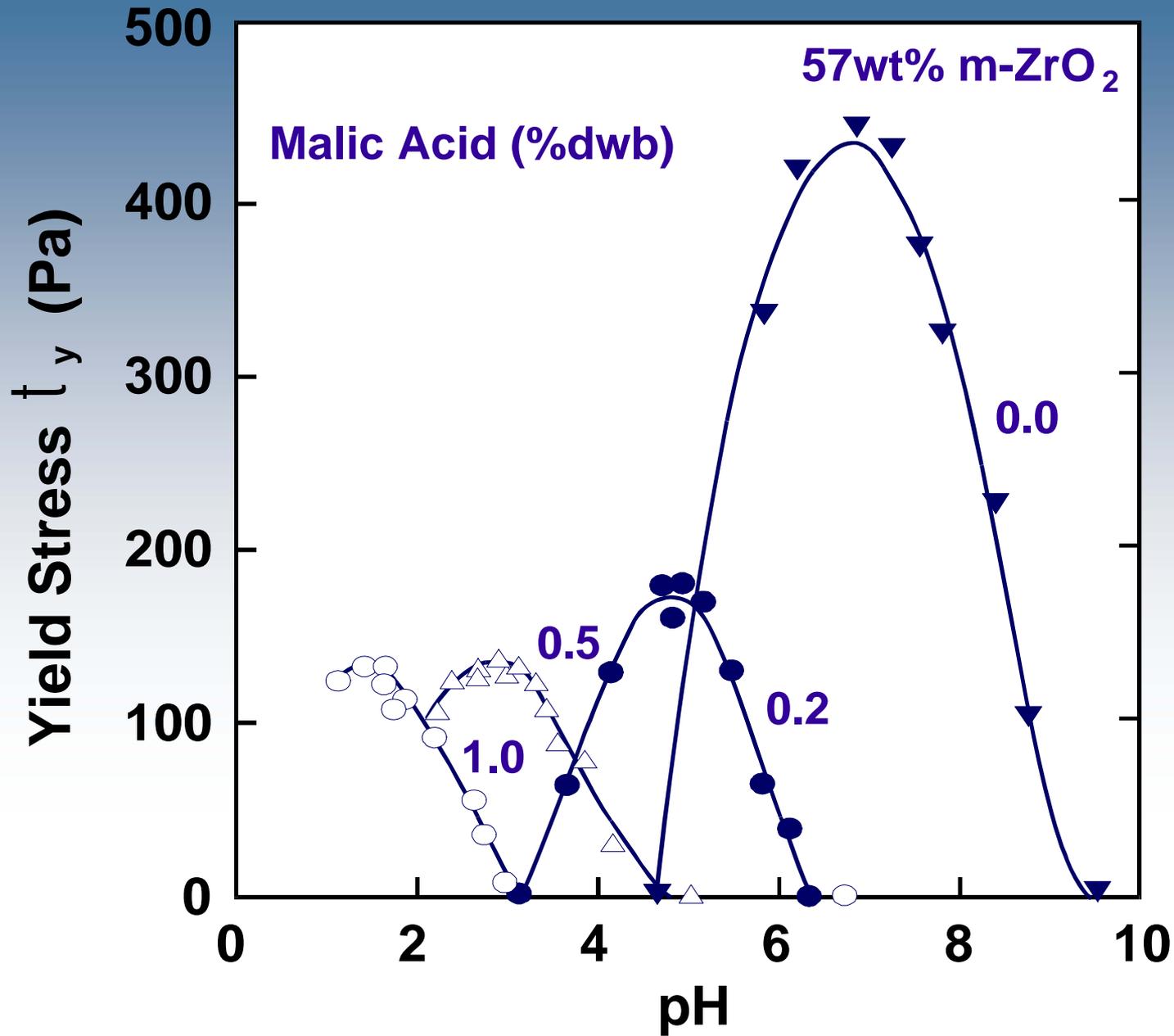


# Yield Stress versus pH behaviour of 57% Zirconia Suspension as a Function of Citrate Concentration

Shear Yield Stress (Pa)

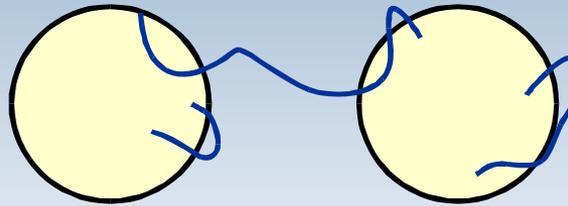






# Bridging Flocculation

When a high Mw polymer is adsorbed onto 2 or more particles at the same time.

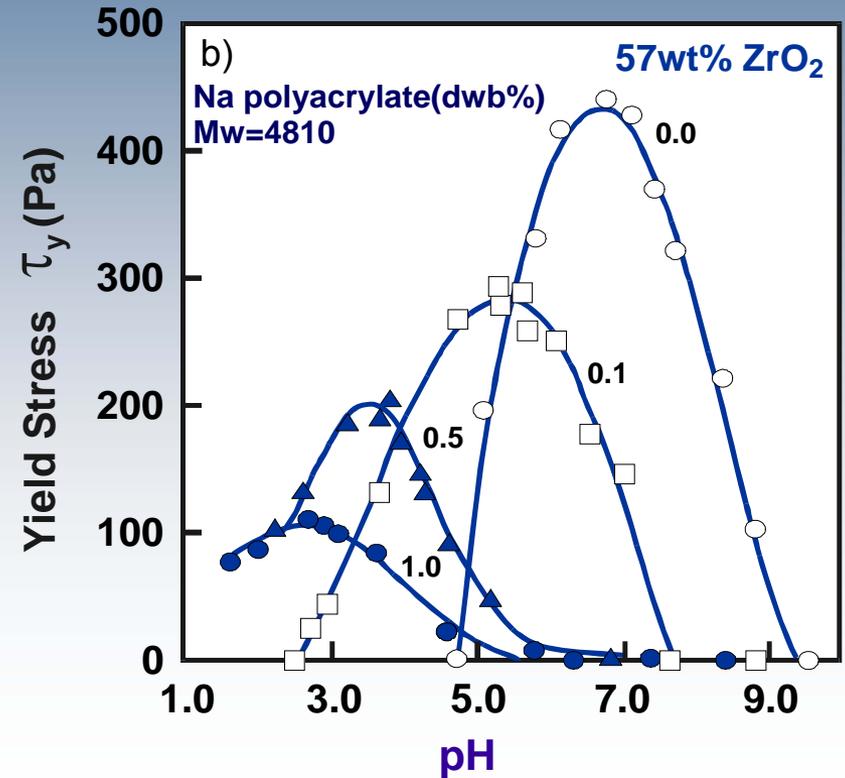
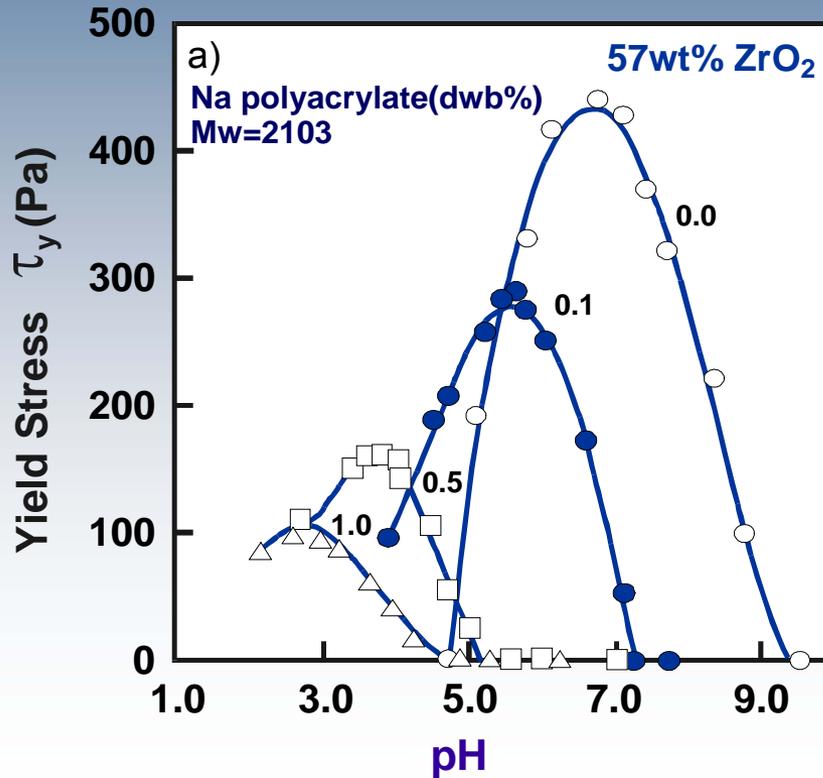


Bridging flocculation is an additional attractive force and is only important for high Mw polymer and at low additive concentration.

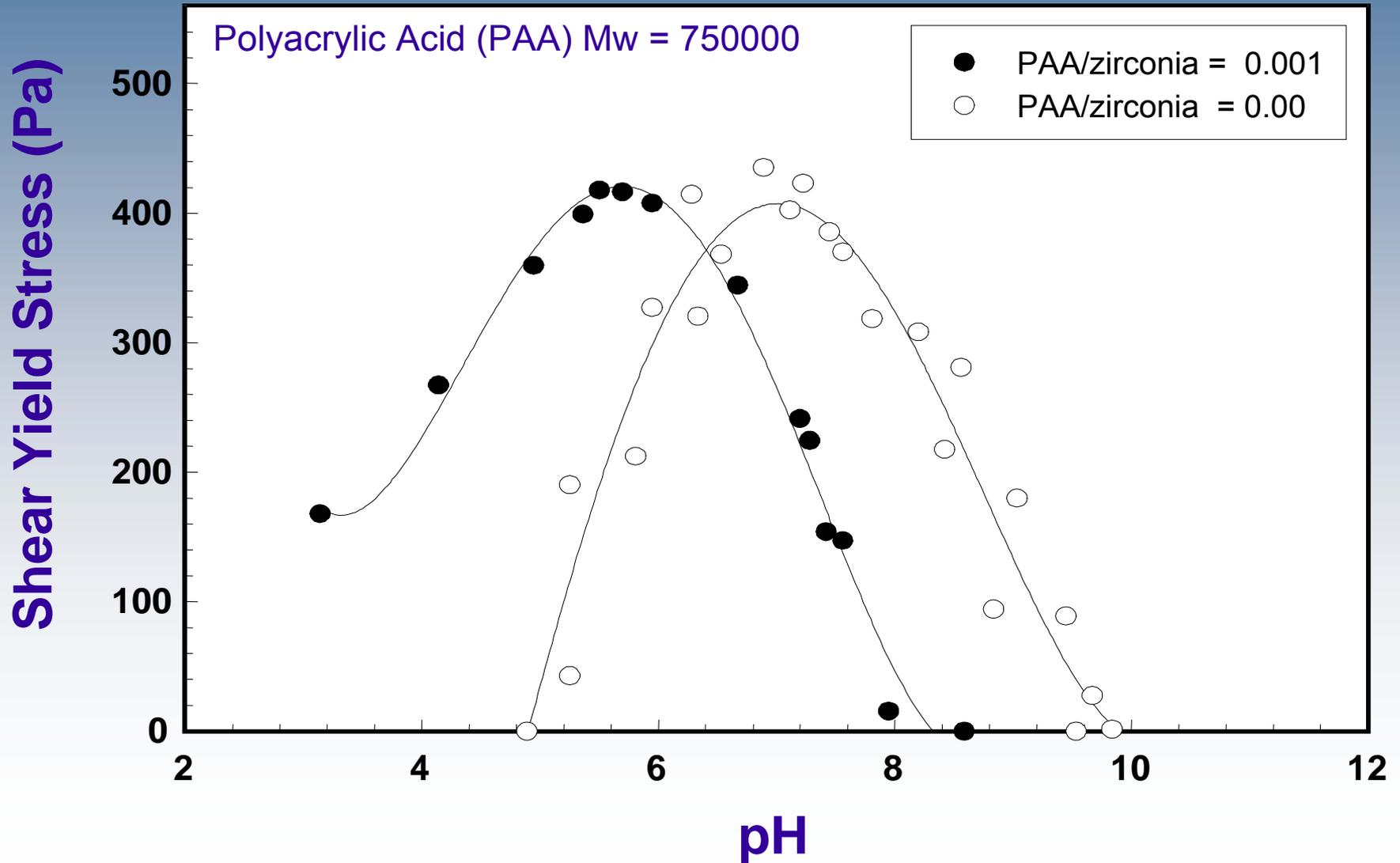


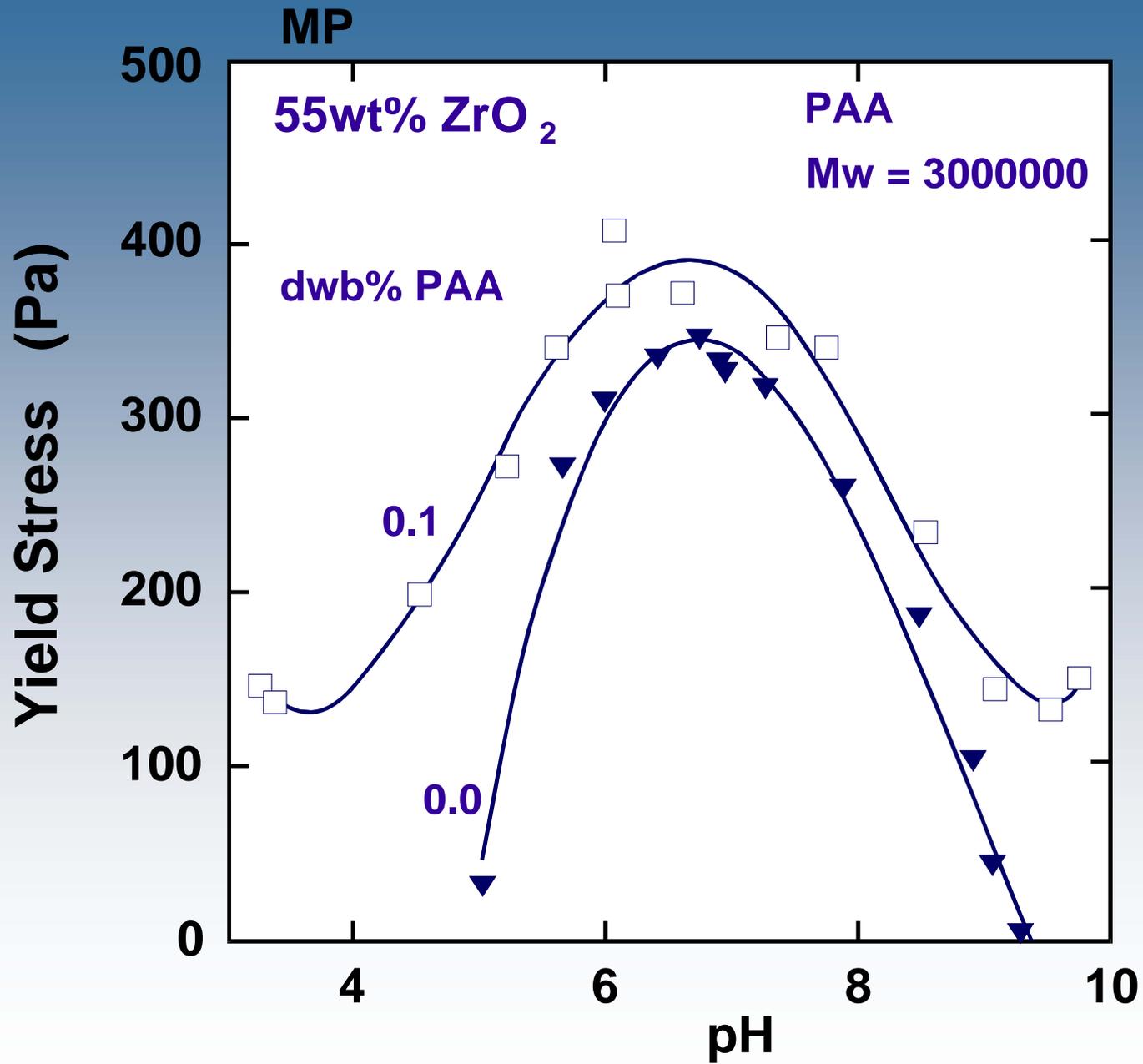
# Z-Tech $\text{ZrO}_2$ , S.A. = $15 \text{ m}^2/\text{g}$

Yield stress-pH behaviour of 57wt%  $\text{ZrO}_2$  suspensions treated with sodium polyacrylate of molecular weight: a)2103, b)4810

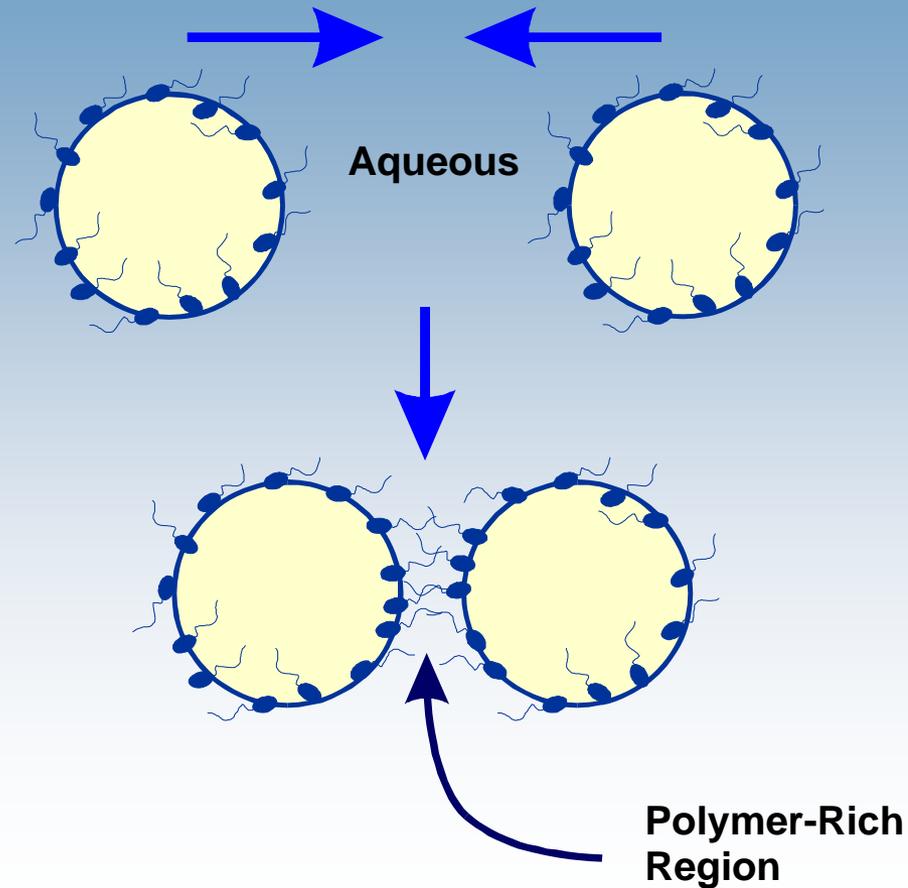


# Shear Yield Stress of Zirconia Suspension at 57wt% as a Function of pH and the Concentration of High Molecular Weight PAA





# Hydrophobic Interaction

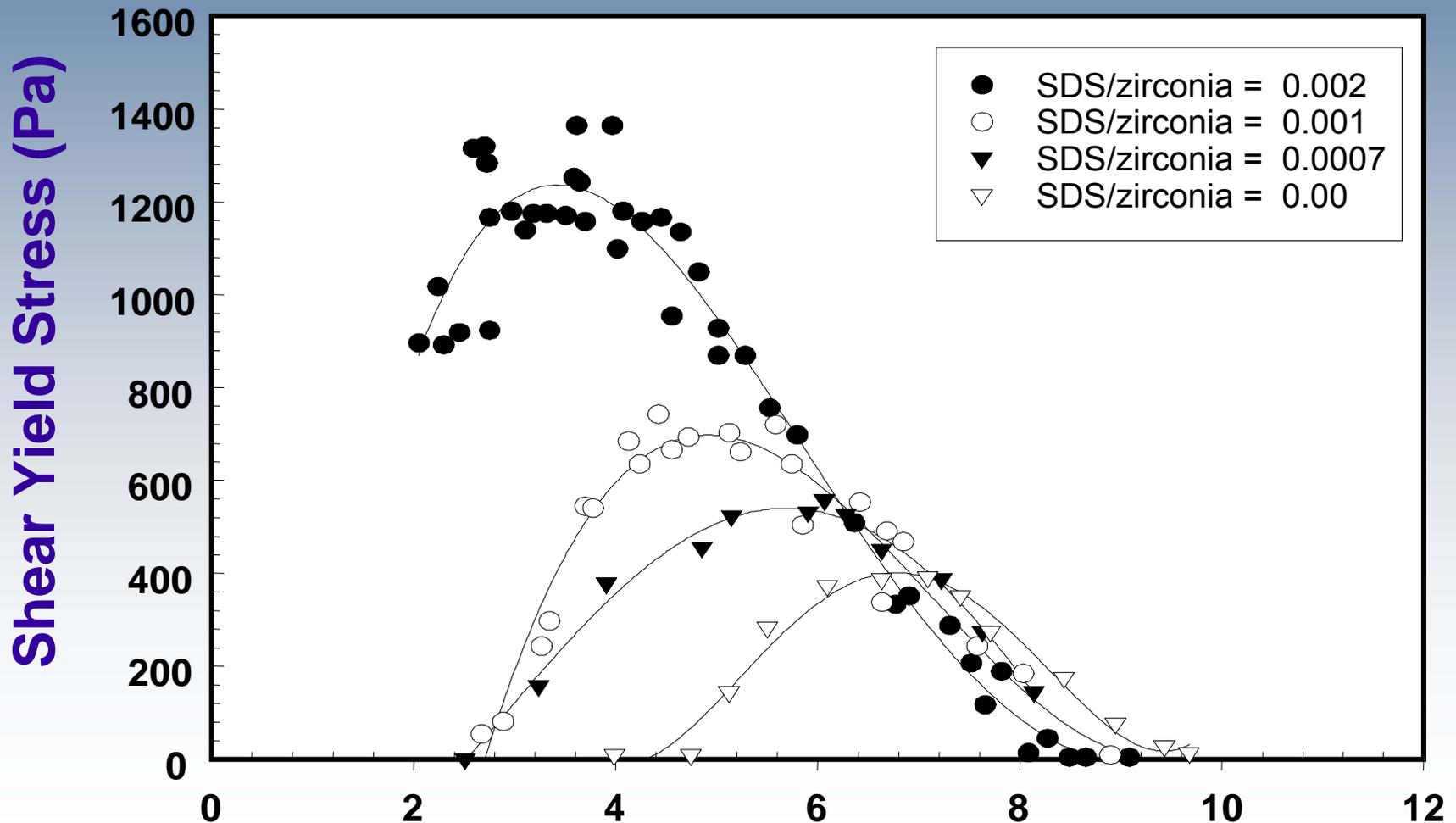


At IEP:

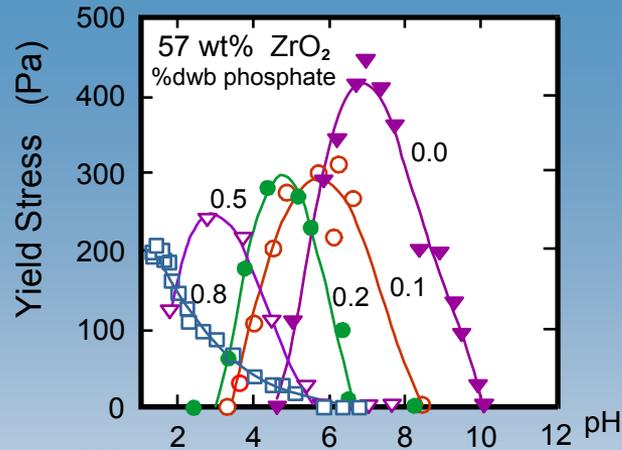
$$V_T = V_{\text{vdW}} + V_{\text{hydrophobic}}$$

Hydrophobic interaction occurs when the adsorbed polymer chains have greater affinity for each other than for the aqueous medium

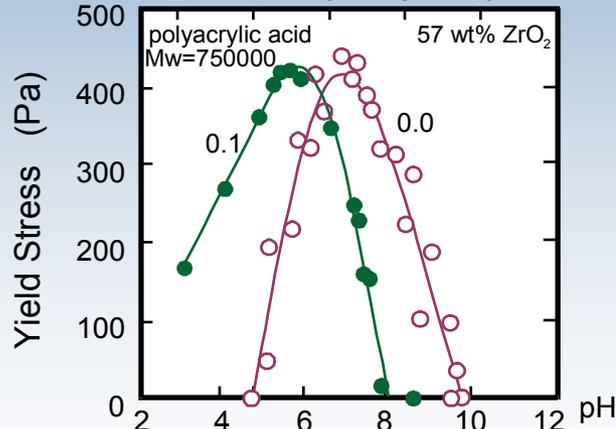
# Shear Yield Stress of Zirconia Suspensions at 57% as a function of pH and Concentration of Sodium Dodecyl Sulfate (SDS)



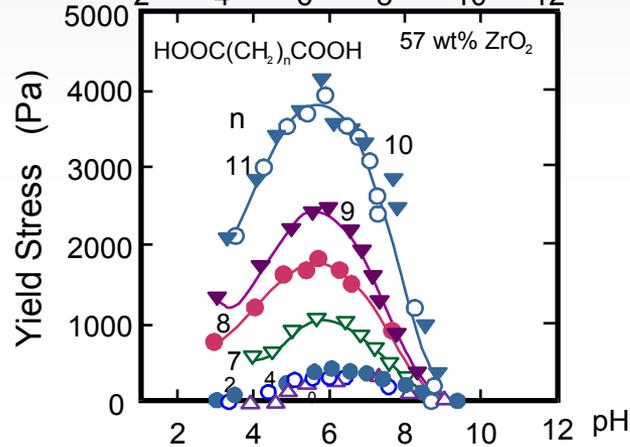
### STERIC

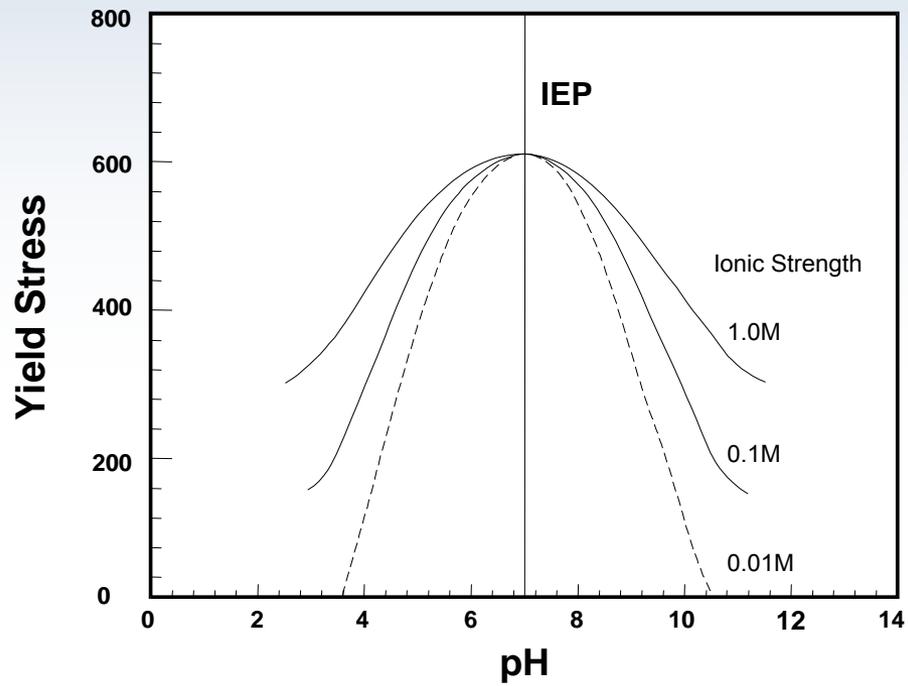
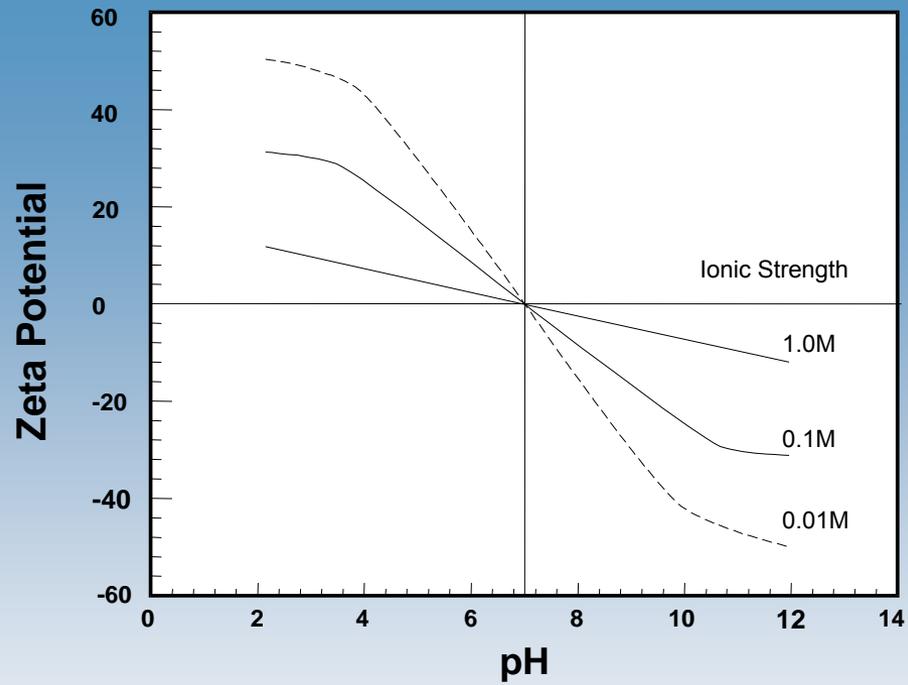


### BRIDGING



### HYDROPHOBIC



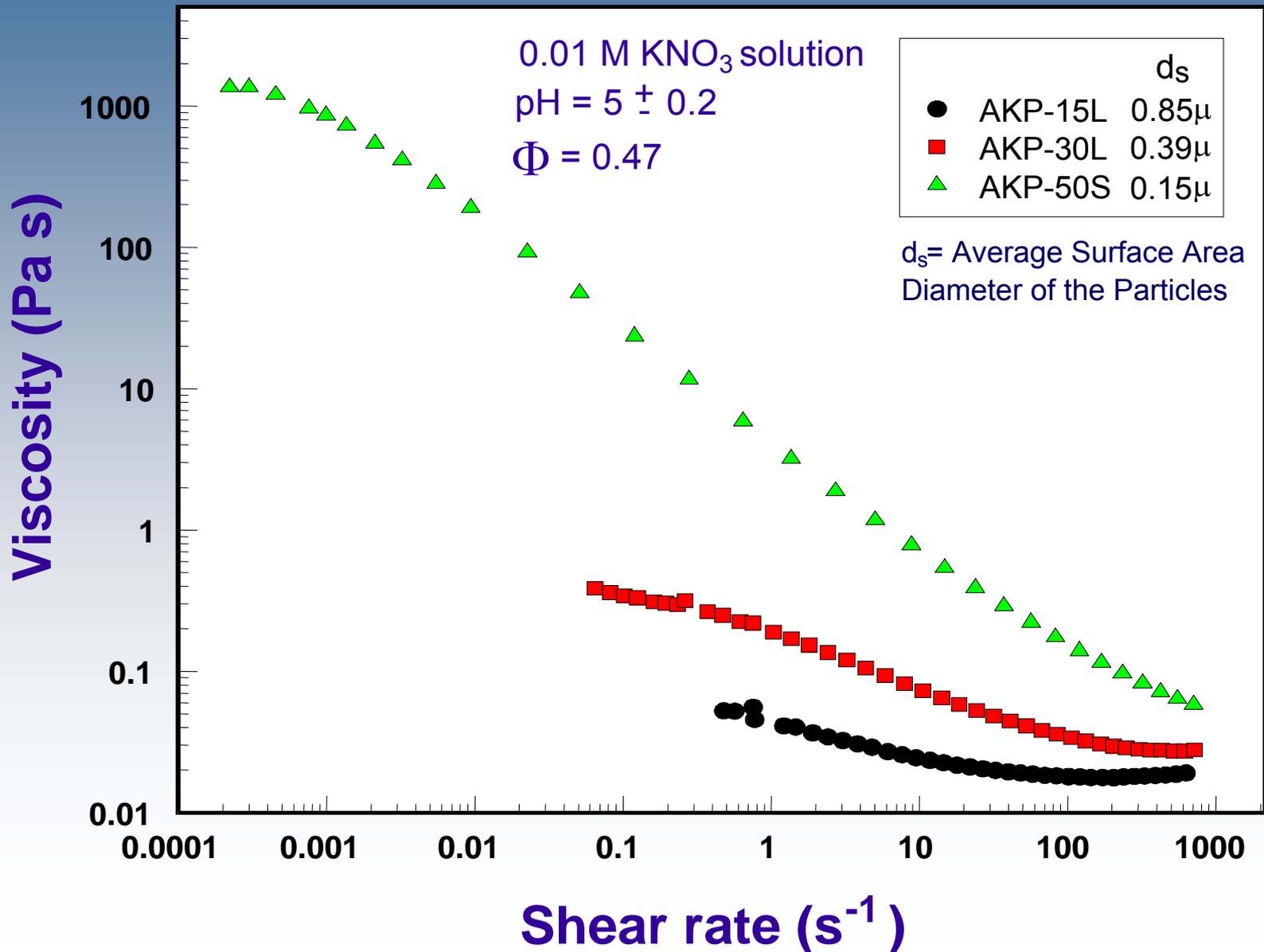


# Properties of Alumina Particles

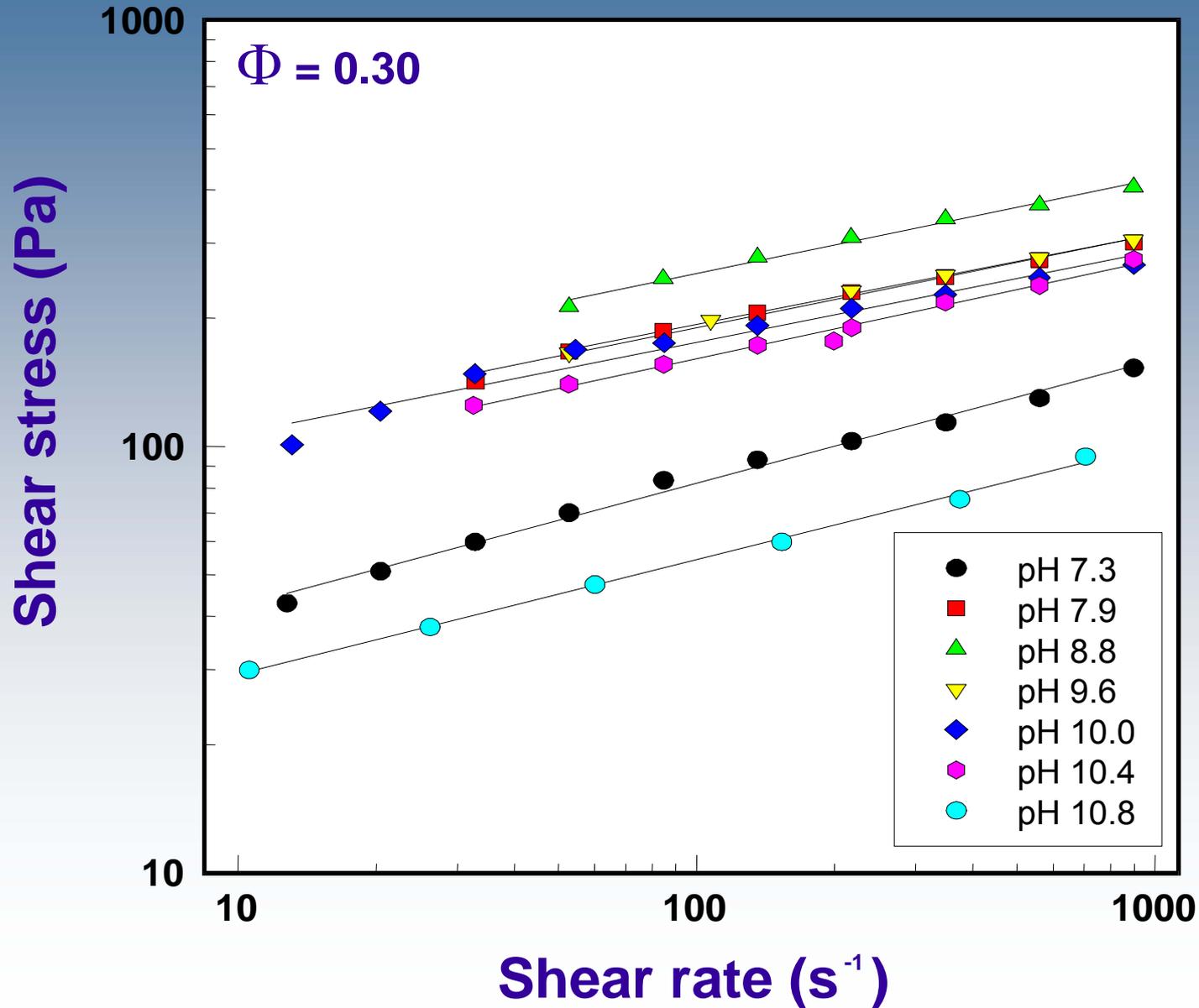
Samples	Density (g/cm <sup>3</sup> )	BET Surface Area (m <sup>2</sup> /g)	Mean Diameter (nm)
AKP-15	3.99	3.8	0.7
AKP-20	3.98	4.3	0.54
AKP-30	3.96	6.8	0.36
AKP-50	3.95	10.5	0.18



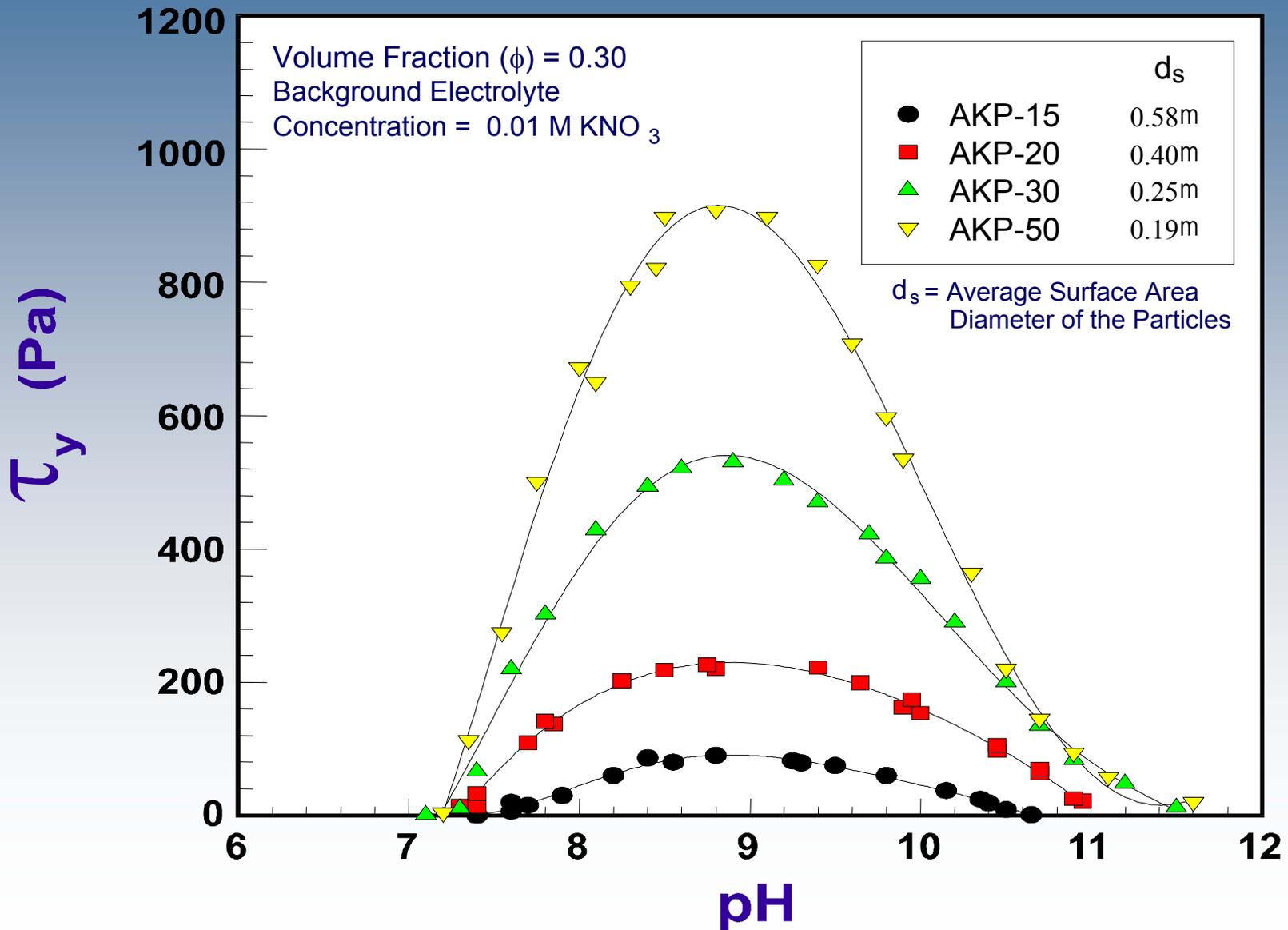
# The Effect of Particle Size on the Viscosity of Alumina Suspensions



# Flow Curves for AKP-20 Suspensions at various pH



# Yield Stress as a Function of pH for Alumina Suspensions of Different Particle Sizes



# For Monodisperse Particle Systems

At the iep

$$\tau_y = \frac{0.011\phi K(\phi,d)}{\pi} \left( \frac{A}{h_0^2} \right) \frac{1}{d}$$

where

A is the Hamaker constant

$h_0$  is the interparticle spacing at contact

d is the particle diameter

Away from the iep

$$\tau_y = \frac{0.011\phi K(\phi,d)}{\pi} \left( \frac{A}{h_0^2} - \frac{24\pi\epsilon\kappa\zeta^2}{(1+e^{\kappa h_0})} \right) \frac{1}{d}$$



# Normalised Yield Stress

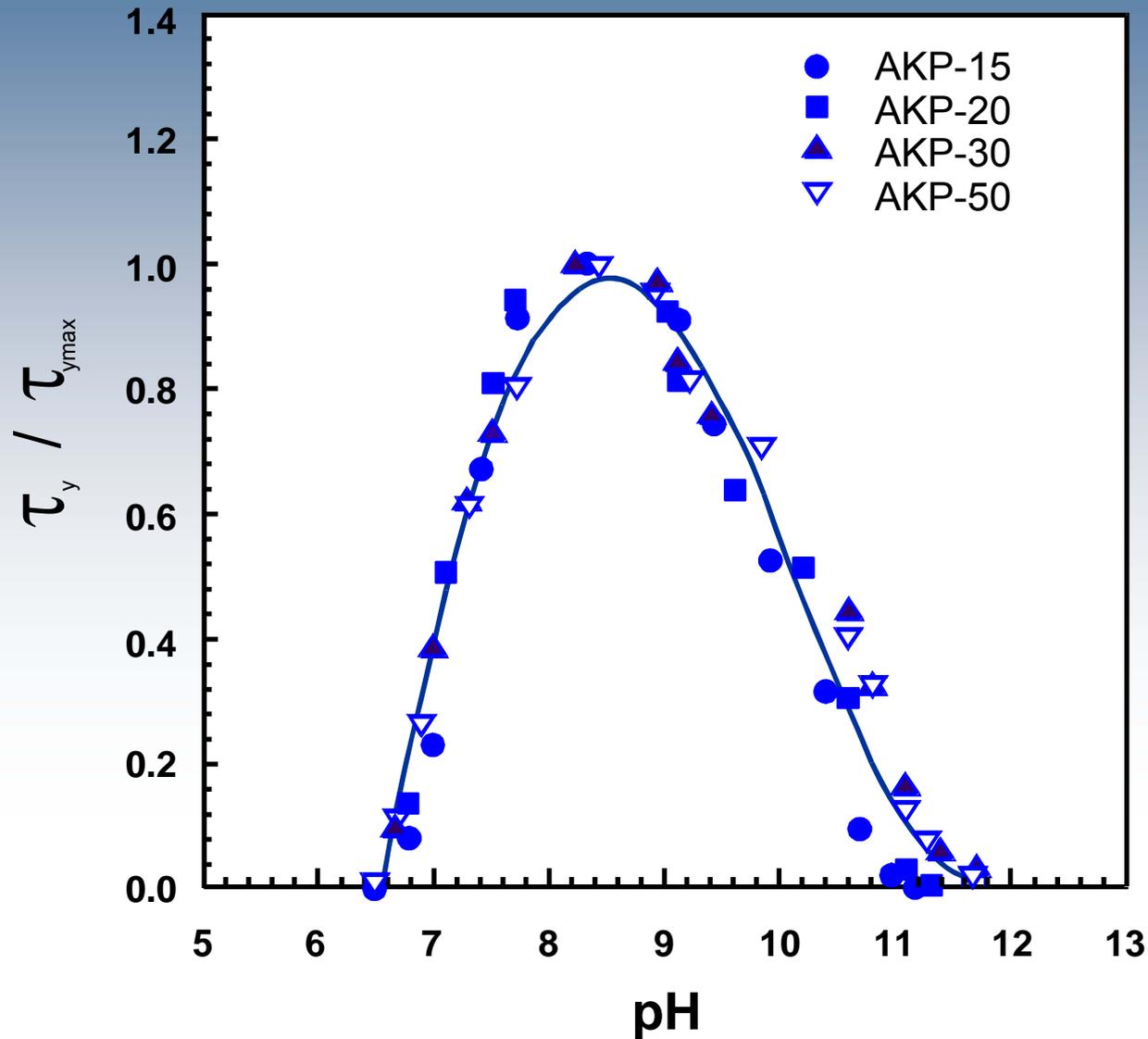
$$\frac{\tau_y}{\tau_{y\max}} = 1 - \frac{24\pi\varepsilon\kappa\zeta^2 h_0^2}{A(1 + e^{\kappa h_0})}$$

No Volume Fraction Dependence

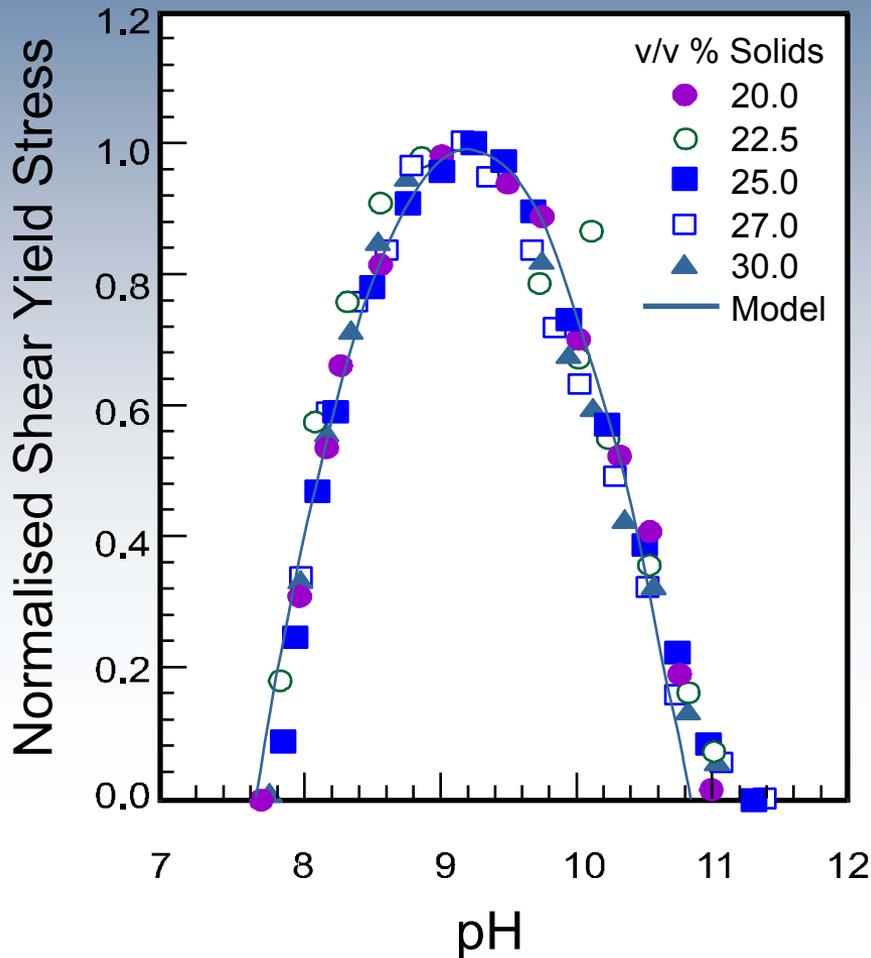
No Size Dependence

$h_0$  is the only Fitting Parameter

# Force Comparison



# Effect of Volume Fraction on Yield Stress

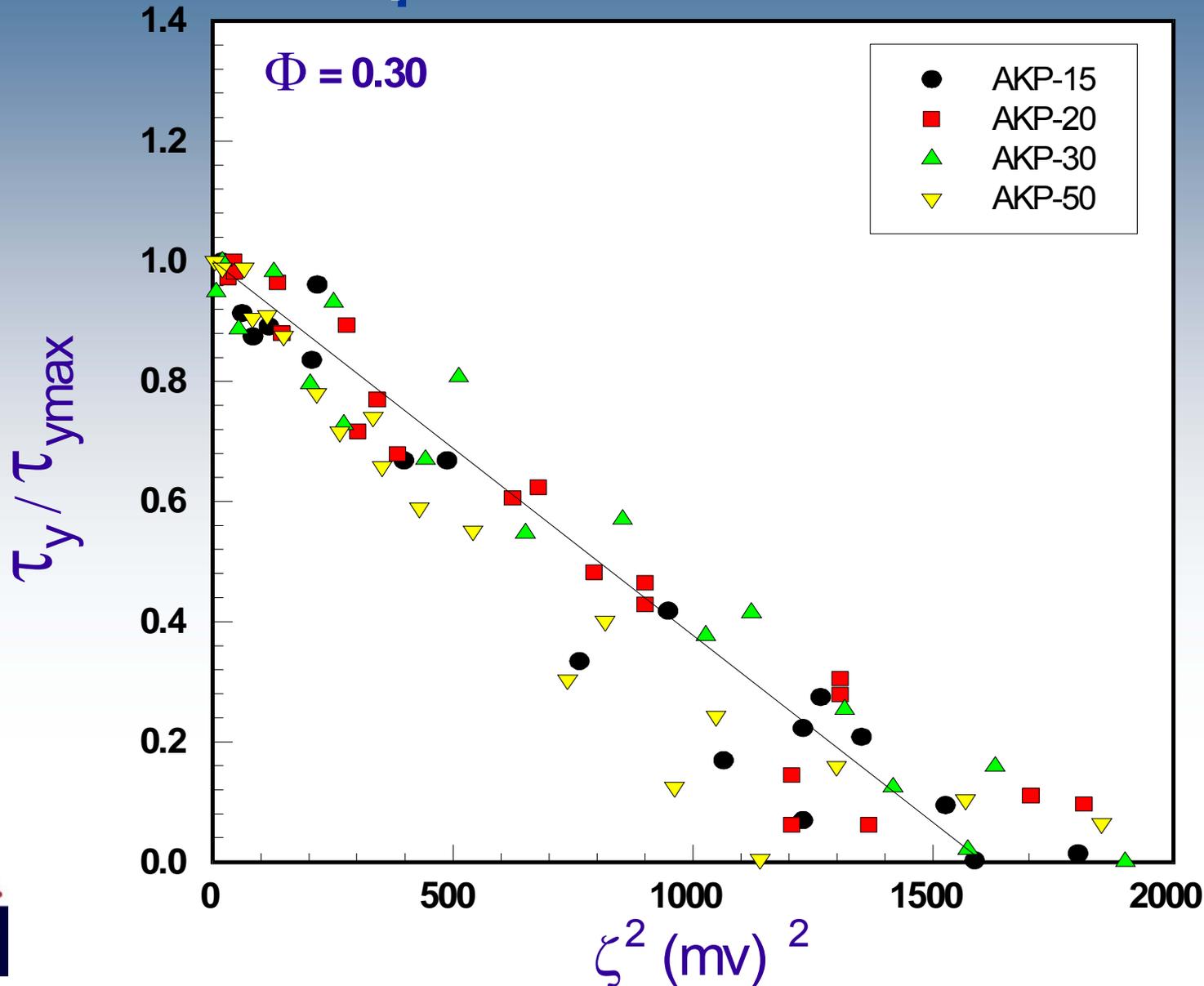


Normalised Yield Stress

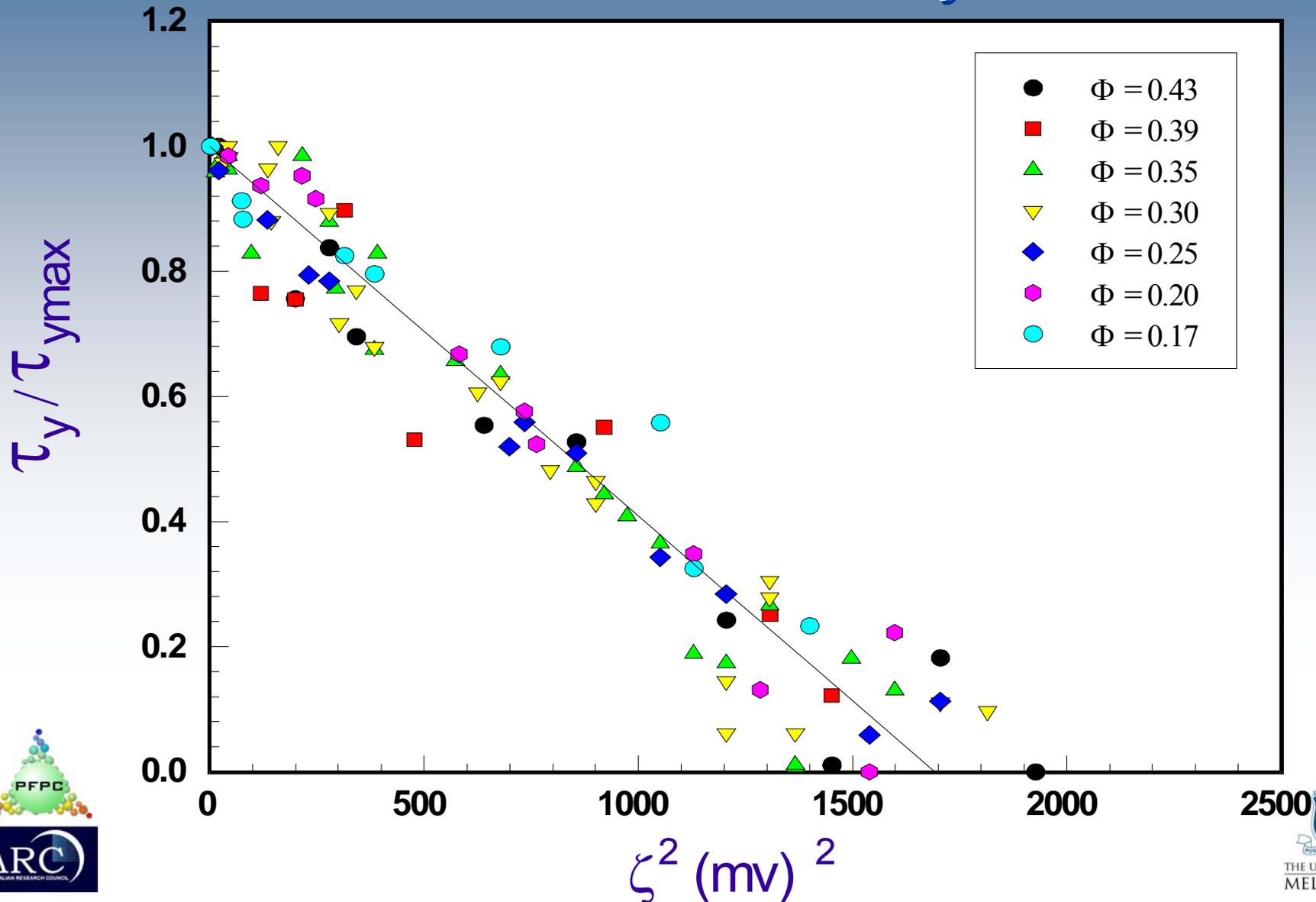
$$\frac{\tau_y}{\tau_{y\max}} = 1 - \frac{24\pi\epsilon\kappa\zeta^2 h_0^2}{A(1+e^{\kappa h_0})}$$

- No Volume Fraction Dependence
- No Size Dependence
- $h_0$  is the only Fitting Parameter

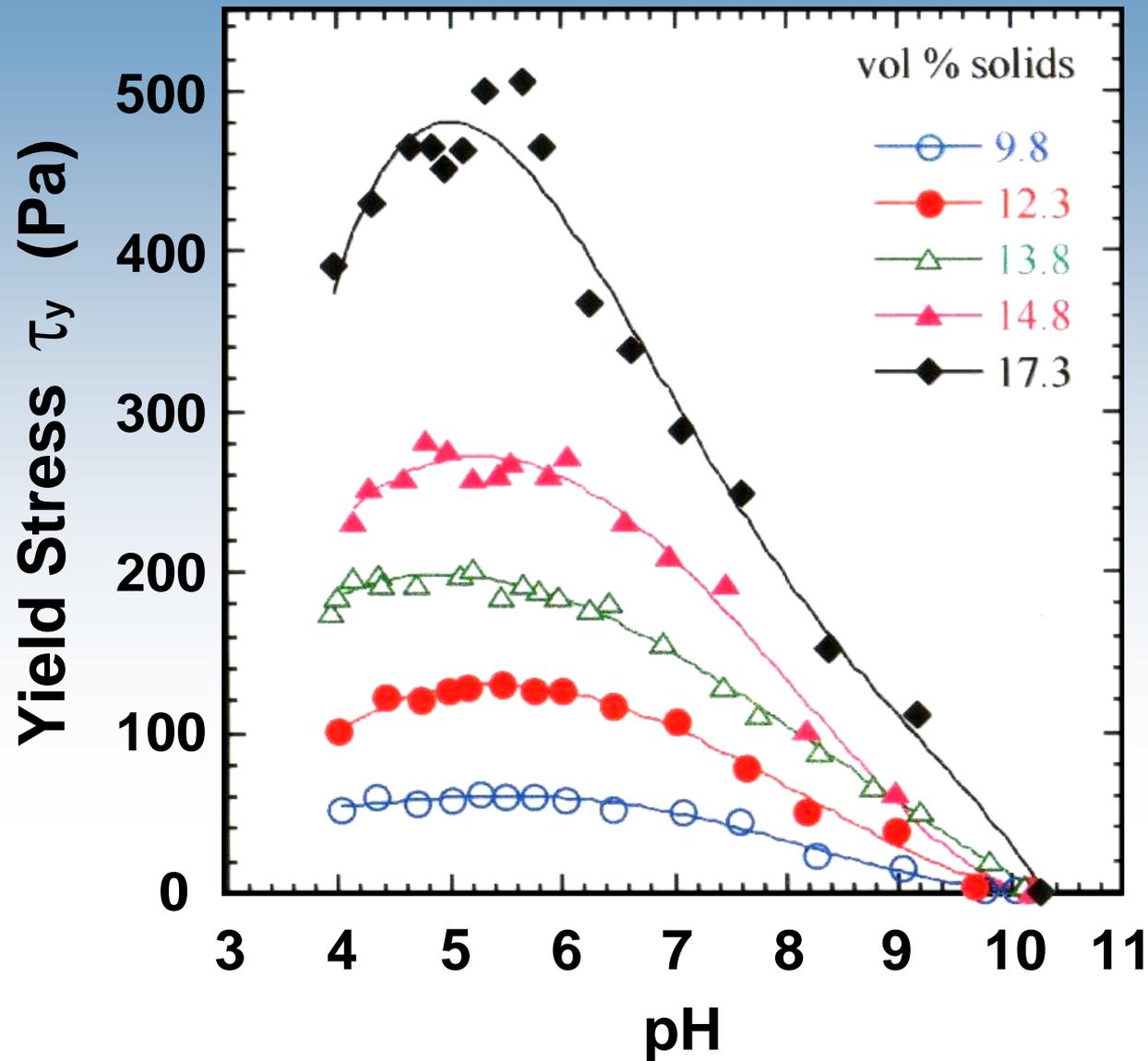
# The Normalised Yield Stress as a Function of $\zeta^2$ for Alumina Suspensions of Different Particle Sizes



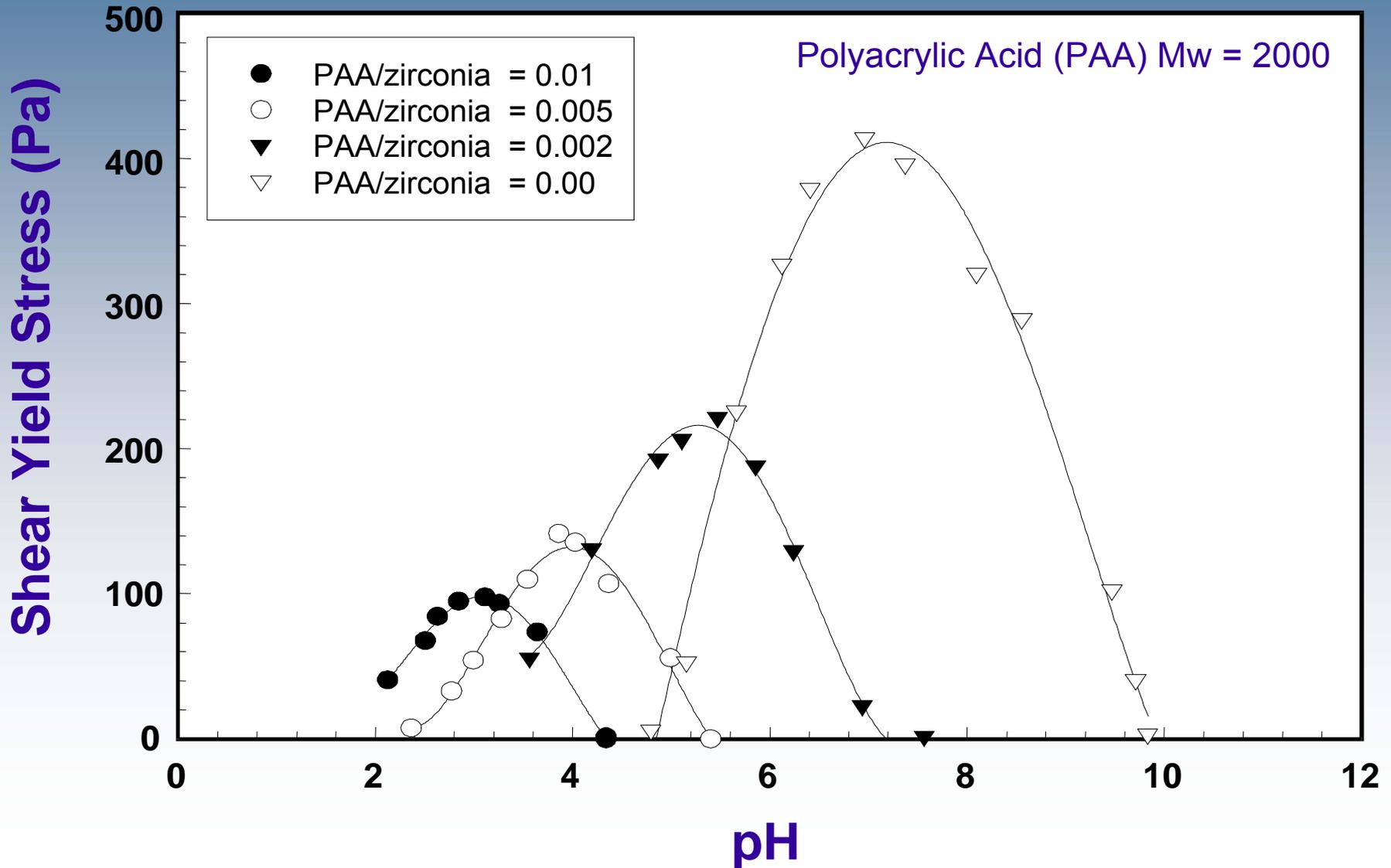
# Normalised Yield Stress of Alumina Suspensions as a Function of $\zeta^2$ for AKP-20.



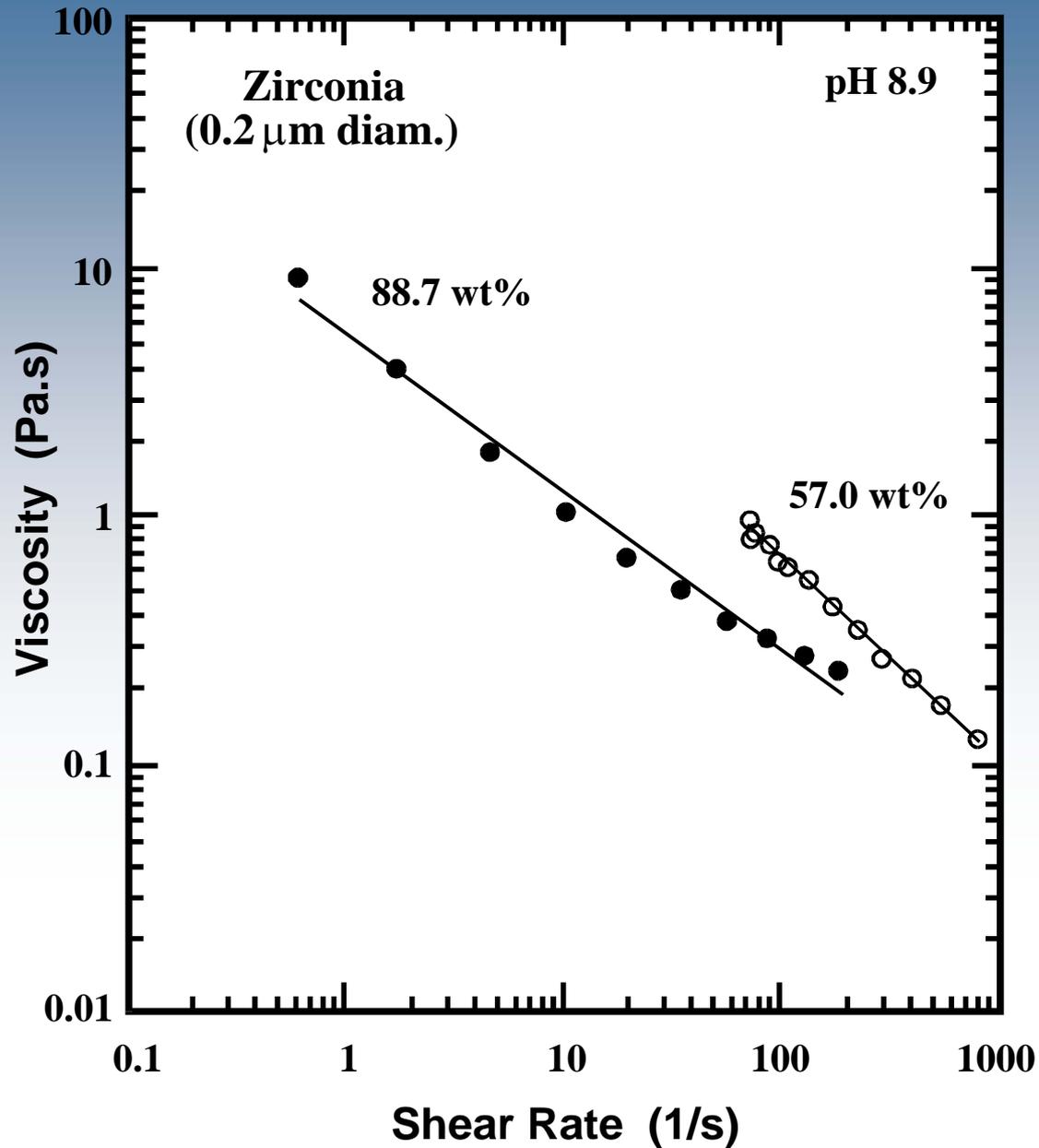
# Kaolin Rheology



# Effect of Low Molecular Weight Polyacrylic Acid on the Shear Yield Stress - pH behaviour for a Zirconia Suspension at 57wt%



# Manipulating the Flow Characteristics of Particulate Fluids





**20g clay in 60g H<sub>2</sub>O**  
**25% solids**

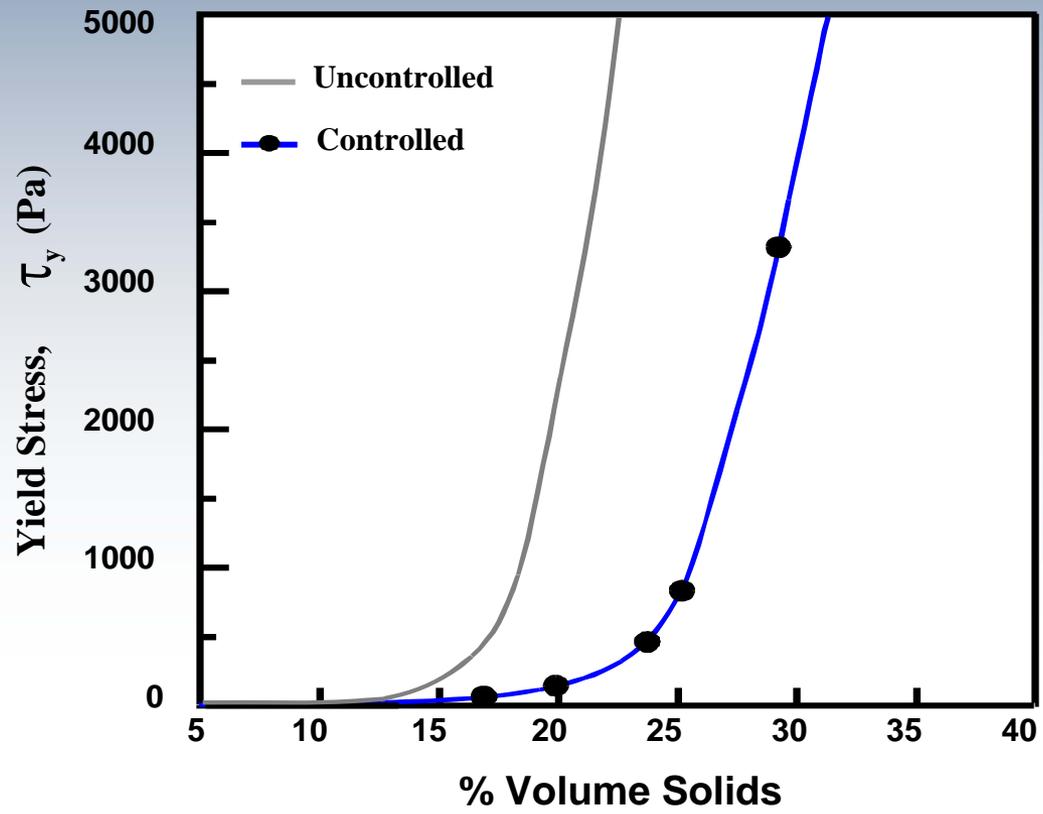


**Uncontrolled Dispersion**  
**25% solids in 1 M CaCl<sub>2</sub>**

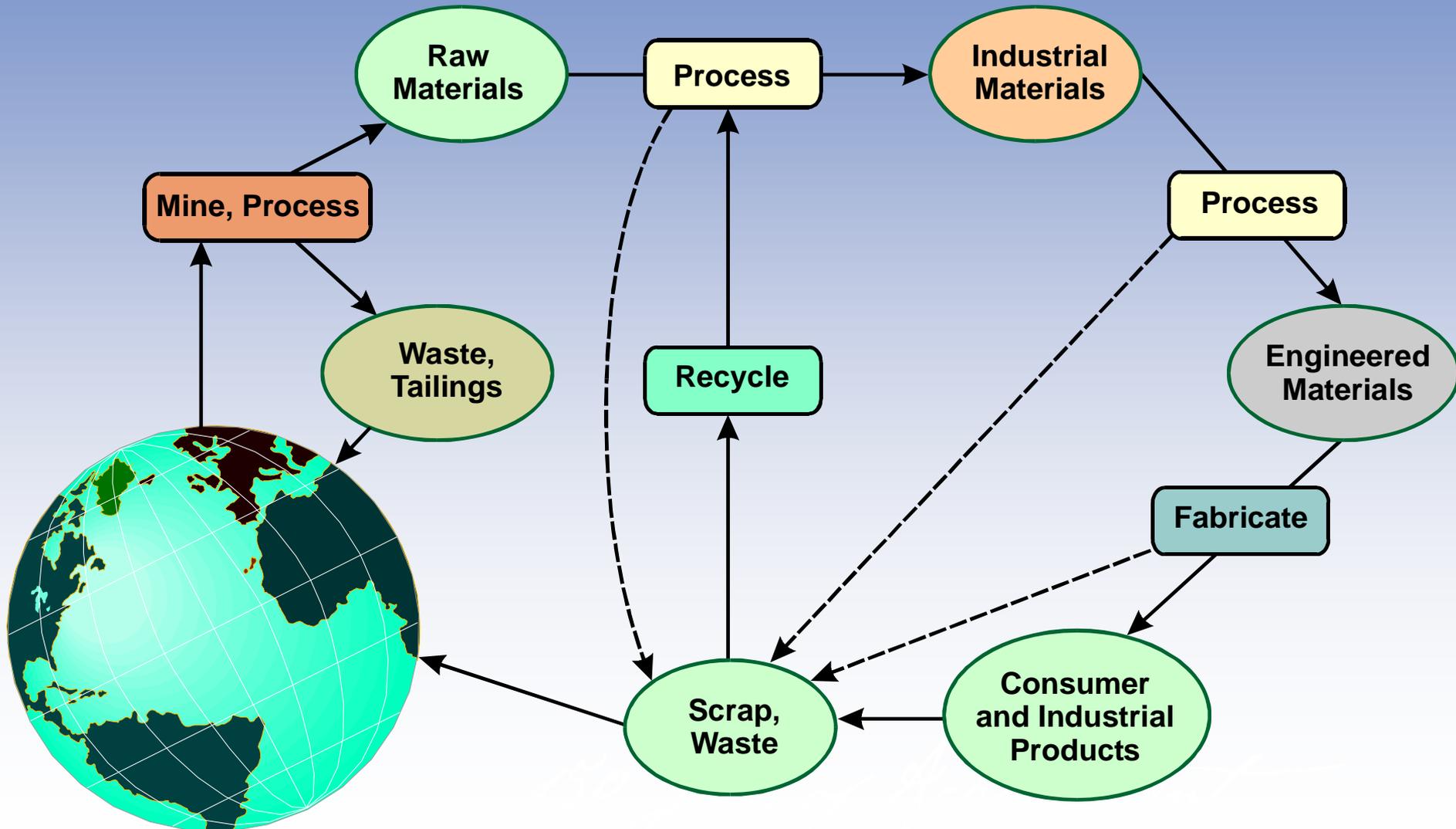


**Controlled Dispersion**  
**25% solids in 1 M CaCl<sub>2</sub>**

# Effect on Yield Stress vs Volume Fraction Behaviour for Clay Dispersed in $\text{CaCl}_2$ and Clay Dispersed in Water with $\text{CaCl}_2$ added later.



# Sustainability, Recycling and Environmental Modelling





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*Photo by Stuart Kirsch, 1996.*

**This forest was killed by dieback after being smothered with mine waste.  
It is on the lower Ok Tedi River near Dome Village.**



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# *In-pit Fill*



# Environmental Policy and Tailings Disposal

Bob Watts

Chief Scientist and Vice President Technology

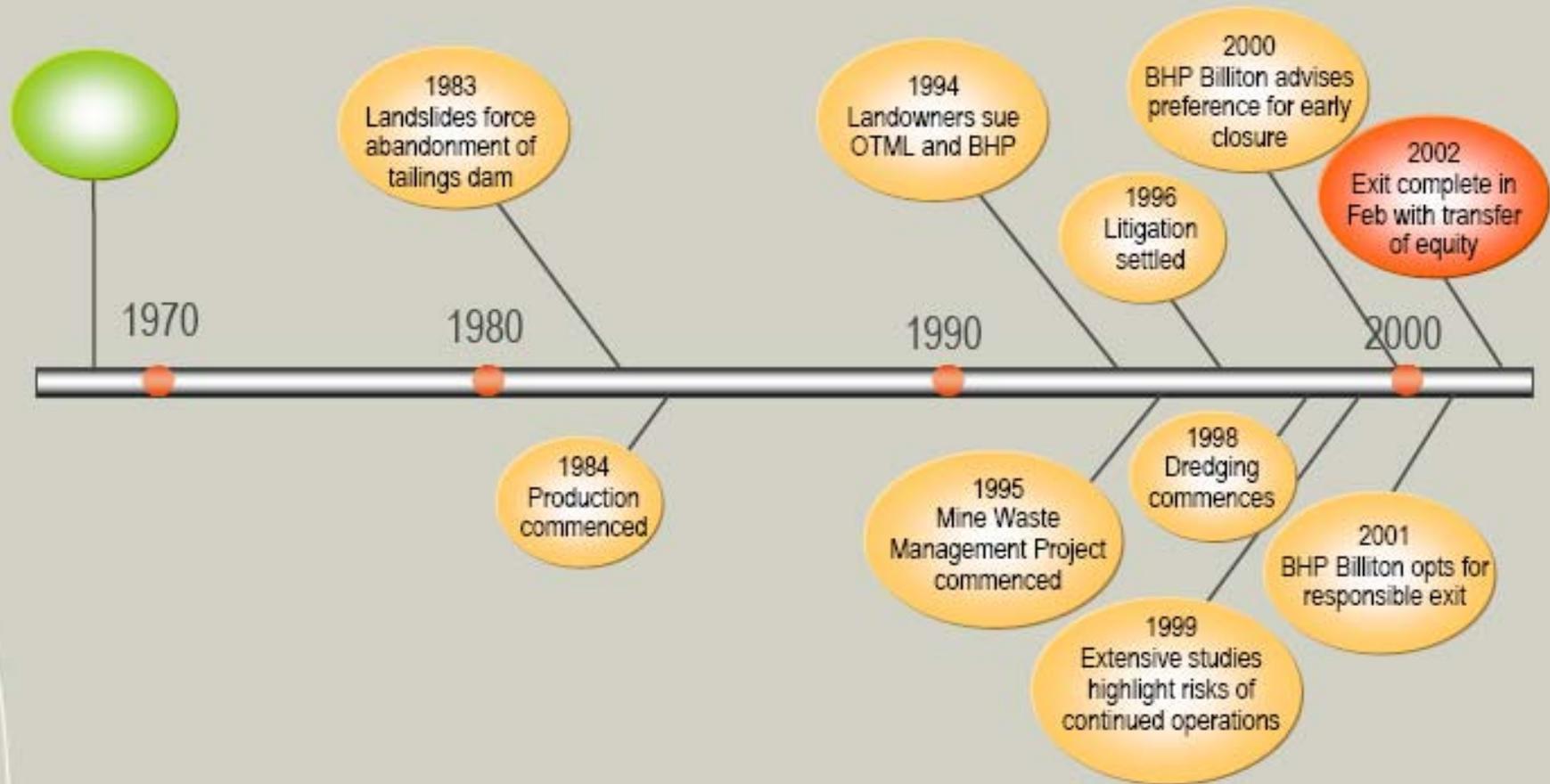
BHP Billiton



bhpbilliton

[Main Menu](#)

# Ok Tedi Copper Mine in PNG

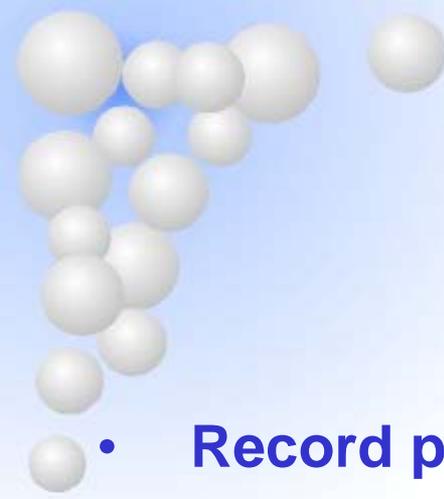




*Photo by Stuart Kirsch, 1996.*

**This forest was killed by dieback after being smothered with mine waste.  
It is on the lower Ok Tedi River near Dome Village.**





# OK TEDI UPDATE

- Record profit – US\$318.8 million – a 23% increase on previous year
- “...we are concerned that OTML’s environmental monitoring indicated that the environmental impact of the mine may prove to be greater than previously understood.”  
(Managing Director, Keith Faulkner)
- “In February 2005, areas of acid rock drainage were appearing on the levees of the Fly River.....”



© 2006 Europa Technologies  
Image © 2006 TerraMetrics  
Image © 2006 NASA

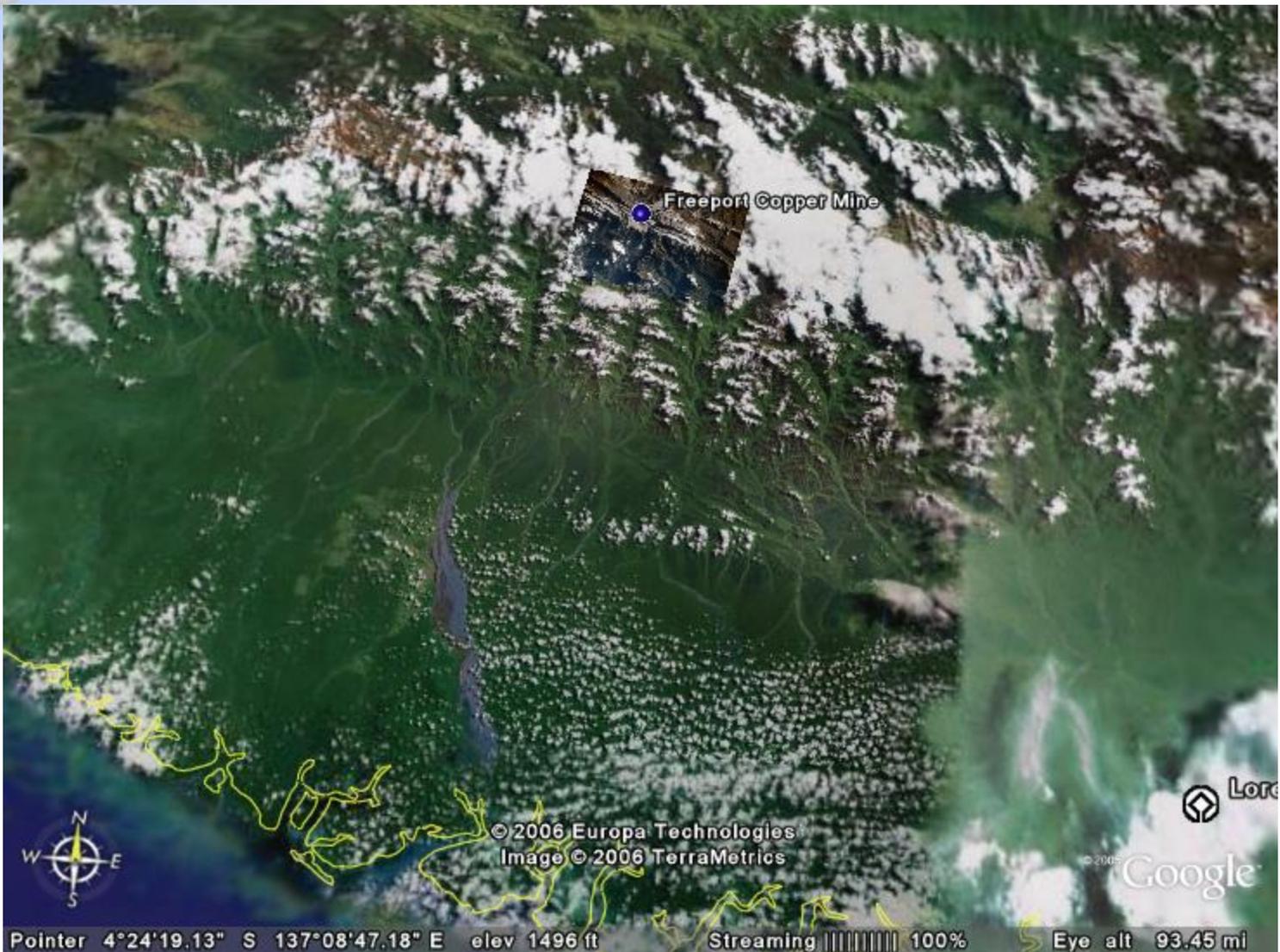
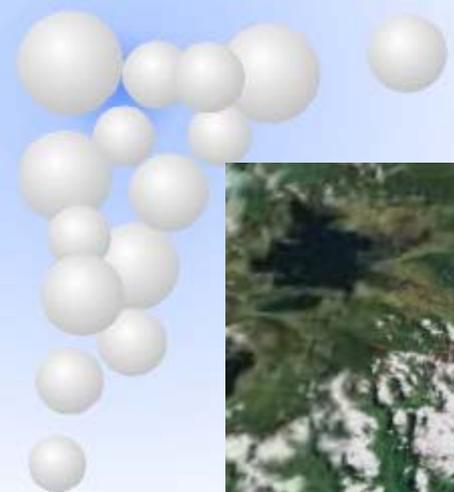
© 2005 Google

Pointer 4°24'19.62" S 137°08'47.22" E elev 1669 ft Streaming ||||| 100%

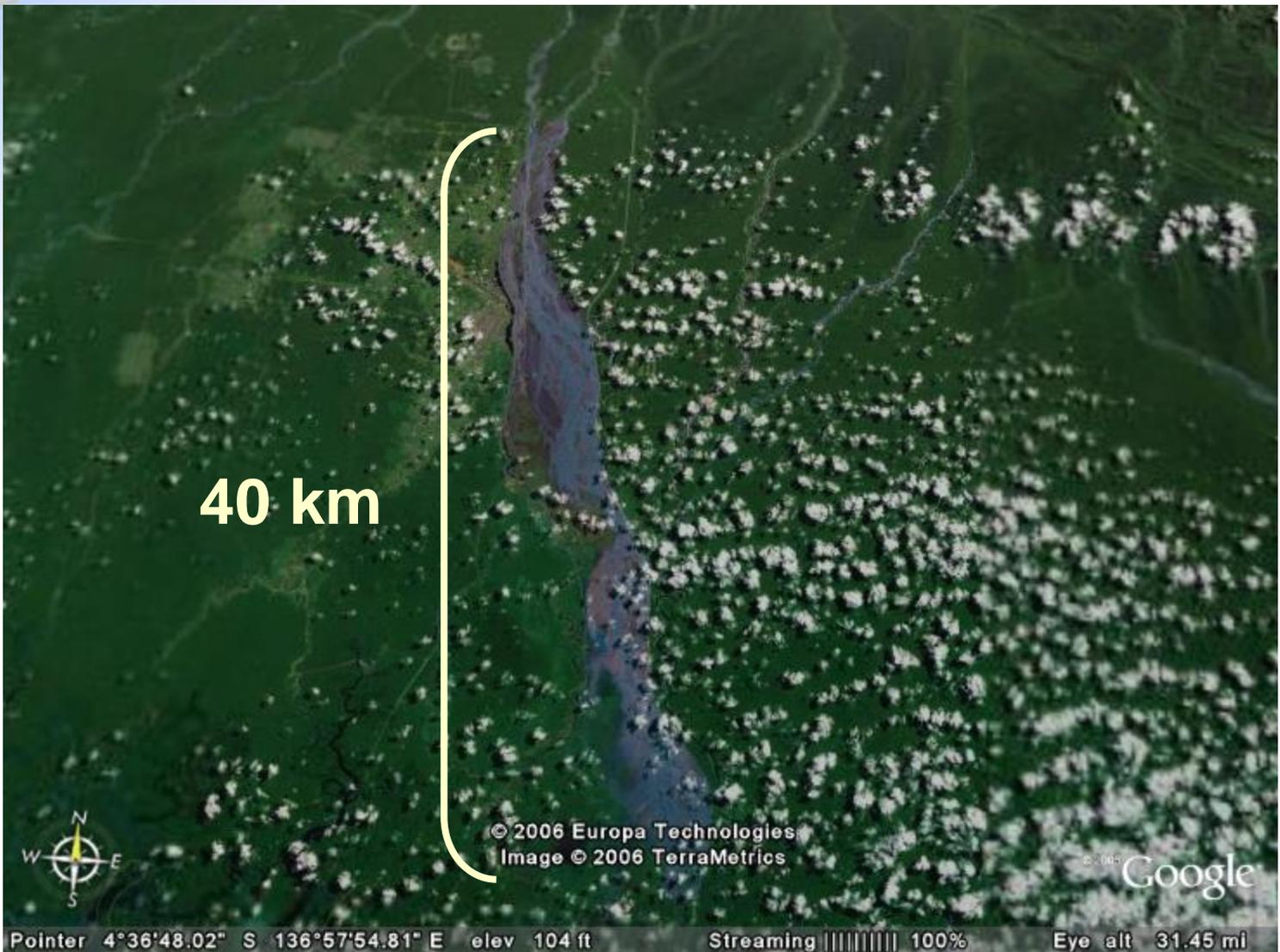
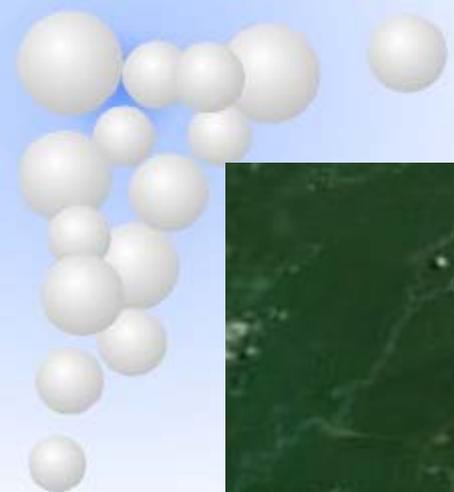
Eye alt 776.00 mi



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Pointer 4°24'19.13" S 137°08'47.18" E elev 1496 ft Streaming 100% Eye alt 93.45 mi



40 km

Pointer 4°36'48.02" S 136°57'54.81" E elev 104 ft Streaming ||||| 100% Eye alt 31.45 mi

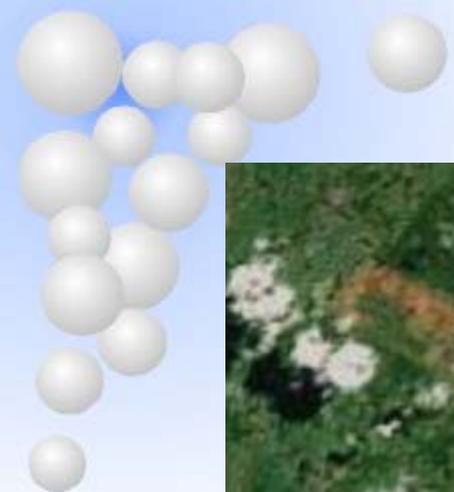


Image © 2006 TerraMetrics

©2006 Google

Pointer 4°33'14.42" S 136°55'02.67" E elev 88 ft Streaming ||||| 100% Eye alt 33287 ft

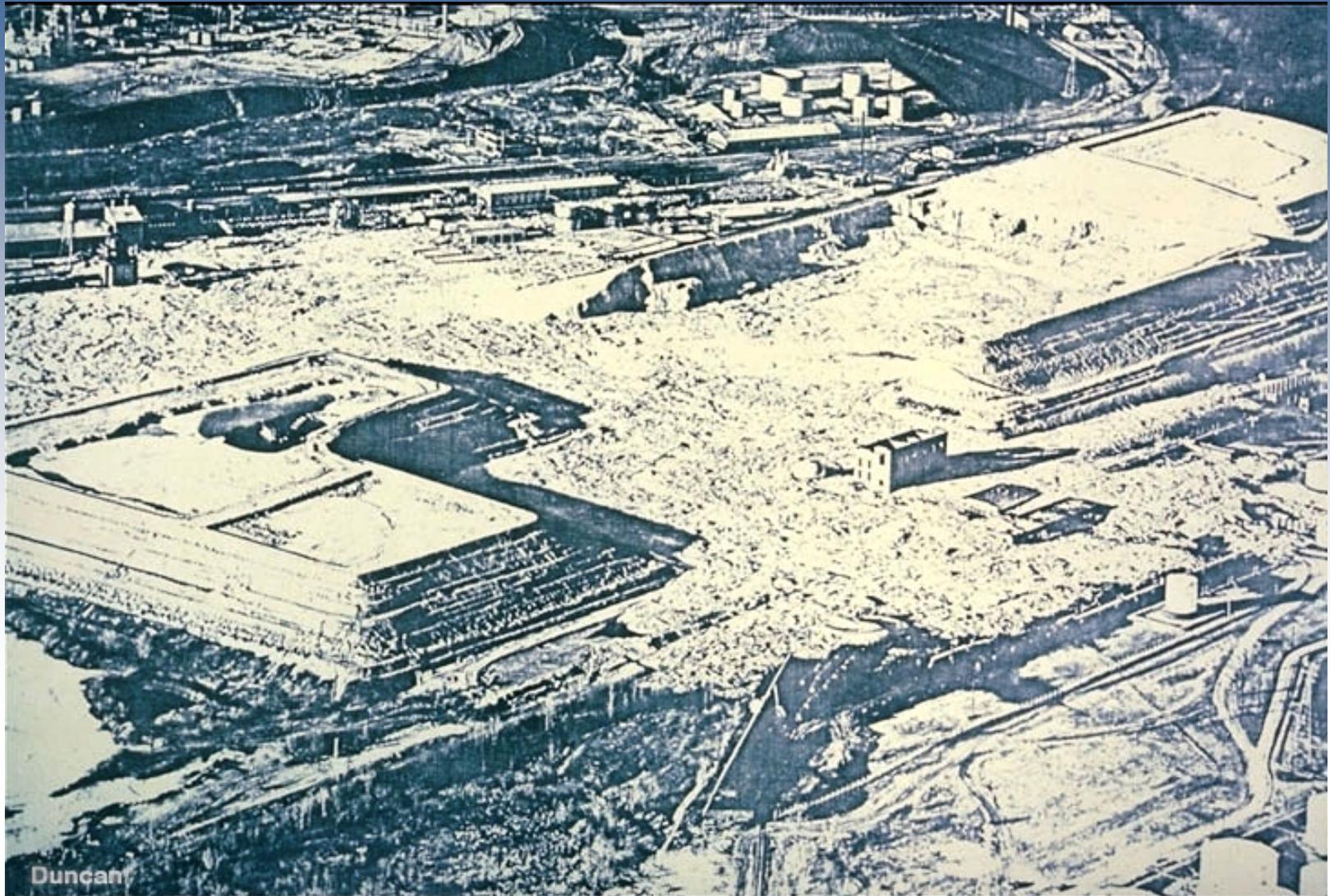




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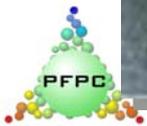
**Failure of dam holding platinum tailings in South Africa**



**Failure of a carbide tailings pond near Louisville, Kentucky.**

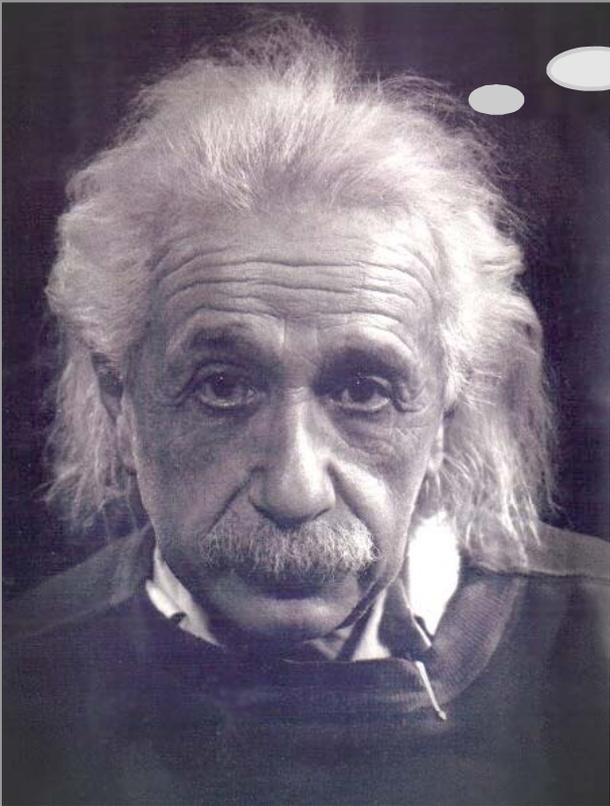


**Failure of dam retaining gypsum tailings in Florida**

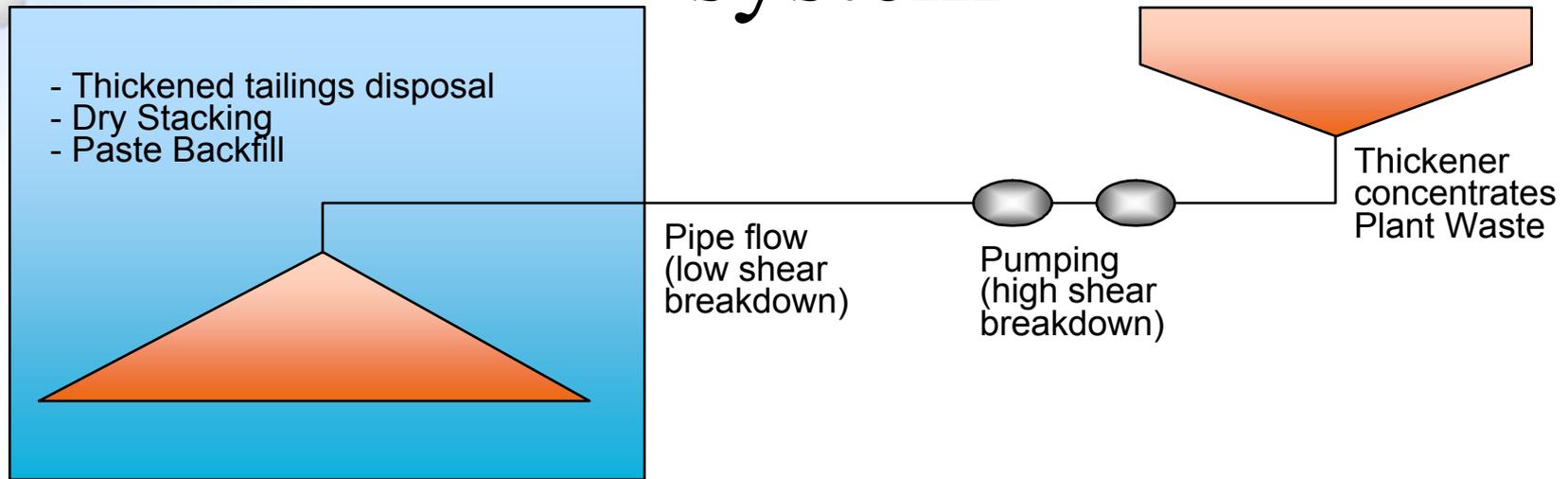


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A problem cannot be solved with the same kind of thinking that created it...



# Suggested approach for determination of tailings disposal system



## DESIGN SEQUENCE

1. Choice of disposal method, Depositional requirements.
2. Rheology requirements for pipeline transport.
3. Thickener design.

# New Developments

## □ Compression Rheology

- Compressive Yield Stress
- Permeability

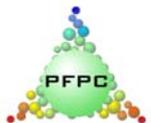
See: BSR Annual Rheology Review 2002:  
Compressive Rheology: An Overview,  
Ross G. de Kretser, David V. Boger  
and Peter J. Scales





# Rheology – Changing thinking in the minerals industry

D V Boger  
Laureate Professor  
The University of Melbourne  
Victoria, Australia

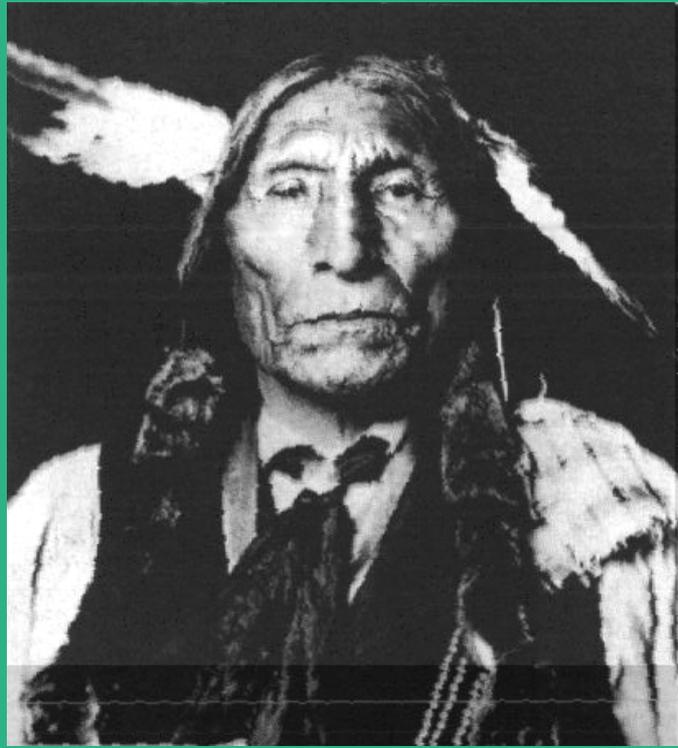


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# Paste and Thickened Tailings Seminars

- Edmonton, Canada, November 1999 hosted by the University of Alberta
- Perth, Australia, April 2000 hosted by the Australian Centre for Geomechanics
- Edmonton, Canada, October 2000 hosted by the University of Alberta
- Pilanesberg, South Africa, May 2001 hosted by the University of the Witwatersrand
- Santiago, Chile, April 2002 hosted by the Instituto de Ingenieros de Minas de Chile and Gecamin Ltda
- Melbourne, Australia, May 2003 hosted by the Australian Centre for Geomechanics and the University of Melbourne
- Cape Town, South Africa, March 2004 hosted by the University of the Witwatersrand and Paterson and Cooke Consulting Engineers Pty Ltd
- Santiago, Chile, April 2005 hosted by the University of Chile
- Limerick, Ireland, April 2006 hosted by Leeds University, Dorr-Oliver EIMCO and Golder Associates (UK) Ltd
- Perth, Australia, March 2007 hosted by the Australian Centre for Geomechanics

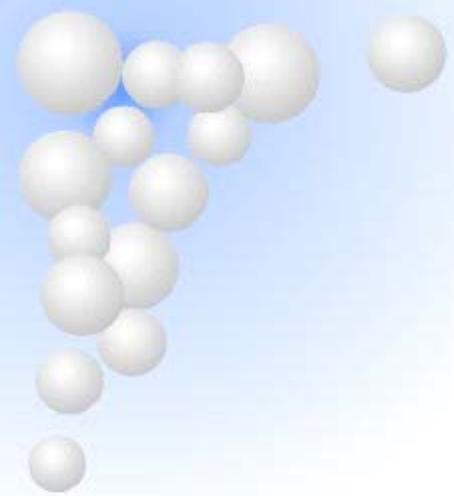
 **Rheology discovered!**



**Wolf Robe (June 1909)**

**"Only when the last tree has died  
and the last river has been poisoned  
and the last fish been caught  
will we realise  
we cannot eat money."**

*Cree Indian saying*





*Sustainable Development is the  
Simultaneous Striving for Economic Prosperity,  
Environmental Health and Social Well-being.*



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*“Environmental considerations dictate that we must manipulate tailings to fit a particular environment rather than manipulating the environment to contain the tailings.”*

*Understanding and exploiting the rheology of tailings helps us do this.*





# The Regulatory Trend

**“It is interesting to observe that many times more technical effort is devoted to ground water and toxicological studies for abandoned deposits than was ever allocated for their original design and generation.**

**Unfortunately much of the cost has been borne by government; should we then be surprised that responsible government is therefore imposing much greater regulatory security?”**

**S.G. Virk, 1990**



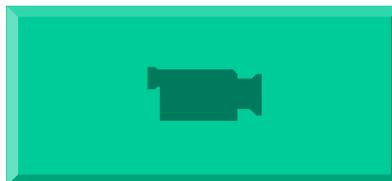
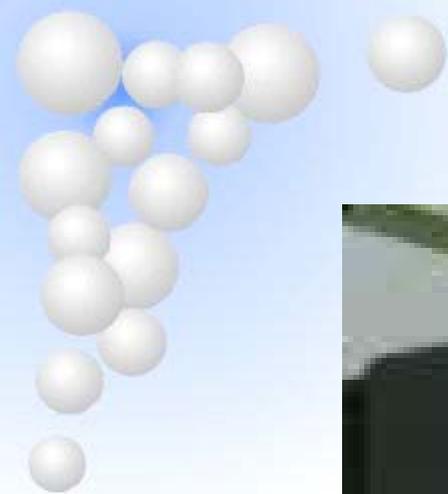
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*Rheological Consulting Services*

# **Rheological Consulting Services Pty. Ltd.**

- ❖ **Australia**
- ❖ **Canada**
- ❖ **Chile**
- ❖ **Jamaica**
- ❖ **New Guinea**
- ❖ **South Africa**
- ❖ **USA**
- ❖ **New Caledonia**
- ❖ **Indonesia**





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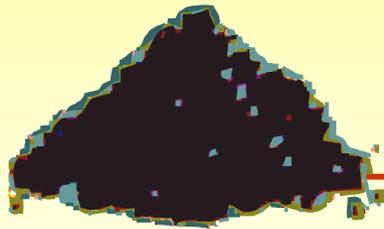
***The evidence is getting stronger that what is good for sustainable development can also be good for business, in sometimes surprising ways.***

***Business, society and the environment can "succeed" simultaneously.***

# Processing

# Products

Ore



Tailings



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